

# Effect of Oxygen Partial Pressure on the Formation Mechanisms of Complex Ca-rich Ferrites

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The formation mechanisms of the complex Ca-rich ferrite iron ore sinter bonding phases SFCA and SFCA-I, during heating of a synthetic sinter mixture in the range 298–1623 K and at  $pO_2 = 0.21$ ,  $5 \times 10^{-3}$  and  $1 \times 10^{-4}$  atm, were determined using *in situ* X-ray diffraction. SFCA and, in particular, SFCA-I are desirable bonding phases in iron ore sinter, and improved understanding of the effect of parameters such as  $pO_2$  on their formation may lead to improved ability to maximise their formation in industrial sintering processes. SFCA-I and SFCA were both observed to form at  $pO_2 = 0.21$  and  $5 \times 10^{-3}$  atm, with the formation of SFCA-I preceding SFCA formation in each case, but via distinctly different mechanisms at each  $pO_2$ . No SFCA-I was observed at  $pO_2 = 1 \times 10^{-4}$  atm; instead, a Ca-rich phase designated  $CF_{AlSi}$ , formed at 1420 K. By 1456 K,  $CF_{AlSi}$  had decomposed to form melt and a small amount of SFCA. Such a low  $pO_2$  during heating of industrial sinter mixtures is, therefore, undesirable, since it would not result in the formation of an abundance of SFCA and SFCA-I bonding phases. In addition, CFA phase, which was determined by Webster *et al.* (*Metall. Mater. Trans. B*, 43(2012), 1344) to be a key precursor phase in the formation of SFCA at  $pO_2 = 5 \times 10^{-3}$  atm, was also observed to form at  $pO_2 = 0.21$  and  $1 \times 10^{-4}$  atm, with the amount decreasing with increasing  $pO_2$ .

KEY WORDS: iron ore sinter; complex Ca-rich ferrite sinter bonding phases; SFCA and SFCA-I; *in situ* X-ray diffraction; oxygen partial pressure; phase formation mechanisms; synchrotron X-ray diffraction.

## 1. Introduction

Iron ore < 6.3 mm in size is too fine for direct use in a blast furnace and must first be agglomerated into iron ore sinter. Sinter is often the major component of blast furnace burden, and the production of high quality sinter is important for efficient blast furnace operation. During the iron ore sintering process, these iron ore fines are mixed with fluxes (*e.g.* limestone) and coke breeze and rapidly heated in 2–4 min to temperatures of  $\sim 1573$  K, followed by slower cooling in air.<sup>1)</sup> This results in partial melting of the mixture and converts the loose raw materials into a porous but physically strong composite material in which the iron-bearing minerals (40–70 vol% hematite,  $Fe_2O_3$ , and magnetite,  $Fe_3O_4$ ) are bonded together by a matrix containing complex Ca-rich ferrite phases (20–50 vol%), glasses (quenched melt) and calcium silicates (each up to 10 vol%).<sup>2)</sup> Oxygen partial pressure ( $pO_2$ ) values range from reducing during the initial stages of sintering as the coke breeze is consumed to oxidising during cooling.<sup>3,4)</sup>

The complex Ca-rich ferrite bonding phases typically also contain some silica and alumina and are known collectively by the acronym ‘SFCA’, which stands for Silico-Ferrite of

Calcium and Aluminium.<sup>5)</sup> Other ferrite phases observed in industrial sinters include monocalcium ferrite,  $CaO \cdot Fe_2O_3$  (abbreviated to CF), dicalcium ferrite,  $2CaO \cdot Fe_2O_3$  ( $C_2F$ ), hemicalcium ferrite,  $CaO \cdot 2Fe_2O_3$  ( $CF_2$ ) and brownmillerite ( $2CaO \cdot (Al_2O_3) \cdot (Fe_2O_3)$ ),  $C_2AF$ , *i.e.*  $A = Al_2O_3$ ).<sup>6)</sup> SFCA phases are believed to be the most desirable bonding phases in iron ore sinter because of their high reducibility,<sup>7)</sup> high mechanical strength and low reduction degradation,<sup>8,9)</sup> all of which are significant factors in determining the productivity and efficiency of the blast furnace.

The SFCA produced in iron ore sinter has, in the past, been divided on the basis of composition, structure and morphology into two main types. One is a high-Fe, low-Si form called SFCA-I, which has been described as having a platy morphology but also as being acicular. Mumme *et al.*<sup>10)</sup> reported that an SFCA-I found in plant sinter contained 84 mass%  $Fe_2O_3$ , 13 mass% CaO, 1 mass%  $SiO_2$  and 2 mass%  $Al_2O_3$ , and also synthesised material with the SFCA-I structure which had composition 83.15 mass%  $Fe_2O_3$ , 12.61 mass% CaO and 4.24 mass%  $Al_2O_3$ . The second ‘SFCA’ type is a low-Fe form that is simply referred to as SFCA and which exhibits a prismatic or columnar morphology in polished sections. SFCA found in industrial, plant sinters typically contains 60–76 mass%  $Fe_2O_3$ , 13–16 mass% CaO, 3–10 mass%  $SiO_2$ , 4–10 mass%  $Al_2O_3$  and 0.7–1.5 mass% MgO.<sup>11,12)</sup> Patrick and Pownceby<sup>13)</sup> systematically resolved

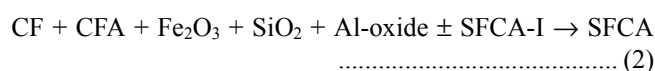
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the equilibrium solid solution range and thermal stability of SFCA within the quaternary system  $\text{Fe}_2\text{O}_3\text{--CaO--SiO}_2\text{--Al}_2\text{O}_3$  in air at 1513–1663 K. More recently a third SFCA with composition 67.3 mass%  $\text{Fe}_2\text{O}_3$ , 12.3 mass% CaO and 20.4 mass%  $\text{Al}_2\text{O}_3$  and designated SFCA-II was reported by Mumme.<sup>14)</sup> It has been reported to be present in plant sinters from South Africa.<sup>15,16)</sup>

McAndrew and Clout<sup>17)</sup> suggested that the texture of intersecting microplates of SFCA-I imparts superior strength and easier reducibility, and sinters containing significant amounts of this phase are of high quality. By comparison, sinters containing high amounts of prismatic SFCA, which is usually associated with glass, are typically weaker, have lower reducibility and are generally of lower quality. The effect of SFCA-II on strength and reducibility of iron ore sinter is unknown.

A large number of investigations<sup>2,3,18–25)</sup> have aimed to determine the formation mechanisms of complex Ca-rich ferrite phases. Increased understanding of the mechanisms has the potential to improve the efficiency of the sintering process by a) being able to predict the optimal sintering conditions (temperature,  $p\text{O}_2$ ) to produce high quality product based on the chemical and physical composition of the iron ore fines, and b) being able to predict the chemical and physical modifications of a particular iron ore fines mixture required to produce high quality product. Both are becoming increasingly important as the total iron content in many iron ores is decreasing and the concentration of alumina and silica-containing gangue minerals is increasing.

