

**Supporting Information for**

**Fast and Accurate Quantum Crystallography: from**

**Small to Large, from Light to Heavy**

Lorraine A. Malaspina,<sup>a</sup> Erna K. Wieduwilt,<sup>a,b</sup> Justin Bergmann,<sup>a,%</sup> Florian  
Kleemiss,<sup>a,c</sup> Benjamin Meyer,<sup>b,&</sup> Manuel F. Ruiz-López,<sup>b</sup> Rumpa Pal,<sup>a,§</sup> Emanuel  
Hupf,<sup>a,§</sup> Jens Beckmann,<sup>a</sup> Ross O. Piltz,<sup>d</sup> Alison J. Edwards,<sup>d</sup> Simon Grabowsky,<sup>a,c\*</sup>  
Alessandro Genoni<sup>b\*</sup>

<sup>a</sup> *Institut für Anorganische Chemie und Kristallographie, Fachbereich 2 – Biologie/Chemie, Universität Bremen, Leobener Straße 3 und 7, 28359 Bremen, Germany*

<sup>b</sup> *Université de Lorraine, CNRS, Laboratoire de Physique et Chimie Théoriques (LPCT), 1 Boulevard Arago, 57078 Metz, France*

<sup>c</sup> *Departement für Chemie und Biochemie, Universität Bern, Freiestrasse 3, 3012 Bern, Switzerland*

<sup>d</sup> *Australian Nuclear Science and Technology Organisation, Australian Centre for Neutron Scattering, New Illawarra Rd, Lucas Heights NSW 2234, Australia*

Present Addresses:

<sup>%</sup> *Lund University, Department of Theoretical Chemistry, Chemical Center, P.O. Box 124, S-22100 Lund, Sweden*

<sup>&</sup> *Laboratory for Computational Molecular Design (LCMD), Institute of Chemical Sciences and Engineering (ISIC), École Polytechnique Fédérale de Lausanne (EPFL), CH-1015 Lausanne, Switzerland*

<sup>§</sup> *Division of Physics, Faculty of Pure and Applied Sciences, University of Tsukuba, 1-1-1 Tennodai, Tsukuba, Ibaraki, 305-8571, Japan*

<sup>§</sup> *Department of Chemistry, University of Alberta, 11227 Saskatchewan Drive, Edmonton, Alberta, Canada T6G 2G2*

Correspondence to Alessandro Genoni ([Alessandro.Genoni@univ-lorraine.fr](mailto:Alessandro.Genoni@univ-lorraine.fr)) and Simon Grabowsky ([simon.grabowsky@dcb.unibe.ch](mailto:simon.grabowsky@dcb.unibe.ch))

## Table of Contents

|   |     |
|---|-----|
| Theoretical bases of the HAR-ELMO technique .....   | 2   |
| Validation of HAR-ELMO .....  | 8   |
| Measurement details .....   | 8   |
| Refinement details .....  | 10  |
| Methodology for validation of HAR-ELMO .....  | 13  |
| Comparison of hydrogen bond distances .....   | 15  |
| Comparison of hydrogen ADPs .....   | 26  |
| Comparison of non-hydrogen ADPs .....   | 28  |
| Comparison of Fractal Dimension plots .....   | 32  |
| Comparison of Normal Probability plots .....  | 37  |
| Comparison of Averaged-K-curve plots .....  | 40  |
| Comparison of Complete-K-curve plots .....  | 48  |
| Comparison of residual and deformation densities .....  | 56  |
| Polypeptides and Protein Refinements .....  | 83  |
| Refinement details .....  | 83  |
| Comparison of hydrogen bond distances .....   | 101 |
| Comparison of residual and deformation densities .....  | 105 |
| Interaction Energies and Hirshfeld Surface Analysis for the fibril-forming segment of the human prion protein. .... | 110 |
| Refinement of coordination compounds .....  | 112 |
| Graphical visualization software used .....   | 121 |
| References .....  | 122 |

## Theoretical bases of the HAR-ELMO technique

**Hirshfeld Atom Refinement.** In all its variants (traditional and new HAR-ELMO strategy) the Hirshfeld Atom Refinement is a self-consistent refinement procedure consisting in the following steps: i) the starting point is always a molecular geometry from a previous independent atom model refinement that represents at least the asymmetric unit of the crystallographic structure; ii) using the current geometry, a wavefunction is computed: in traditional HAR, a tailor-made quantum mechanical calculation (at Hartree-Fock or Density Functional Theory level) is directly performed, while, in the new HAR-ELMO strategy, the wavefunction is obtained by transferring ELMOs from the constructed libraries; iii) from the obtained wavefunction, a molecular electron density is calculated and afterwards partitioned into atomic contributions through the Hirshfeld stockholder partitioning technique; iv) the resulting Hirshfeld atoms (atomic density functions) are then used for the computation of the global calculated structure factors that allow the evaluation of the statistical agreement with the experimental structure factors ( $\chi^2$ ); v) the statistical agreement is minimized with respect to the atomic coordinates and ADPs using standard least-squares refinement to obtain a new molecular geometry and new ADPs; vi) if convergence is achieved (maximum shift of any refined parameter over its standard uncertainty (s.u) lower than 0.01, namely  $\Delta\text{param/s.u.} < 0.01$ ), the new atomic positions and ADPs represent the refined crystallographic structure, otherwise the new molecular geometry is the starting point for a new iteration from point (ii) to point (v).