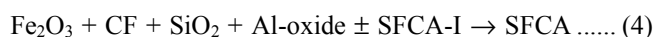
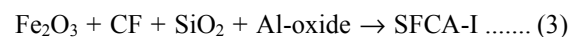
In the most recent of these mechanistic investigations, Webster *et al.*<sup>25)</sup> implemented *in situ* X-ray diffraction (XRD) in order to determine the SFCA and SFCA-I formation mechanisms in synthetic iron ore sinter mixtures, containing 1, 5 and 10 mass%  $\text{Al}_2\text{O}_3$ , in the range 298–1623 K and at an oxygen partial pressure of  $5 \times 10^{-3}$  atm. The selection of the  $p\text{O}_2$  was based on work of Hsieh and Whiteman,<sup>2)</sup> where it was shown that this oxygen partial pressure maximised the formation of Ca-rich ferrite phases, whilst producing mineral assemblages similar to those found in industrial sinters. Webster *et al.*<sup>25)</sup> showed that during heating, SFCA-I formation was associated with reaction between  $\text{Fe}_2\text{O}_3$ ,  $\text{SiO}_2$  and  $\text{Al}_2\text{O}_3$ -substituted  $\text{C}_2\text{F}$  [*i.e.*  $\text{C}_2(\text{F}_{1-x}\text{A}_x)$ ]. In contrast, SFCA formation was associated with reaction between CF,  $\text{SiO}_2$  and a phase designated CFA which had average composition 71.7 mass%  $\text{Fe}_2\text{O}_3$ , 12.9 mass% CaO, 0.3 mass%  $\text{SiO}_2$  and 15.1 mass%  $\text{Al}_2\text{O}_3$ . The initial formation of SFCA at  $\sim 1433$  K was independent of SFCA-I, however at higher temperature ( $T > 1473$  K) SFCA-I was consumed in the formation of SFCA. Eqs. (1) and (2) (unbalanced) summarise the reactions involved in the formation of SFCA-I and SFCA determined by Webster *et al.*<sup>25)</sup> (the ‘ $\pm$ ’ in Eq. (2) represents the initial formation of SFCA being independent of SFCA-I).



Increasing  $\text{Al}_2\text{O}_3$  concentration in the starting sinter mixture increased the temperature range over which SFCA-I was stable before the initial formation of SFCA. Increasing  $\text{Al}_2\text{O}_3$

concentration also increased the stability range of SFCA before it melted to form a  $\text{Fe}_3\text{O}_4$  + melt phase assemblage.

The formation of CFA during heating had not been described in a previous *in situ* XRD investigation of reaction sequences in the formation of SFCA phases, which was performed under vacuum in the range 298–1533 K by Scarlett *et al.*<sup>23,24)</sup> Eqs. (3) and (4) summarise the reactions involved in the formation of SFCA-I and SFCA determined by Scarlett *et al.*:



Based on the absence of  $\text{Fe}_3\text{O}_4$  in the study of Scarlett *et al.*<sup>23,24)</sup> it was inferred by Webster *et al.*<sup>25)</sup> that the oxygen partial pressure was somewhere in the range  $0.21 - 5 \times 10^{-3}$  atm, and it was speculated that  $p\text{O}_2$  may affect the formation of CFA. Given that CFA was a precursor phase involved in the formation of the SFCA phases in the study of Webster *et al.*<sup>25)</sup> it is also likely that  $p\text{O}_2$  would exert an influence on the formation mechanisms of SFCA and SFCA-I during heating. The purpose of the current investigation was to determine the effect of  $p\text{O}_2$  on the formation of CFA, and also on the formation of SFCA and SFCA-I bonding phases, during the heating of a synthetic sinter starting mixture. A series of *in situ* XRD and phase equilibria experiments were performed over the range 298–1623 K and at  $p\text{O}_2$  values of 0.21,  $5 \times 10^{-3}$  and  $1 \times 10^{-4}$  atm in order to characterise the phase evolution.

## 2. Experimental

### 2.1. Starting Sinter Mixture Preparation

The nominal concentration of the synthetic starting sinter mixture for the *in situ* XRD experiments, in terms of mass% of oxides, was 77.36, 14.08, 3.56 and 5.00 mass%  $\text{Fe}_2\text{O}_3$ , CaO,  $\text{SiO}_2$  and  $\text{Al}_2\text{O}_3$ , respectively. This mixture was equivalent to mixture SM4/5 previously investigated by Webster *et al.*<sup>25)</sup> and was designed to maximise the formation of the SFCA phase.<sup>13)</sup> It was prepared from fine grained ( $< 20 \mu\text{m}$ ) synthetic  $\text{Fe}_2\text{O}_3$  (Acros Organics, 99.999%), calcite,  $\text{CaCO}_3$  (Thermo Fisher, 99.95%), quartz,  $\text{SiO}_2$  (Sigma Aldrich, 99.995), and gibbsite,  $\text{Al}(\text{OH})_3$  (Alcan OP25 Super White, 99.9%); these were mixed under acetone in a mortar and pestle. In terms of its relevance to a typical industrial iron ore sinter mixture of fines, flux and coke, this composition is indicative of the reactive ultra-fine coating component of the mixture ( $< \sim 1$  mm), rather than the bulk composition which also includes larger ‘nuclei’ ore particles.

### 2.2. In Situ XRD

*In situ* XRD experiments were performed using an INEL diffractometer, which incorporates a CPS120 position-sensitive detector allowing for simultaneous collection of up to  $120^\circ 2\theta$  of diffraction data. The Co tube was operated at 40 kV and 35 mA. An Anton Paar model HTK 10 high temperature chamber, employing a platinum resistance strip heater inside it, was positioned on the instrument (**Fig. 1**). A slurry of the sinter sample mixture and ethanol was prepared and placed into a sample well, measuring approximately  $20 \times 7 \times 0.2$  mm, on the platinum heater.

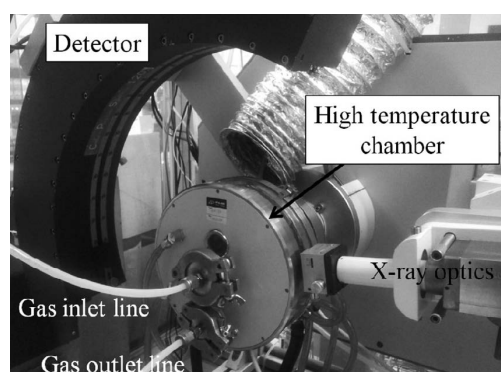


Fig. 1. The high temperature chamber fitted to the laboratory INEL X-ray diffractometer.