**Theory of Extremely Localized Molecular Orbitals.** Extremely localized molecular orbitals (ELMOs)<sup>S1</sup> are molecular orbitals strictly localized on small molecular subunits (e.g., atoms, bonds and functional groups) that are obtained by imposing *a priori* a localization scheme that subdivides the molecule under investigation into fragments that may overlap. This fragmentation allows the definition of a local basis set  $\beta_i = \{|\chi_{i\mu}\rangle\}_{\mu=1}^{M_i}$  for each subunit. Each of the subunits is constituted only by those basis functions that are centered on the atoms that belong to the fragment. These

basis sets are afterwards exploited to expand the ELMOs of each subunit and, for instance, the generic  $\alpha$ -th ELMO for the  $i$ -th fragment can be written in this way:

$$|\varphi_{i\alpha}\rangle = \sum_{\mu=1}^{M_i} C_{i\mu,i\alpha} |\chi_{i\mu}\rangle \quad (\text{S1})$$

Following Stoll,<sup>S1</sup> a single Slater determinant constructed with extremely localized molecular orbitals defined by equation (S1) describes the system under examination:

$$|\Psi_{ELMO}\rangle = \frac{1}{\sqrt{(2N)! \det[\mathbf{S}]}} \hat{A} \left[ \prod_{i=1}^f \prod_{\alpha=1}^{n_i} \varphi_{i\alpha} \bar{\varphi}_{i\alpha} \right] \quad (\text{S2})$$

where  $\hat{A}$  is the usual antisymmetrizer,  $n_i$  is the number of occupied ELMOs for the  $i$ -th fragment,  $\varphi_{i\alpha}$  is a spinorbital with spatial part  $\varphi_{i\alpha}$  and spin part  $\alpha$  and  $\bar{\varphi}_{i\alpha}$  is a spinorbital with spatial part  $\varphi_{i\alpha}$  and spin part  $\beta$ . Furthermore,  $\det[\mathbf{S}]$  is the determinant of the overlap-matrix of the occupied ELMOs, which is actually due to the non-orthogonality of the ELMOs.

ELMOs result from the variational minimization of the ELMO energy (S2) with respect to expansion coefficients  $\{C_{i\mu,i\alpha}\}$  in (S1) and it is possible to show that this is mathematically equivalent to self-consistently solving the following modified Hartree-Fock equations (namely, the Stoll equations) for each fragment:<sup>S1</sup>

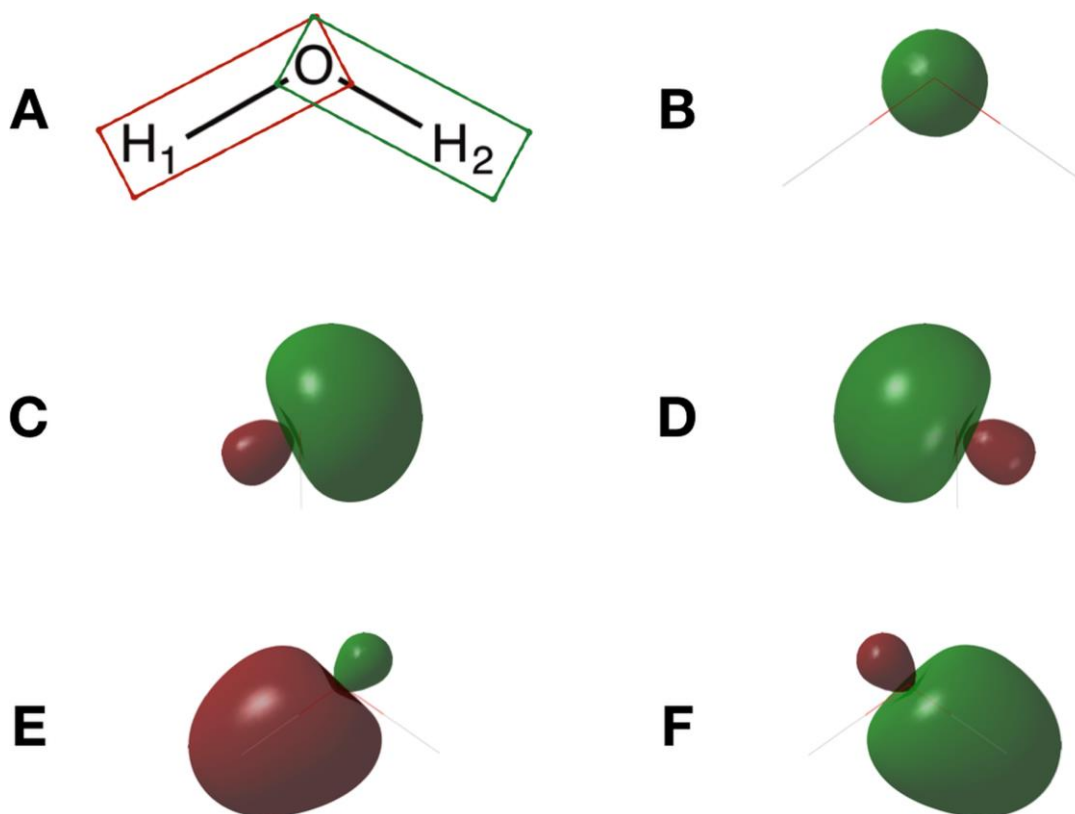
$$\hat{F}_i |\varphi_{i\alpha}\rangle = \varepsilon_{i\alpha} |\varphi_{i\alpha}\rangle \quad (\text{S3})$$

with  $\hat{F}_i$  as the modified Fock operator for the  $i$ -th subunit, namely:

$$\hat{F}_i = (1 - \hat{\rho} + \hat{\rho}_i^\dagger) \hat{F} (1 - \hat{\rho} + \hat{\rho}_i) \quad (\text{S4})$$

where  $\hat{F}$  is the usual Fock operator,  $\hat{\rho}$  is the global density operator (which depends on all the occupied ELMOs of the system) and  $\hat{\rho}_i$  is the density operator for the  $i$ -th fragment (which, on the contrary, depends only on the occupied ELMOs of the subunit).

As an example, in Figure S1 we show the different kinds of ELMOs that can be obtained for the water molecule by defining a localization pattern strictly corresponding to the Lewis structure of the system (Figure S1-A): i) an ELMO describing the oxygen core electrons (Figure S1-B); ii) two ELMOs associated with the two oxygen lone pairs (Figure S1-C and Figure S1-D); iii) two ELMOs corresponding to the two O-H bonds of the molecules (Figure S1-E and Figure S1-F).



**Figure S1:** (A) Lewis structure of the water molecule and corresponding localization scheme: the two overlapping fragments O-H1 and O-H2 are explicitly depicted, while, for the sake of clarity, atomic fragment O associated with the core and lone pair electrons of the oxygen atom is not shown; (B) ELMO describing the core electrons of the oxygen atom; (C) and (D) ELMOs describing the lone pairs of the oxygen atom; (E) ELMO describing the O-H1 bond of the molecule; (F) ELMO describing the O-H2 bond of the molecule. All the ELMOs were computed using the cc-pVDZ basis-set and were plotted considering a 0.15 a.u. isosurface.