The experimental  $pO_2$  values of 0.21,  $5 \times 10^{-3}$  and  $1 \times 10^{-4}$  atm were obtained by flowing compressed air, and special gas mixtures containing 0.5 and 0.01%  $O_2$  in  $N_2$  (BOC Gases), respectively, into the Anton Paar chamber. Before each experiment the chamber was purged for 10 min by a flow ( $\sim 1 \text{ L min}^{-1}$ ) of the designated gas mixture, after which the sample was heated under a continuous flow of the gas.

A heating rate of  $20 \text{ K min}^{-1}$  was used from 298 to 873 K (approaching the decomposition temperature of  $CaCO_3$ ), then a slower rate of  $10 \text{ K min}^{-1}$  to 1 623 K was used during the period of SFCA-I and SFCA phase formation and melting. The temperature was measured by a Pt/PtRh10% thermocouple connected to the underside of the platinum strip. *In situ* XRD data were collected throughout heating, with individual datasets collected for 0.5 min. Data were collected in asymmetrical diffraction geometry with an incident beam angle of  $10^\circ$ , over the range  $10^\circ \leq 2\theta \leq 112^\circ$ . The temperatures of phase formation/transformation given throughout the manuscript are those at the start, which is when the temperatures were automatically recorded, of the relevant dataset. The uncertainty in these temperature values, therefore, was the difference between the temperatures at the start of successive datasets, and the magnitude of the uncertainty depended on the heating rate (*i.e.* 10 and 5 K for the 20 and  $10 \text{ K min}^{-1}$  heating regimes, respectively).

For the purposes of visualisation of the decomposition and formation of phases as the experiment progressed, the datasets were stacked to produce a plot of accumulated data with temperature plotted vs  $2\theta$ , viewed down the intensity axis (Figs. 2(a), 2(b) and 2(c)). Rietveld refinement was performed using TOPAS,<sup>26)</sup> with the crystal structure information provided in Blake *et al.*, Maslen *et al.*, Saalfeld and Wedde, Lager *et al.*, Oftedal, Bersetegui *et al.*, Decker and Kasper, and Hamilton used for  $Fe_2O_3$ ,  $CaCO_3$ ,  $Al(OH)_3$ ,  $SiO_2$ ,  $CaO$ ,  $C_2(F_{1-x}A_x)$ , CF and  $Fe_3O_4$ , respectively.<sup>27–34)</sup> Single peak fitting to extract reflection intensities was also performed using TOPAS, with reflections modelled using a pseudo-Voigt profile function. The background was modelled using a Chebychev polynomial function.

### 2.3. Heat/Quench Experiments and Microscopic Characterisation

Laboratory heat/quench experiments were performed in order to investigate key phases revealed by the *in situ* XRD experiments in more detail. For these experiments, 0.5 g of the starting sinter mixture was pelletised and heated in a

platinum crucible in a vertical tube furnace under the required  $pO_2$  condition, followed by water quenching. The temperature adjacent to the crucible was measured using a Pt/PtRh13% thermocouple connected to an ice-point cell, and the temperature is considered accurate to  $\pm 10 \text{ K}$ .

Scanning electron microscopy (SEM) was performed using a FEI Quanta 400 Field Emission Environmental SEM operated at an accelerating voltage of 10 kV and a working distance of 10 mm. Energy dispersive spectroscopy (EDS) was performed on this instrument using a Bruker X-Flash 5010 Si-drift EDS detector. Electron probe microanalysis (EPMA) was performed using a JEOL JXA-8900F Superprobe.  $Fe_2O_3$ , wollastonite ( $CaSiO_3$ , CS) and “Magalox” (a synthetic spinel, composition  $MgAl_2O_4$ ) were used as standards for the microprobe analyses which were conducted in wavelength dispersive mode using an accelerating voltage of 10 kV, a beam diameter of  $< 1 \mu\text{m}$  and counting times of 15 sec.

### 2.4. Synthesis and Characterisation of SFCA and SFCA-I Materials

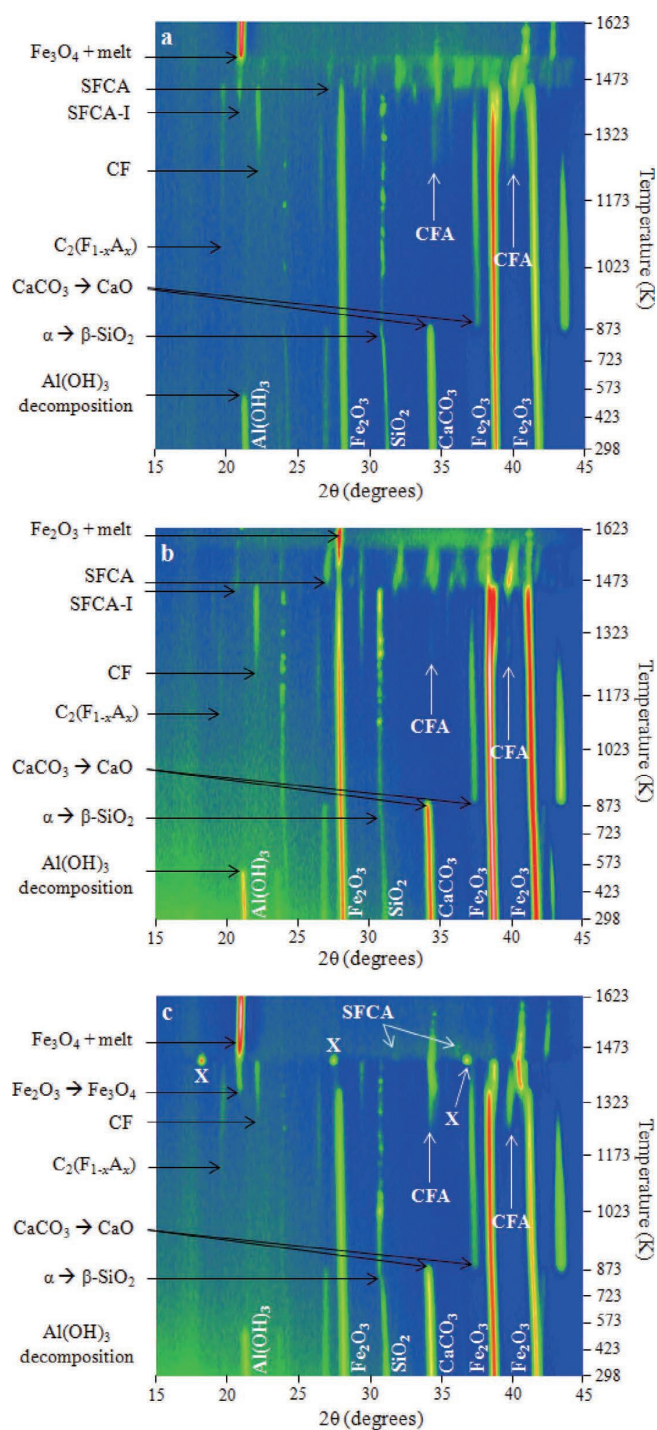
Synthesis of SFCA and SFCA-I materials, in order to investigate their structures in more detail, was carried out by heating pellets of the desired mixtures in a vertical tube furnace in air at 1 533 K for 24 hr. This was followed by air quenching, grinding, re-pelletising, and reheating for a further 24 hr followed by air quenching. This process was repeated to produce the final materials with a total heating time of 72 hr. EPMA data were collected using the procedure in Section 2.3.

Synchrotron XRD (S-XRD) data were collected for these materials, at room temperature on the powder diffraction beamline at the Australian Synchrotron<sup>35)</sup> over the range  $2^\circ \leq 2\theta \leq 82.5^\circ$ . Samples were contained within 0.3 mm glass capillaries which were continuously rotated during data collection to improve particle statistics and to reduce the effects of preferred orientation. The X-ray wavelength was  $0.7279 \text{ \AA}$ , calibrated using  $LaB_6$  (NIST 660b line position and profile standard) contained in a 0.3 mm ID capillary. Pawley refinements<sup>36)</sup> of the S-XRD data were performed using TOPAS. The triclinic ( $P\bar{1}$ ) unit cell information for SFCA ( $a = 9.050$ ,  $b = 10.025$ ,  $c = 10.927 \text{ \AA}$ ,  $\alpha = 60.46$ ,  $\beta = 73.79$ ,  $\gamma = 65.94^\circ$ ) and SFCA-I ( $a = 10.431$ ,  $b = 10.610$ ,  $c = 11.839 \text{ \AA}$ ,  $\alpha = 94.14$ ,  $\beta = 111.35$ ,  $\gamma = 110.27^\circ$ ) described by Mumme *et al.*<sup>10)</sup> were used as the starting parameters for the refinements.

For determination of  $Fe^{2+}$  content, the materials were dissolved with hydrofluoric and hydrochloric acids. The resulting solutions were then titrated to the electrochemical equivalence point against a standard dichromate solution using a 798 Metrohm MPT Titrino autotitrator. The  $Fe^{2+}$  content was calculated from the titre volumes.

### 3. Results and Discussion

Figure 2(a) shows the plot of accumulated *in situ* XRD data for the  $pO_2 = 5 \times 10^{-3}$  atm experiment. The results, in terms of the phases observed and the temperature range of their stability, are in excellent agreement with those reported previously by Webster *et al.*<sup>25)</sup> for the corresponding experiment for this sinter mixture composition performed at the Australian Synchrotron and for which the reaction mecha-



**Fig. 2.** *In situ* XRD data collected at a)  $pO_2 = 5 \times 10^{-3}$  atm, b) 0.21 atm and c)  $1 \times 10^{-4}$  atm. Annotated on the plots are: the major reflections for materials in the starting mixture; the low-temperature ( $< 923$  K) phase transformation ( $\alpha \rightarrow \beta$ -SiO<sub>2</sub>) and decomposition (e.g. CaCO<sub>3</sub> → CaO) events; the formation events of C<sub>2</sub>(F<sub>1-x</sub>A<sub>x</sub>), CF, SFCA-I, SFCA, the Fe<sub>3</sub>O<sub>4</sub> + melt phase assemblage (for a and c), and the Fe<sub>2</sub>O<sub>3</sub> + melt phase assemblage (for b); and the major reflections for CFA. X denotes the reflections for the unknown phase (for c).

nisms presented in Eqs. (1) and (2) applied. More specifically, Al(OH)<sub>3</sub> decomposition to an amorphous Al-oxide was complete by 562 K, transformation of the  $\alpha$ -form of SiO<sub>2</sub> to  $\beta$ -SiO<sub>2</sub> was complete by 845 K (in excellent agreement with the 846 K reported by Kihara,<sup>37</sup>) which gives a high level of confidence in the accuracy of the thermocouple), and decomposition of CaCO<sub>3</sub> to CaO was complete by

**Table 1.** Temperatures of formation of the significant phases and phase assemblages observed in the *in situ* XRD data collected at  $pO_2 = 0.21, 5 \times 10^{-3}$  and  $1 \times 10^{-4}$  atm.

$pO_2$ (atm)	Temperature (K)					
	C <sub>2</sub> (F <sub>1-x</sub> A <sub>x</sub> )	CF/CFA	SFCA-I	X (i.e. CF <sub>AISI</sub> )	SFCA	Fe <sub>3</sub> O <sub>4</sub> + melt/ Fe <sub>2</sub> O <sub>3</sub> + melt
0.21	1027	1223	1416	–	1446	1594
$5 \times 10^{-3}$	1037	1243	1377	–	1441	1532
$1 \times 10^{-4}$	1027	1230	–	1420	1438	1479

883 K. The first Ca-rich ferrite to form was C<sub>2</sub>(F<sub>1-x</sub>A<sub>x</sub>) at 1037 K, followed by CF and CFA at 1243 K, SFCA-I at 1377 K, and SFCA at 1441 K. Melting of both SFCA-I and SFCA was complete by 1532 K, after which the Fe<sub>3</sub>O<sub>4</sub> + melt phase assemblage had formed. Fe<sub>3</sub>O<sub>4</sub> formed as a result of incongruent melting of SFCA, since Fe<sub>2</sub>O<sub>3</sub> was fully consumed in the reactions to form the ‘SFCA’ phases by 1472 K, which is before the predicted Fe<sub>2</sub>O<sub>3</sub> → Fe<sub>3</sub>O<sub>4</sub> transformation temperature of 1513 K.<sup>38</sup>) **Table 1** summarises the formation temperatures of these phases and phase assemblages.

Figures 2(b) and 2(c) show the plots of accumulated *in situ* XRD data for the experiments conducted at  $pO_2 = 0.21$  and  $1 \times 10^{-4}$  atm, respectively. The low temperature ( $< 923$  K) phase decomposition and transformation events are very similar to those in Fig. 2(a). Oxygen partial pressure, therefore, does not have a significant effect on these events. In addition,  $pO_2$  does not have a significant effect on the initial formation temperature of C<sub>2</sub>(F<sub>1-x</sub>A<sub>x</sub>) and CF (Table 1).