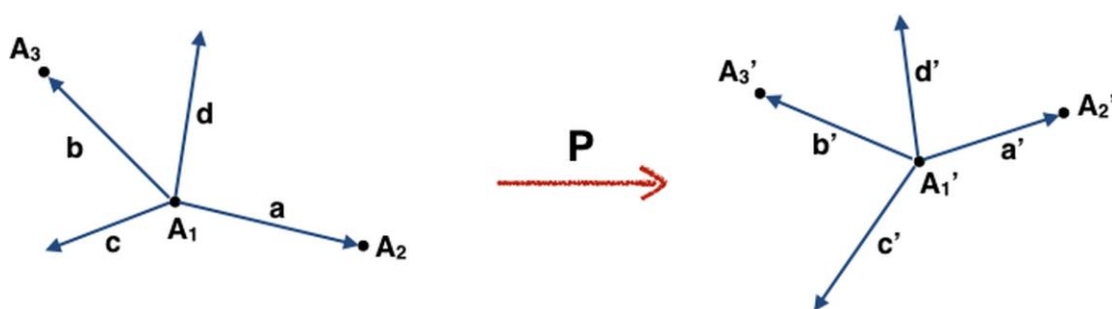
**ELMOs transferability and rotation.** As a consequence of their extreme localization, ELMOs are orbitals easily transferable from one molecule to another, and particularly from a model system (which is usually the small molecule on which the orbital is originally computed) to the target system under investigation. Following Philipp and Friesner,<sup>S2</sup> this can be done by defining a suitable rotation matrix  $\mathbf{P}$  that transforms the ELMO coefficients (see equation (S1)) obtained in the geometry of the model system to the ELMO coefficients in the geometry of the target molecule. As already indicated in detail in previous publications about ELMO transferability and libraries,<sup>S3-S5</sup> the rotation matrix is obtained through the definition *i*) of a reference frame ( $\mathbf{a}$ ,  $\mathbf{c}$ ,  $\mathbf{d}$ ) in the model molecule and *ii*) of a reference frame ( $\mathbf{a}'$ ,  $\mathbf{c}'$ ,  $\mathbf{d}'$ ) in the target system (see Figure S2). These reference frames originate from the choice of

two atomic triads (one for the model molecule and one for the target system) that ensure the uniqueness of the rotation.

If we indicate the two triads for the model and target molecules as  $(A_1, A_2, A_3)$  and  $(A_1', A_2', A_3')$ , respectively, the vectors defining the two reference frames are the following ones:  $\mathbf{a}$  ( $\mathbf{a}'$ ) is the position vector of  $A_2$  ( $A_2'$ ) relative to  $A_1$  ( $A_1'$ ) (see Figure S2), while  $\mathbf{c}$  ( $\mathbf{c}'$ ) and  $\mathbf{d}$  ( $\mathbf{d}'$ ) result from the following vector products:

$$\begin{cases} \mathbf{c} = \mathbf{a} \times \mathbf{b} & (\mathbf{c}' = \mathbf{a}' \times \mathbf{b}') \\ \mathbf{d} = \mathbf{c} \times \mathbf{a} & (\mathbf{d}' = \mathbf{c}' \times \mathbf{a}') \end{cases} \quad (S5)$$

with  $\mathbf{b}$  ( $\mathbf{b}'$ ) as the position vector of  $A_3$  ( $A_3'$ ) with respect to  $A_1$  ( $A_1'$ ) (see Figure S2).



**Figure S2:** Schematic representation of reference frames and atomic triads that are necessary to define matrix  $\mathbf{P}$  associated with the rotation of the ELMOs from the geometry of the model system (left) to the geometry of the target molecule (right).

For ELMOs localized only on one atom (i.e., ELMOs corresponding to core or lone-pair electrons) the atomic triads are constituted of the atom on which the ELMO is localized and, in general, by two other bonded atoms. For ELMOs describing two-center bonds, the triads are given by the two atoms that form the bond and by an atom representing the local dissymmetry of the bond under consideration.<sup>S6</sup> For three-center ELMOs (e.g., ELMOs used to describe electronic delocalization such as in peptide bonds or aromatic rings<sup>S5</sup>), the triads of atoms are automatically chosen. For ELMOs localized on more than three atoms, the definition of triads (and, consequently, of reference frames) that simultaneously take into account the orientation of all the atoms in the subunit is obviously impossible and this is the reason why all the ELMOs available in the current databanks are localized at the most on three atoms (see next subsection).

Rotation matrix  $\mathbf{P}$  that leads from reference frame  $(\mathbf{a}, \mathbf{c}, \mathbf{d})$  to reference frame  $(\mathbf{a}', \mathbf{c}', \mathbf{d}')$  is the “key-matrix” that allows the construction of all the matrices for the rotation

of all kinds of basis functions and associated ELMO coefficients. In fact, it can be easily shown<sup>S3</sup> that, excluding *s*-type atomic orbitals, which are invariant owing to their spherical symmetry, the *p*-type basis functions (and the related coefficients) can be exactly transformed by matrix **P**, while basis functions (and corresponding coefficients) with angular momentum greater than 1 can be rotated using transformation matrices expressed in function of **P**.

**Structure of the ELMO libraries.** As already mentioned in the main text, the current ELMO libraries<sup>S5</sup> enable the description of all the possible fragments of a water molecule and of the twenty natural amino acids in all their possible protonation states and forms (namely, N-terminal, C-terminal and non-terminal forms). They have been constructed by computing ELMOs on proper model molecules that take into account the chemical environment of the considered fragments. At the moment, the ELMO databases are available for five standard basis sets of quantum chemistry (i.e., 6-31G, 6-311G, 6-31G(d,p), 6-311G(d,p) and cc-pVDZ) and contain molecular orbitals localized on one-atom and two-atom fragments, which are associated with core/lone pair and bonding electrons, respectively, and molecular orbitals localized on three-atom fragments, which properly describe the delocalized nature of the electronic structure in some particular regions of proteins and polypeptides (e.g., in carboxylic groups, peptide bonds or aromatic rings).

All the ELMOs in the current version of the databanks were computed on optimized geometries (at B3LYP/6-311++G(d,p) level) of model molecules properly designed to take into account the usual chemical environment of the fragments of interest in polypeptides and proteins. In particular, for each fragment, except for the one corresponding to the peptide bond, the model molecules were constructed using the *Nearest Functional Group Approximation* (NFGA), which consists in considering the subunit of interest and its nearest neighbor functional groups capped with hydrogen atoms.<sup>S3</sup> For peptide bonds the simpler *Nearest Bond Approximation* (NBA) was taken into account, according to which the model molecule consists of the fragment under investigation and its nearest neighbor bonds always capped with hydrogen atoms.<sup>S3</sup>

In the ELMO libraries, for each fragment of the different amino acids, not only the coefficients of the corresponding occupied and virtual ELMOs are stored, but also the coordinates associated with the atomic triads in the model molecule, which are crucial

to define the rotation of the molecular orbitals from the geometry of the model system to the geometry of the target molecule (see previous subsection).

The transfer of the ELMOs from the databanks to target structures is carried out through the in-house program ELMODB. The software basically parses PDB files of polypeptides or proteins and, for each of their residues, it carries out the transfer procedure for one fragment at a time.

As already mentioned in the main text, the ELMODB program has been designed also to read tailor-made ELMOs associated with special fragments of molecules that are not covered by the current version of the databanks. These ELMOs must be determined on proper model systems and afterwards stored (together with the atomic coordinates of the associated model molecule triads) in a specific folder to which the ELMODB program has access. As an example and also for the sake of completeness, the model molecules used to compute the ELMOs exploited in the HAR-ELMO refinements of the coordination compounds investigated in this paper are indicated in the section “Refinement of coordination compounds” of this Supporting Information. A complete overview on the construction and organization of the ELMO databanks and on the main features of the ELMODB program can be found in the original paper about the ELMO libraries.<sup>S5</sup>

# Validation of HAR-ELMO

## Measurement details

The results presented here involve the comparison of the results obtained through the HAR and HAR-ELMO approaches for the following X-ray datasets:

- Glycyl-*L*-alanine, at 12 K,  $\lambda = 0.5259(2)$  Å, data set taken from ref. S7 (ref. 26 in the main text)
- Glycyl-*L*-alanine, at 50 K,  $\lambda = 0.5259(2)$  Å, data set taken from ref. S7
- Glycyl-*L*-alanine, at 100 K,  $\lambda = 0.5259(2)$  Å, data set taken from ref. S7
- Glycyl-*L*-alanine, at 150 K,  $\lambda = 0.5259(2)$  Å, data set taken from ref. S7
- Glycyl-*L*-alanine, at 295 K,  $\lambda = 0.5259(2)$  Å, data set taken from ref. S7
- *L*-alanine, at 23 K,  $\lambda = 0.71073$  Å, data set taken from ref. ref. S8 (ref. 35 in the main text)
- *L*-alanine, at 100 K,  $\lambda = 0.71073$  Å, new measurement (see Table S1 and main text)
- *L*-alanine, at 150 K,  $\lambda = 0.71073$  Å, new measurement (see Table S1 and main text)

Neutron-diffraction data sets are available for all structures except for *L*-alanine and Glycyl-*L*-alanine at 100 K:

- Glycyl-*L*-alanine, at 12 K,  $\lambda = 0.8313(2)$  Å, data set taken from ref. S9 (ref. 36 in the main text)
- Glycyl-*L*-alanine, at 50 K,  $\lambda = 0.8313(2)$  Å, data set taken from ref. S9
- Glycyl-*L*-alanine, at 150 K,  $\lambda = 0.8313(2)$  Å, data set taken from ref. S9
- Glycyl-*L*-alanine, at 295 K,  $\lambda = 0.8313(2)$  Å, data set taken from ref. S9
- *L*-alanine, at 23 K,  $\lambda = 0.750$  to  $1.500$  Å (Laue), new measurement (see Table S1 and main text)
- *L*-alanine, at 150 K,  $\lambda = 0.750$  to  $1.500$  Å (Laue), new measurement (see Table S1 and main text)