In contrast, however,  $pO_2$  did have an effect on the stability of Fe<sub>2</sub>O<sub>3</sub>. At  $pO_2 = 1 \times 10^{-4}$  atm, Fe<sub>3</sub>O<sub>4</sub> formed through the Fe<sub>2</sub>O<sub>3</sub> → Fe<sub>3</sub>O<sub>4</sub> reduction reaction which was complete by 1367 K, in good agreement with the theoretical value of 1371 K.<sup>38</sup>) In the 0.21 atm experiment Fe<sub>3</sub>O<sub>4</sub> did not form, with Fe<sub>2</sub>O<sub>3</sub> remaining stable up to 1623 K. In air the Fe<sub>2</sub>O<sub>3</sub> → Fe<sub>3</sub>O<sub>4</sub> reduction reaction is predicted to occur within the range 1623–1682 K; the presence of labile Ca<sup>2+</sup> in the system will likely displace the reaction to lower temperature than the theoretical value of 1682 K.<sup>38,39</sup>)

### 3.1. CFA Formation

Similarly to the experiment at  $pO_2 = 5 \times 10^{-3}$  atm, characteristic CFA reflections were observed at  $pO_2 = 0.21$  and  $1 \times 10^{-4}$  atm, occurring at 34.5 and 39.9° 2 $\theta$  ( $d = 3.02$  and 2.62 Å, respectively, annotated in Figs. 2(b) and 2(c)). The reflections in the experiment at  $pO_2 = 0.21$  atm appeared to be of lower relative intensity to those in the other experiments, suggesting less CFA was formed under the more oxidising conditions. In the absence of previously published structural information for CFA necessary to perform Rietveld refinement-based quantitative phase analysis (QPA) of this phase, and also the absence of single-phase CFA material necessary to perform QPA using the PONKCS method,<sup>40</sup>) an alternative method was required in order to confirm that the amount of CFA formed at  $pO_2 = 0.21$  atm was less than at the other  $pO_2$  values. In the alternative approach, the intensity ( $I_{CFA}$ ) of the major CFA-phase reflection with  $d = 2.62$  Å was normalised by the intensity of the major Fe<sub>2</sub>O<sub>3</sub> reflection ( $I_{Hem}$ ) at 38.8° 2 $\theta$  in the dataset collected at room temperature. **Figure 3** shows  $I_{CFA}/I_{Hem}$  as a function of temper-

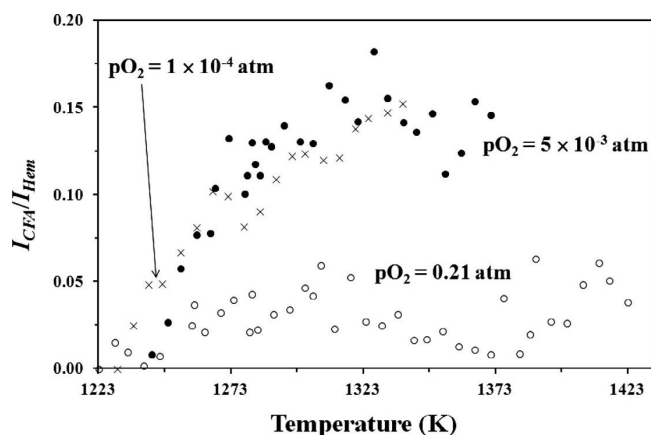


Fig. 3. The variation in normalised intensity,  $I_{CFA}/I_{Hem}$ , of the characteristic CFA reflection ( $d = 2.62 \text{ \AA}$ ) as a function of temperature and  $pO_2$ .

ature for each  $pO_2$ .

For the experiment at  $pO_2 = 5 \times 10^{-3}$  atm  $I_{CFA}/I_{Hem}$  is plotted from 1223 to 1371 K (*i.e.* just before the initial formation temperature of SFCA-I) due to significant overlap between the CFA and SFCA-I reflections. For the same reason  $I_{CFA}/I_{Hem}$  is plotted up to 1412 K for the  $pO_2 = 0.21$  atm experiment, while for the  $pO_2 = 1 \times 10^{-4}$  atm experiment it is plotted to 1338 K (*i.e.* just before the initial formation temperature of  $Fe_3O_4$ ), due to overlap between the CFA and  $Fe_3O_4$  reflections. Figure 3 confirms that the amount of CFA that formed at  $pO_2 = 0.21$  atm was less than at the more reduced  $pO_2$  values, and that the amount of CFA formed at  $pO_2 = 5 \times 10^{-3}$  and  $pO_2 = 1 \times 10^{-4}$  atm was similar.

### 3.2. SFCA and SFCA-I Phase Formation and Melting

Similar to the experiment at  $pO_2 = 5 \times 10^{-3}$  atm, SFCA-I and SFCA were observed to form at  $pO_2 = 0.21$  atm, at 1416 and 1446 K, respectively. Melting of both SFCA phases was complete by 1594 K, producing the  $Fe_2O_3$  + melt phase assemblage. For the  $pO_2 = 1 \times 10^{-4}$  atm experiment, very weak reflections for SFCA were observed; SFCA initially formed at 1438 K and was present until melting was complete by 1479 K producing the  $Fe_3O_4$  + melt phase assemblage. The decrease in melting point with decreasing  $pO_2$  is in agreement with previous work.<sup>39</sup> Characteristic reflections for SFCA-I were not observed for the  $pO_2 = 1 \times 10^{-4}$  atm experiment. Instead, reflections from an unknown phase (annotated with 'X' in Fig. 2(c)) were first observed at 1420 K and were present until decomposition of this phase was complete at 1456 K. No suitable match could be made between this phase and any phase within the Database of the International Centre for Diffraction Data (ICDD). However, based on the d-spacings of its reflections in Fig. 2(c) (5.66, 3.77 and 2.83  $\text{\AA}$  at 1431 K), it appears likely to have a simple cubic crystal structure. Further work is required to determine the details of its crystal structure.

Based on a comparison of the three experiments the effect of decreasing  $pO_2$  was to significantly decrease the thermal stability range of SFCA which was 1446–1594, 1441–1532 and 1438–1479 K at  $pO_2 = 0.21$ ,  $5 \times 10^{-3}$  and  $1 \times 10^{-4}$  atm, respectively (see Table 1). In contrast, the effect of decreasing oxygen partial pressure from 0.21 to  $5 \times 10^{-3}$  atm was to stabilise the formation of SFCA-I at a lower temper-

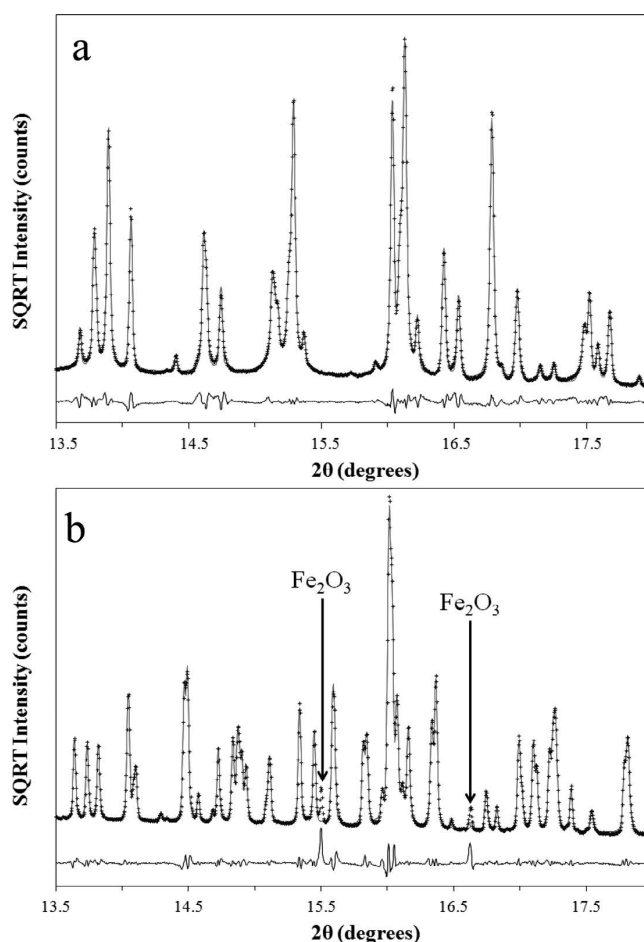


Fig. 4. Output of Pawley refinements to S-XRD data collected for a) SFCA; and b) SFCA-I synthesised at  $pO_2 = 0.21$  atm at 1533 K for 72 hr. The data are shown only at low  $2\theta$  values over a narrow angular range of the complete datasets. Experimental data are shown as plus signs, the calculated patterns are solid lines, and the difference patterns are the solid lines below.  $Fe_2O_3$  reflections are annotated on the SFCA-I plot.

Table 2. Summary of the EPMA compositional results, in terms of mass% oxides, for the SFCA and SFCA-I materials synthesised at  $pO_2 = 0.21$  atm at 1533 K for 72 hr. The numbers in parentheses are the standard deviations of  $\sim 30$  point analyses for each phase.

Sample	Composition (mass%)				
	$Fe_2O_3$	CaO	$SiO_2$	$Al_2O_3$	Total
SFCA	80.0 (1.2)	13.5 (0.3)	3.0 (0.2)	4.7 (0.1)	101.2 (1.2)
SFCA-I	83.5 (2.0)	12.9 (0.1)	0.0 (0.1)	5.0 (0.8)	101.5 (1.7)

ature, and it is hypothesised that SFCA-I may accommodate more  $Fe^{2+}$  into its structure than SFCA.

Following on from the latter observation it is noted that in SFCA and SFCA-I materials synthesised in air in the range 1473–1573 K by Mumme *et al.*,<sup>10</sup> the SFCA-I contained a higher amount of  $Fe^{2+}$  in its structure compared with SFCA. However, the assignment of the amount of  $Fe^{2+}$  was based purely on charge balance considerations, and a more rigorous analytical approach was required to determine whether this is indeed the case. Here, SFCA and SFCA-I materials were synthesised in air at 1533 K. Table 2 shows the EPMA-determined compositions for each. Figure 4 shows the output of



Pawley refinements to the high resolution S-XRD data collected for SFCA (Fig. 4(a)) and SFCA-I (Fig. 4(b)). The quality of the fit shown in Fig. 4(a) indicated that the SFCA was single phase; conversely the fit to the data collected for SFCA-I indicated the presence of a minor impurity phase, which was subsequently identified as  $\text{Fe}_2\text{O}_3$  (ICDD No. 33-0664).

Subsequent  $\text{Fe}^{2+}$  determination via titration showed that the bulk SFCA and SFCA-I materials contained 0.46(0.01) and 1.38(0.01) mass%  $\text{Fe}^{2+}$ , respectively. If it is assumed that  $\text{Fe}_2\text{O}_3$  contains  $\text{Fe}^{3+}$  only, then these results are in agreement with the hypothesis that SFCA-I can accommodate more  $\text{Fe}^{2+}$  than SFCA. Future work will aim to further test this hypothesis, by investigating the effect of oxygen partial pressure in the range  $p\text{O}_2 = 0.21 - 1 \times 10^{-4}$  atm, on the equilibrium phase assemblages produced from these SFCA and SFCA-I starting mixtures at a number of temperatures in the range 1 423–1 573 K.

### 3.3. Characterisation of the Unknown Phase, $p\text{O}_2 = 1 \times 10^{-4}$ atm

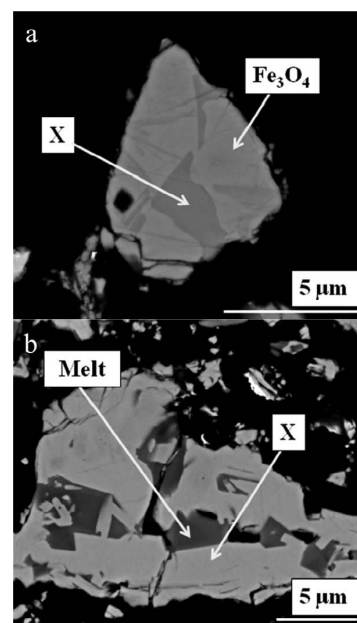
The 'X' phase appears to be a short-lived transient phase, and attempts to quench-in this phase by heating pellets of the starting sinter mixture in a platinum crucible in a vertical tube furnace were unsuccessful. In order to quench-in X phase for *ex situ* examination using SEM, EDS and EPMA, a repeat *in situ* XRD experiment was performed, under the same conditions except that the sample was cooled at  $200 \text{ K min}^{-1}$  to 298 K once the temperature had reached 1 433 K (the temperature at which X phase reflections were most intense). Diffraction data were also collected during cooling, and the reflections for X phase, as well as  $\text{Fe}_3\text{O}_4$  and SFCA, persisted down to 298 K. The product was then removed from the Pt strip heater and prepared for microscopic and compositional examination.

**Figure 5** shows backscattered electron micrographs of the product of this experiment; Fig. 5(a) shows a grain containing  $\text{Fe}_3\text{O}_4$  and X phase, and Fig. 5(b) shows a grain containing X phase and a dark-contrast phase which EDS suggested was likely to be quenched melt. **Table 3** shows the composition of each of these phases, determined using EMPA, assuming all Fe was present as  $\text{Fe}^{3+}$ . The results show that the Fe and Ca totals for X phase are similar to that for CF (*i.e.* 74 and 26 mass%  $\text{Fe}_2\text{O}_3$  and CaO, respectively), and too Ca-rich and Fe-poor to be closely related to SFCA-I (see Section 1). X phase is renamed  $\text{CF}_{\text{AlSi}}$  throughout the remainder of the manuscript, which reflects its compositional similarity with CF and its low Al and Si content.

### 3.4. Reaction Mechanisms, $p\text{O}_2 = 1 \times 10^{-4}$ atm

**Figure 6** shows the *in situ* XRD data collected over the range 1 401–1 456 K at  $p\text{O}_2 = 1 \times 10^{-4}$  atm. The appearance and subsequent increase in intensity of the reflections for  $\text{CF}_{\text{AlSi}}$  at 1 420–1 431 K coincided with a decrease in intensity (and ultimately the disappearance) of the  $\text{C}_2(\text{F}_{1-x}\text{A}_x)$ , CF and  $\text{SiO}_2$  reflections. Figures 6 and 2(c) showed that melting of  $\text{CF}_{\text{AlSi}}$  at temperatures above 1 438 K coincided with the appearance of the minor SFCA reflections, and an increase in the background which is consistent with the formation of melt.