**Table S1:** Measurement details for the new X-ray and neutron single-crystal diffraction experiments of *L*-alanine.

| <b>Compound</b>                      | <b><i>L</i>-alanine</b>                                       |  |  |  |
|--------------------------------------|---|--|--|--|
| <b>Chemical formula</b>              | C <sub>3</sub> H <sub>7</sub> N <sub>1</sub> O <sub>2</sub>   |  |  |  |
| <b><i>M<sub>r</sub></i> (u)</b>      | 89.0947   |  |  |  |
| <b>Crystal system</b>                | Orthorhombic  |  |  |  |
| <b>Space group</b>                   | <i>P</i> 2 <sub>1</sub> 2 <sub>1</sub> 2 <sub>1</sub>         |  |  |  |
| <b><i>a, b, c</i> (Å)</b>            | 5.9279(10)*<br>12.2597(17)<br>5.7939(9)                       | 5.9596(2)*<br>12.2828(3)<br>5.7899(1)                          | 5.9587(2)<br>12.2796(4)<br>5.7876(2)   | 5.9596(2)<br>12.2828(3)<br>5.7899(1)   |
| <b><i>V</i> (Å<sup>3</sup>)</b>      | 421.07(7)   | 423.82(2)  | 423.48(2)  | 423.82(2)  |
| <b><i>Z</i></b>                      | 4   | 4  | 4  | 4  |
| <b>Radiation type</b>                | Neutron   | Neutron  | X-ray<br>(MoKα)  | X-ray<br>(MoKα)  |
| <b>Wavelength (Å)</b>                | 0.750 to<br>1.500   | 0.750 to<br>1.500  | 0.71073  | 0.71073  |
| <b>Temperature (K)</b>               | 23  | 150  | 100(2)   | 150(2)   |
| <b>Crystal size (mm)</b>             | 1.9x1.6x1.0   | 3.5x1.9x1.0  | 0.46x0.26x<br>0.17   | 0.29x0.21x<br>0.19   |
| <b>Absorption cor.</b>               | none  | none   | multi-scan   | multi-scan   |
| <b><i>μ</i> (mm<sup>-1</sup>)</b>    | 0.0   | 0.0  | 0.117  | 0.117  |
| <b><i>T<sub>min</sub></i></b>        | -   | -  | 0.943  | 0.631  |
| <b><i>T<sub>max</sub></i></b>        | -   | -  | 0.996  | 0.754  |
| <b>Extinction cor:<sup>S10</sup></b> | 8.8(5)  | 5.0(6)   | none   | none   |
| <b>Resolution (Å)</b>                | 0.500   | 0.500  | 0.45   | 0.55   |
| <b>hkl ranges</b>                    | <i>h</i> = -11, 9<br><i>k</i> = -18, 23<br><i>l</i> = -11, 11 | <i>h</i> = -11, 11<br><i>k</i> = -24, 24<br><i>l</i> = -10, 10 | <i>h</i> = -13, 11<br><i>k</i> = -27, 27<br><i>l</i> = -12, 12                                     | <i>h</i> = -10, 10<br><i>k</i> = -21, 22<br><i>l</i> = -10, 10                                     |
| <b>Theta min</b>                     |   |  | 3.318  | 3.317  |
| <b>Theta max</b>                     | 71.48   | 71.11  | 52.157   | 40.238   |
| <b>Theta full</b>                    | 71.39   | 71.01  | 25.242   | 25.242   |
| <b>Comple. (max)</b>                 | 0.874   | 0.875  | 0.992  | 0.999  |
| <b>Comple. (full)</b>                | 0.874   | 0.875  | 0.987  | 0.998  |
| <b>Refl. Measured</b>                | 35505   | 94436  | 31869  | 21264  |
| <b>Unique refl.</b>                  | 1541  | 1554   | 4783   | 2667   |
| <b>Unique obs. refl.</b>             | 1486  | 1310   | 4611   | 2602   |
| <b>Obs. criteria</b>                 | <i>I</i> >2σ( <i>I</i> )                                      | <i>I</i> >2σ( <i>I</i> )                                       | <i>F</i> >0<br><i>F</i> / <i>u</i> ( <i>F</i> )>3.0<br><i> F<sub>calc</sub> </i> >10 <sup>-3</sup> | <i>F</i> >0<br><i>F</i> / <i>u</i> ( <i>F</i> )>3.0<br><i> F<sub>calc</sub> </i> >10 <sup>-3</sup> |
| <b><i>R<sub>int</sub></i></b>        | 0.0470  | 0.1015   | 0.0223   | 0.0402   |
| <b><i>R<sub>sym</sub></i></b>        | 0.0519  | 0.0937   | 0.0148   | 0.0212   |

\*For the refinements of the Laue neutron-diffraction experiments, the cell parameters of the respective X-ray diffraction data sets at the same temperatures were used.

## Refinement details

**Table S2:** Refinements against X-ray data for Gly-*L*-Ala at 12 K, CCDC deposition nos.: 1917823-1917825.

|  | <b>HAR</b>                                      | <b>HAR-ELMO</b>                                 | <b>IAM</b>                    |
|--|---|---|-------------------------------|
| <b><math>R[F &gt; 3\sigma(F)]</math>, <math>wR(F)</math>, <math>S</math></b>                                 | 0.016, 0.061, 1.27                              | 0.017, 0.061, 1.35                              | 0.025, 0.061, 2.44            |
| <b>No. of reflections</b>  | 2394  | 2394  | 2394                          |
| <b>No. of parameters</b>   | 181   | 181   | 131                           |
| <b>H-atom treatment</b>  | All H-atom parameters refined (anisotropically) | All H-atom parameters refined (anisotropically) | H atoms refined isotropically |
| <b><math>\Delta\rho_{\max}</math>, <math>\Delta\rho_{\min}</math> (<math>\text{e}\text{\AA}^{-3}</math>)</b> | 0.14, -0.17                                     | 0.14, -0.18                                     | 0.20, -0.21                   |

**Table S3:** Refinements against X-ray data for Gly-*L*-Ala at 50 K, CCDC deposition nos.: 1917826-1917828.

|  | <b>HAR</b>                                      | <b>HAR-ELMO</b>                                 | <b>IAM</b>                    |
|--|---|---|-------------------------------|
| <b><math>R[F &gt; 3\sigma(F)]</math>, <math>wR(F)</math>, <math>S</math></b>                                 | 0.018, 0.065, 1.22                              | 0.019, 0.065, 1.31                              | 0.026, 0.065, 2.14            |
| <b>No. of reflections</b>  | 2295  | 2295  | 2295                          |
| <b>No. of parameters</b>   | 181   | 181   | 131                           |
| <b>H-atom treatment</b>  | All H-atom parameters refined (anisotropically) | All H-atom parameters refined (anisotropically) | H atoms refined isotropically |
| <b><math>\Delta\rho_{\max}</math>, <math>\Delta\rho_{\min}</math> (<math>\text{e}\text{\AA}^{-3}</math>)</b> | 0.12, -0.13                                     | 0.12, -0.13                                     | 0.17, -0.18                   |

**Table S4:** Refinements against X-ray data for Gly-*L*-Ala at 100 K, CCDC deposition nos.: 1917829-1917831.

|  | <b>HAR</b>                                      | <b>HAR-ELMO</b>                                 | <b>IAM</b>                    |
|--|---|---|-------------------------------|
| <b><math>R[F &gt; 3\sigma(F)]</math>, <math>wR(F)</math>, <math>S</math></b>                                 | 0.017, 0.082, 1.56                              | 0.018, 0.082, 1.66                              | 0.026, 0.082, 3.10            |
| <b>No. of reflections</b>  | 2456  | 2456  | 2456                          |
| <b>No. of parameters</b>   | 181   | 181   | 131                           |
| <b>H-atom treatment</b>  | All H-atom parameters refined (anisotropically) | All H-atom parameters refined (anisotropically) | H atoms refined isotropically |
| <b><math>\Delta\rho_{\max}</math>, <math>\Delta\rho_{\min}</math> (<math>\text{e}\text{\AA}^{-3}</math>)</b> | 0.14, -0.20                                     | 0.13, -0.17                                     | 0.17, -0.20                   |

**Table S5:** Refinements against X-ray data for Gly-*L*-Ala at 150 K, CCDC deposition nos.: 1917832-1917834.

|  | <b>HAR</b>                                      | <b>HAR-ELMO</b>                                 | <b>IAM</b>                    |
|--|---|---|-------------------------------|
| <b><math>R[F &gt; 3\sigma(F)]</math>, <math>wR(F)</math>, <math>S</math></b>                                 | 0.016, 0.064, 1.53                              | 0.017, 0.064, 1.65                              | 0.025, 0.064, 3.09            |
| <b>No. of reflections</b>  | 2440  | 2440  | 2440                          |
| <b>No. of parameters</b>   | 181   | 181   | 131                           |
| <b>H-atom treatment</b>  | All H-atom parameters refined (anisotropically) | All H-atom parameters refined (anisotropically) | H atoms refined isotropically |
| <b><math>\Delta\rho_{\max}</math>, <math>\Delta\rho_{\min}</math> (<math>\text{e}\text{\AA}^{-3}</math>)</b> | 0.12, -0.13                                     | 0.13, -0.14                                     | 0.14, -0.19                   |

**Table S6:** Refinements against X-ray data for Gly-*L*-Ala at 295 K, CCDC deposition nos.: 1917835-1917837.

|  | <b>HAR</b>                                      | <b>HAR-ELMO</b>                                 | <b>IAM</b>                    |
|--|---|---|-------------------------------|
| <b><math>R[F &gt; 3\sigma(F)]</math>, <math>wR(F)</math>, <math>S</math></b>                                 | 0.019, 0.075, 1.42                              | 0.021, 0.075, 1.55                              | 0.030, 0.075, 2.74            |
| <b>No. of reflections</b>  | 2357  | 2357  | 2357                          |
| <b>No. of parameters</b>   | 181   | 181   | 131                           |
| <b>H-atom treatment</b>  | All H-atom parameters refined (anisotropically) | All H-atom parameters refined (anisotropically) | H atoms refined isotropically |
| <b><math>\Delta\rho_{\max}</math>, <math>\Delta\rho_{\min}</math> (<math>\text{e}\text{\AA}^{-3}</math>)</b> | 0.13, -0.15                                     | 0.12, -0.14                                     | 0.14, -0.17                   |

**Table S7:** Refinements against X-ray data for *L*-Ala at 23 K, CCDC deposition nos.: 1917816-1917818.

|  | <b>HAR</b>                                      | <b>HAR-ELMO</b>                                 | <b>IAM</b>                    |
|--|---|---|-------------------------------|
| <b><math>R[F &gt; 3\sigma(F)]</math>, <math>wR(F)</math>, <math>S</math></b>                                 | 0.020, 0.069, 1.18                              | 0.020, 0.069, 1.29                              | 0.028, 0.069, 2.28            |
| <b>No. of reflections</b>  | 2405  | 2405  | 2405                          |
| <b>No. of parameters</b>   | 118   | 118   | 83                            |
| <b>H-atom treatment</b>  | All H-atom parameters refined (anisotropically) | All H-atom parameters refined (anisotropically) | H atoms refined isotropically |
| <b><math>\Delta\rho_{\max}</math>, <math>\Delta\rho_{\min}</math> (<math>\text{e}\text{\AA}^{-3}</math>)</b> | 0.11, -0.10                                     | 0.11, -0.11                                     | 0.28, -0.27                   |

**Table S8:** Refinements against X-ray data for *L*-Ala at 100 K, CCDC deposition nos.: 1917810-1917812.

|  | <b>HAR</b>                                      | <b>HAR-ELMO</b>                                 | <b>IAM</b>                    |
|--|---|---|-------------------------------|
| <b><math>R[F &gt; 3\sigma(F)]</math>, <math>wR(F)</math>, <math>S</math></b>                                 | 0.020, 0.065, 2.10                              | 0.020, 0.065, 2.30                              | 0.027, 0.065, 4.13            |
| <b>No. of reflections</b>  | 4611  | 4611  | 4611                          |
| <b>No. of parameters</b>   | 118   | 118   | 83                            |
| <b>H-atom treatment</b>  | All H-atom parameters refined (anisotropically) | All H-atom parameters refined (anisotropically) | H atoms refined isotropically |
| <b><math>\Delta\rho_{\max}</math>, <math>\Delta\rho_{\min}</math> (<math>\text{e}\text{\AA}^{-3}</math>)</b> | 0.15, -0.22                                     | 0.16, -0.27                                     | 0.27, -0.25                   |

**Table S9:** Refinements against X-ray data for *L*-Ala at 150 K, CCDC deposition nos.: 1917820-1917822.

|  | <b>HAR</b>                                      | <b>HAR-ELMO</b>                                 | <b>IAM</b>                    |
|--|---|---|-------------------------------|
| <b><math>R[F &gt; 3\sigma(F)]</math>, <math>wR(F)</math>, <math>S</math></b>                                 | 0.020, 0.074, 1.78                              | 0.021, 0.074, 1.88                              | 0.028, 0.074, 2.62            |
| <b>No. of reflections</b>  | 2602  | 2602  | 2602                          |
| <b>No. of parameters</b>   | 118   | 118   | 83                            |
| <b>H-atom treatment</b>  | All H-atom parameters refined (anisotropically) | All H-atom parameters refined (anisotropically) | H atoms refined isotropically |
| <b><math>\Delta\rho_{\max}</math>, <math>\Delta\rho_{\min}</math> (<math>\text{e}\text{\AA}^{-3}</math>)</b> | 0.17, -0.15                                     | 0.16, -0.16                                     | 0.30, -0.20                   |

**Table S10:** Refinement against neutron data for *L*-Ala at 23 K and 150 K, CCDC deposition nos.: 1917813, 1917685.

| <b>Temperature (K)</b>   | 23  | 150   |
|--|---|---|
| <b><math>R[F &gt; 3\sigma(F)]</math>, <math>wR(F)</math>, <math>S</math></b>                                 | 0.033, 0.027, 1.00                              | 0.038, 0.033, 1.00                              |
| <b>No. of reflections</b>  | 1483  | 1305  |
| <b>No. of parameters</b>   | 119   | 119   |
| <b>H-atom treatment</b>  | All H-atom parameters refined (anisotropically) | All H-atom parameters refined (anisotropically) |
| <b><math>\Delta\rho_{\max}</math>, <math>\Delta\rho_{\min}</math> (<math>\text{e}\text{\AA}^{-3}</math>)</b> | 1.43, -1.68                                     | 1.03, -1.17                                     |

## Methodology for validation of HAR-ELMO

HAR refinements were performed at RHF/6-311G(d,p) level. Corresponding HAR-ELMO refinements were performed by transferring ELMOs from the ELMO libraries also using the 6-311G(d,p) basis-set.