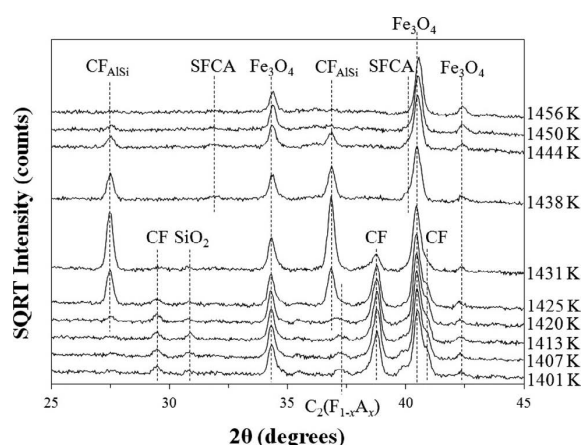
Whilst not evident in Fig. 6, the formation of  $\text{CF}_{\text{AlSi}}$  did correspond with the consumption of some  $\text{Fe}_3\text{O}_4$  and it is considered likely, therefore, that  $\text{CF}_{\text{AlSi}}$  contains a significant



**Fig. 5.** Backscattered electron micrographs of the product of the *in situ* XRD experiment designed to quench in the unknown X phase. a) Shows regions of  $\text{Fe}_3\text{O}_4$  and X phase, and b) shows regions of X phase and melt. The black areas are pores.

**Table 3.** Summary of the compositional results, in terms of mass% oxides, for the product of the *in situ* XRD experiment performed at  $p\text{O}_2 = 1 \times 10^{-4}$  atm, where the sample was cooled from 1 433 K during heating at  $200 \text{ K min}^{-1}$  to 298 K. The numbers in parentheses are the standard deviations of triplicate point analyses for each phase.

Phase	Composition (mass%)				
	$\text{Fe}_2\text{O}_3$	CaO	$\text{SiO}_2$	$\text{Al}_2\text{O}_3$	Total
$\text{Fe}_3\text{O}_4$	96.5 (2.2)	2.5 (1.3)	0.1 (0.1)	1.5 (0.1)	100.5 (1.0)
X ( <i>i.e.</i> $\text{CF}_{\text{AlSi}}$ )	71.6 (1.0)	24.1 (0.3)	0.3 (0.1)	2.4 (0.3)	98.5 (0.9)
Melt	19.2 (1.6)	37.4 (0.4)	18.9 (0.4)	21.6 (1.7)	97.1 (0.9)



**Fig. 6.** *In situ* XRD data collected at  $p\text{O}_2 = 1 \times 10^{-4}$  atm over the range 1 401–1 456 K. The datasets have been offset in the intensity axis to avoid overlap and improve clarity.

amount of  $\text{Fe}^{2+}$ . **Figure 7** shows the results of Rietveld-refinement based QPA, in the temperature range 1 073–1 456 K, performed for the  $p\text{O}_2 = 1 \times 10^{-4}$  atm experiment. The values for phase concentration are absolute, rather than

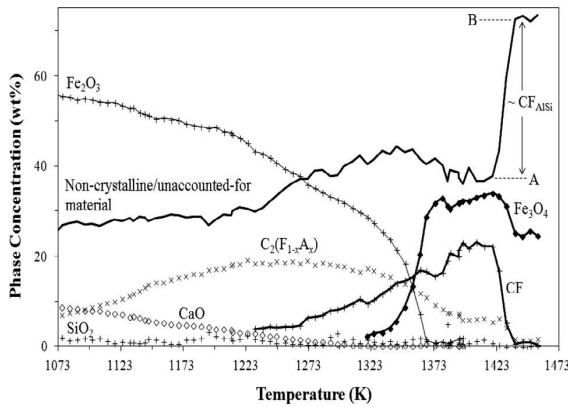


Fig. 7. Results of the Rietveld refinement-based quantitative phase analysis for the *in situ* XRD experiment performed at  $pO_2 = 1 \times 10^{-4}$  atm. Shown are the absolute concentrations of the phases in the system as a function of temperature, which were calculated using the relationships shown in Eqs. (5) and (9).

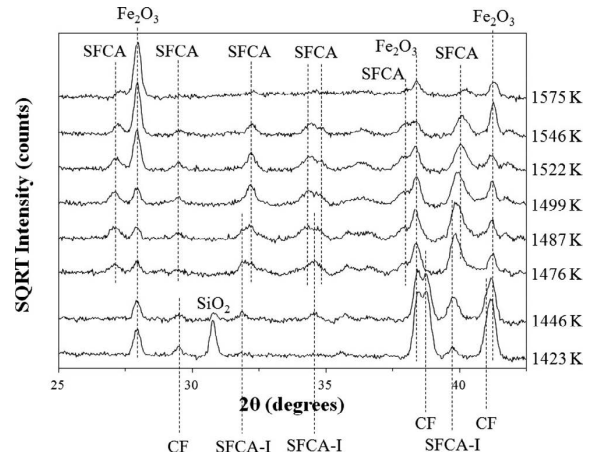


Fig. 8. *In situ* XRD data collected at  $pO_2 = 0.21$  atm over the range 1423–1575 K. The datasets have been offset in the intensity axis to avoid overlap and improve clarity.

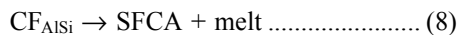
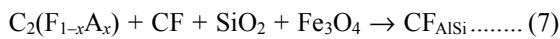
relative, values which were determined using the relationship shown in Eq. (5) (after Madsen and Scarlett<sup>41</sup>),

$$W_i = \frac{\mu_m^* S_i (ZMV)_i}{K} \dots\dots\dots (5)$$

Here,  $W_i$  is the weight fraction of phase  $i$ ,  $S_i$  is the Rietveld scale factor of phase  $i$ ,  $ZM$  is the unit-cell mass of the phase,  $V$  the unit-cell volume,  $\mu_m^*$  is the mass absorption coefficient of the entire mixture, and  $K$  is a scaling factor used to put  $W_i$  on an absolute basis.  $K$  is constant during an experiment as long as the experimental conditions (*e.g.* mA and kV of the Co tube) do not change,<sup>24,42,43</sup> and was calculated using i) the known concentrations of  $Fe_2O_3$ ,  $CaCO_3$ ,  $SiO_2$  and  $Al(OH)_3$  in the starting mixture, and ii) the Rietveld-refined scale factors for  $Fe_2O_3$ ,  $CaCO_3$ ,  $SiO_2$  and  $Al(OH)_3$  in the first dataset collected at 25°C, using Eq. (6).