No self-consistent field of cluster charges was used in any of the refinements since it is not available in the ELMODB program, although it is known that the use of cluster charges leads to better hydrogen bond distances for groups involved in strong intermolecular interactions such as hydrogen bonds.<sup>S11</sup> The ELMO libraries contain pre-computed ELMOs, which, at the moment, cannot be updated according to the crystal environment represented by the surrounding cluster charges.

In HAR and HAR-ELMO, all hydrogen atoms were refined using anisotropic displacement parameters. Therefore the IAM results will be excluded from all the ADP statistics.

The statistics presented here are based on the following quantities:

- 1) - the mean ratio of the bond lengths  $\langle r_A/r_B \rangle$ 
  - the mean ratio of the diagonal ADPs  $\langle U^i_A/U^i_B \rangle$
  
- 2) - the mean absolute differences (MADs) of the bond lengths ( $r_A$  and  $r_B$ )  $\langle |\Delta r_{A-B}| \rangle$ 
  - the mean absolute differences of the diagonal ADPs  $\langle |\Delta U^i_{A-B}| \rangle$
  - the mean absolute differences of all ADPs  $\langle |\Delta U^{ij}_{A-B}| \rangle$ .

Note that the off-diagonal terms are generally small in magnitude and their differences tend to conceal deviations of the diagonal terms.

- 3) The root-mean-squared differences (wRMSDs) of bond distances and ADPs weighted by the combined standard uncertainties (csus):

The wRMSDs of the bond lengths measure the average deviation of the bond distances obtained through method A from the bond distances obtained through method B (given in equation (S6)).

The wRMSDs of the ADPs measure the average deviation of all ADPs obtained through method A from the ADPs resulting from method B (given in equation (S7)).

$$wRMSD = \left\langle \frac{(r_A - r_B)^2}{s.u.(r_A)^2 + s.u.(r_B)^2} \right\rangle^{\frac{1}{2}} \quad (S6)$$

$$wRMSD = \left\langle \frac{(U_A^{ij} - U_B^{ij})^2}{s.u.(U_A^{ij})^2 + s.u.(U_B^{ij})^2} \right\rangle^{\frac{1}{2}} \quad (S7)$$

The expected values for the previous statistical quantities are the following:

- Type (1) should be close to 1 for good statistical agreement;
- Type (2) should be close to 0 for good statistical agreement;
- Type (3) should be 0 for exact agreement, close to 1 for good statistical agreement.

However, in the calculations of the wRMSD, standard uncertainties (s.u.) are used (see equations (S6) and (S7)). Therefore, considering that standard uncertainties are normally underestimated, values ranging from 1.5 to 2.0 are not uncommon for wRMSDs.

## Comparison of hydrogen bond distances

Table S11: Statistical results for X-H bond distances, averaged among all bonds.

| Compound               | Method<br>(A / B)  | $\langle r_A/r_B \rangle$ | $\langle  \Delta r_{A-B}  \rangle$<br>(in Å) | wRMSD  |
|------------------------|--------------------|---------------------------|--|--------|
| <b>Gly-L-Ala 12 K</b>  | HAR / Neutron      | 0.996                     | 0.006  | 1.295  |
|                        | HAR-ELMO / Neutron | 0.995                     | 0.010  | 1.393  |
|                        | IAM / Neutron      | 0.871                     | 0.139  | 11.588 |
|                        | HAR / HAR-ELMO     | 1.001                     | 0.011  | 1.406  |
| <b>Gly-L-Ala 50 K</b>  | HAR / Neutron      | 1.003                     | 0.010  | 1.236  |
|                        | HAR-ELMO / Neutron | 1.002                     | 0.011  | 1.414  |
|                        | IAM / Neutron      | 0.883                     | 0.125  | 12.807 |
|                        | HAR / HAR-ELMO     | 1.001                     | 0.009  | 0.885  |
| <b>Gly-L-Ala 100 K</b> | HAR / Neutron      | -                         | -  | -      |
|                        | HAR-ELMO / Neutron | -                         | -  | -      |
|                        | IAM / Neutron      | -                         | -  | -      |
|                        | HAR / HAR-ELMO     | 1.000                     | 0.011  | 1.425  |
| <b>Gly-L-Ala 150 K</b> | HAR / Neutron      | 1.000                     | 0.008  | 1.378  |
|                        | HAR-ELMO / Neutron | 1.000                     | 0.013  | 1.997  |
|                        | IAM / Neutron      | 0.880                     | 0.128  | 10.767 |
|                        | HAR / HAR-ELMO     | 1.000                     | 0.012  | 1.432  |
| <b>Gly-L-Ala 295 K</b> | HAR / Neutron      | 0.994                     | 0.011  | 1.061  |
|                        | HAR-ELMO / Neutron | 0.993                     | 0.020  | 1.784  |
|                        | IAM / Neutron      | 0.887                     | 0.120  | 9.113  |
|                        | HAR / HAR-ELMO     | 1.001                     | 0.013  | 1.448  |
| <b>L-Ala 23 K</b>      | HAR / Neutron      | 0.991                     | 0.010  | 1.875  |
|                        | HAR-ELMO / Neutron | 0.974                     | 0.028  | 3.995  |
|                        | IAM / Neutron      | 0.916                     | 0.090  | 9.070  |
|                        | HAR / HAR-ELMO     | 1.018                     | 0.019  | 2.171  |
| <b>L-Ala 100 K</b>     | HAR / Neutron      | -                         | -  | -      |
|                        | HAR-ELMO / Neutron | -                         | -  | -      |
|                        | IAM / Neutron      | -                         | -  | -      |
|                        | HAR / HAR-ELMO     | 1.012                     | 0.012  | 2.326  |
| <b>L-Ala 150 K</b>     | HAR / Neutron      | 0.995                     | 0.009  | 1.186  |
|                        | HAR-ELMO / Neutron | 0.981                     | 0.020  | 2.276  |
|                        | IAM / Neutron      | 0.902                     | 0.105  | 9.733  |
|                        | HAR / HAR-ELMO     | 1.014                     | 0.014  | 1.242  |