$$K = \frac{\mu_m^* \sum_{i=1}^n S_i (ZMV)_i}{\sum_{i=1}^n W_i} \dots\dots\dots (6)$$

In Fig. 7, a decrease in the  $Fe_3O_4$  concentration at  $\sim 1423$  K corresponds with the formation of  $CF_{AlSi}$ , and the following plateau in concentration corresponds with the end of this reaction. Eqs. (7) and (8) summarise the reactions involved in the formation of  $CF_{AlSi}$  and SFCA at  $pO_2 = 1 \times 10^{-4}$  atm:



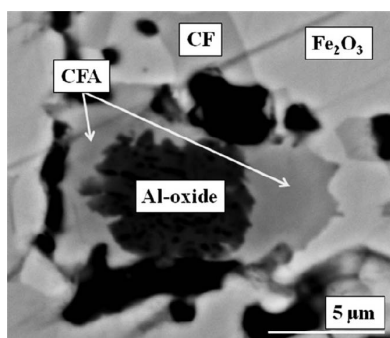
The determination of absolute, rather than relative, concentrations in the manner described has the advantage of allowing for estimation of the non-crystalline/unaccounted-for phase content as a function of temperature. This was achieved using Eq. (9),<sup>41</sup> and the variation of the non-crystalline/unaccounted-for phase content, which includes  $CF_{AlSi}$  because its crystal structure details are unknown, is also shown in Fig. 7. Using this method the maximum possible concentration of  $CF_{AlSi}$  in the system is estimated as being  $\sim 35$  mass% (*i.e.* the difference between levels B and A labelled in Fig. 7).

$$W_{unknown} = 100 - \sum_{i=1}^n W_i \dots\dots\dots (9)$$

**3.5. Reaction Mechanisms,  $pO_2 = 0.21$  atm**

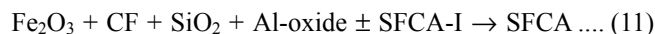
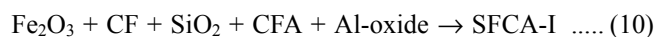
One of the key differences between the results of this experiment, and the results at  $pO_2 = 5 \times 10^{-3}$  atm described by Webster *et al.*<sup>25</sup> and here in Eqs. (1) and (2), is that  $C_2(F_{1-x}A_x)$ , instead of being directly involved in the reaction to form SFCA-I, was fully consumed in its reaction with  $Fe_2O_3$  to form CF and CFA *before* the formation of SFCA-I. **Figure 8** shows the *in situ* XRD data collected over the range 1423–1575 K at  $pO_2 = 0.21$  atm. The typical  $C_2(F_{1-x}A_x)$  reflections at  $26.4$  and  $37.2^\circ 2\theta$  ( $d = 3.92$  and  $2.80 \text{ \AA}$ , respectively) are not present at 1423 K which is before SFCA-I was first evident. A second difference from the results at  $pO_2 = 5 \times 10^{-3}$  atm is that instead of the amount of CF increasing during the early stages of SFCA-I formation, CF was directly involved in the formation of SFCA-I, with the intensities of the CF reflections in Fig. 8 decreasing with the appearance, and subsequent increase in intensity, of the SFCA-I reflections. Both of these results correlate with those obtained by Scarlett *et al.*,<sup>23,24</sup> which is evidence that their experiments which yielded the SFCA-I and SFCA formation mechanisms shown in Eqs. (3) and (4) were conducted towards the high  $pO_2$  end of the range  $pO_2 = 0.21 - 5 \times 10^{-3}$  atm. The formation of SFCA-I was also associated with a decrease in intensity of the  $Fe_2O_3$  and  $SiO_2$  reflections. Further formation of SFCA-I, and the initial formation of SFCA, resulted in a further decrease in intensity of the  $Fe_2O_3$  reflections and the disappearance of the  $SiO_2$  reflections.

Given the low intensity of the CFA reflections, and the overlap of the major CFA reflection at  $39.9^\circ 2\theta$  with a major SFCA-I reflection, it is difficult to determine from these *in situ* data whether, like CF, CFA was involved in the reaction to form SFCA-I or, as was the case at  $pO_2 = 5 \times 10^{-3}$  atm, it was only involved in the reaction to form SFCA. Given that  $C_2(F_{1-x}A_x)$  was not directly involved in the reaction to form SFCA-I, and CF and  $Fe_2O_3$  do not incorporate significant amounts of  $Al^{3+}$ ,<sup>25</sup> it is considered likely that CFA did react to provide the  $Al^{3+}$  content required to form SFCA-I. **Figure 9** shows a backscattered electron micrograph of the



**Fig. 9.** Backscattered electron micrograph of the product of the heat/quench experiment performed at 1323 K for 24 h at  $p_{O_2} = 0.21$  atm, showing CFA,  $Fe_2O_3$ , CF and unreacted Al-oxide. The black areas are pores.

product of the heat/quench experiment performed at  $p_{O_2} = 0.21$  atm and 1323 K for 24 h, with unreacted amorphous Al-oxide encased by CFA, meaning that CFA reacts before the Al-oxide itself is available. EDS analysis confirmed that CF contained a very low concentration of  $Al^{3+}$  similar to that which was determined by Webster *et al.*<sup>25</sup> Eqs. (10) and (11) summarise the reactions involved in the formation of SFCA-I and SFCA at  $p_{O_2} = 0.21$  atm:



#### 4. Conclusion

The formation mechanisms of SFCA and SFCA-I iron ore sinter phases during heating of a synthetic iron ore sinter mixture in the range 298–1623 K and at  $p_{O_2} = 0.21$ ,  $5 \times 10^{-3}$  and  $1 \times 10^{-4}$  atm were determined using *in situ* XRD. Oxygen partial pressure has a significant effect on the formation of SFCA-I and SFCA. Importantly, if the oxygen partial pressure is too low, then desirable SFCA-I will not form. Rather, a Ca-rich ferrite phase designated  $CF_{AlSi}$ , will form through reaction between  $C_2(F_{1-x}A_x)$ , CF,  $SiO_2$  and  $Fe_3O_4$ . On the other hand, if the  $p_{O_2}$  is too high, the thermal stability range of SFCA-I before the formation of SFCA will be reduced. In addition, CFA, which had previously been determined to be a key precursor phase in the formation of SFCA at  $p_{O_2} = 5 \times 10^{-3}$  atm, was also observed to form at  $p_{O_2} = 0.21$  and  $1 \times 10^{-4}$  atm with the amount decreasing with increasing  $p_{O_2}$ . Future work will investigate the effect of  $p_{O_2}$  on the equilibrium phase assemblages produced from a number of different starting mixtures at a number of temperatures in the range 1423–1573 K. It will also implement *in situ* XRD to investigate the phase formation mechanisms, during heating in the range 298–1623 K, in sinter mixtures with compositions designed to form SFCA-I instead of SFCA, and will be the first *in situ* XRD-based study to do so.

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