**Table S12:** Average bond distances and statistical results for X-H bond distances according to the bond type, distances in Å, units of differences are Å. The numbers in brackets are the sample standard deviations from the averaging procedure.

| Compound                   | Method (A / B)       | Bond type | $\langle r(X-H) \rangle$ (method A) | $\langle r_A/r_B \rangle$ | $\langle  \Delta r_{A-B}  \rangle$ | wRMSD  |
|----------------------------|----------------------|-----------|-------------------------------------|---------------------------|------------------------------------|--------|
| <b>Gly-L-Ala<br/>12 K</b>  | Neutron<br>reference | N-H       | 1.039(11)                           | N/A                       | N/A                                | N/A    |
|                            |                      | C-H       | 1.096(10)                           | N/A                       | N/A                                | N/A    |
|                            | HAR/ Neutron         | N-H       | 1.031(23)                           | 0.992                     | 0.010                              | 1.855  |
|                            |                      | C-H       | 1.095(14)                           | 0.998                     | 0.004                              | 0.708  |
|                            | HAR-ELMO/<br>Neutron | N-H       | 1.025(10)                           | 0.987                     | 0.014                              | 1.790  |
|                            |                      | C-H       | 1.097(19)                           | 1.000                     | 0.007                              | 1.049  |
|                            | IAM/ Neutron         | N-H       | 0.889(29)                           | 0.855                     | 0.151                              | 12.226 |
|                            |                      | C-H       | 0.966(32)                           | 0.881                     | 0.131                              | 11.142 |
|                            | HAR /<br>HAR-ELMO    | N-H       | as above                            | 1.006                     | 0.017                              | 1.896  |
|                            |                      | C-H       | as above                            | 0.998                     | 0.007                              | 0.948  |
| <b>Gly-L-Ala<br/>50 K</b>  | Neutron<br>reference | N-H       | 1.037(13)                           | N/A                       | N/A                                | N/A    |
|                            |                      | C-H       | 1.093(9)                            | N/A                       | N/A                                | N/A    |
|                            | HAR/ Neutron         | N-H       | 1.038(22)                           | 1.001                     | 0.008                              | 0.894  |
|                            |                      | C-H       | 1.098(16)                           | 1.005                     | 0.012                              | 1.419  |
|                            | HAR-ELMO/<br>Neutron | N-H       | 1.033(7)                            | 0.996                     | 0.009                              | 0.987  |
|                            |                      | C-H       | 1.100(17)                           | 1.006                     | 0.013                              | 1.638  |
|                            | IAM/ Neutron         | N-H       | 0.901(11)                           | 0.869                     | 0.136                              | 10.166 |
|                            |                      | C-H       | 0.976(30)                           | 0.893                     | 0.117                              | 14.299 |
|                            | HAR /<br>HAR-ELMO    | N-H       | as above                            | 1.005                     | 0.016                              | 1.262  |
|                            |                      | C-H       | as above                            | 0.999                     | 0.005                              | 0.493  |
| <b>Gly-L-Ala<br/>100 K</b> | Neutron<br>reference | N-H       | -                                   | N/A                       | N/A                                | N/A    |
|                            |                      | C-H       | -                                   | N/A                       | N/A                                | N/A    |
|                            | HAR/ Neutron         | N-H       | 1.028(20)                           | -                         | -                                  | -      |
|                            |                      | C-H       | 1.095(14)                           | -                         | -                                  | -      |
|                            | HAR-ELMO/<br>Neutron | N-H       | 1.023(17)                           | -                         | -                                  | -      |
|                            |                      | C-H       | 1.099(12)                           | -                         | -                                  | -      |
|                            | IAM/ Neutron         | N-H       | 0.902(19)                           | -                         | -                                  | -      |
|                            |                      | C-H       | 0.965(32)                           | -                         | -                                  | -      |
|                            | HAR /<br>HAR-ELMO    | N-H       | as above                            | 1.005                     | 0.016                              | 1.833  |
|                            |                      | C-H       | as above                            | 0.996                     | 0.008                              | 1.071  |

**Table S12:** continued.

| <b>Compound</b>            | <b>Method<br/>(A / B )</b> | <b>Bond<br/>type</b> | <b><math>\langle r(\text{X—H}) \rangle</math><br/>(method A)</b> | <b><math>\langle r_A/r_B \rangle</math></b> | <b><math>\langle  \Delta r_{A-B}  \rangle</math></b> | <b>wRMSD</b> |
|----------------------------|----------------------------|----------------------|--|---|--|--------------|
| <b>Gly-L-Ala<br/>150 K</b> | Neutron<br>reference       | N-H                  | 1.040(12)  | N/A   | N/A  | N/A          |
|                            |                            | C-H                  | 1.091(10)  | N/A   | N/A  | N/A          |
|                            | HAR/ Neutron               | N-H                  | 1.030(16)  | 0.991                                       | 0.011  | 1.706        |
|                            |                            | C-H                  | 1.097(13)  | 1.006                                       | 0.007  | 1.107        |
|                            | HAR-ELMO/<br>Neutron       | N-H                  | 1.026(12)  | 0.987                                       | 0.018  | 2.307        |
|                            |                            | C-H                  | 1.100(15)  | 1.009                                       | 0.010  | 1.760        |
|                            | IAM/ Neutron               | N-H                  | 0.891(26)  | 0.857                                       | 0.149  | 12.134       |
|                            |                            | C-H                  | 0.977(41)  | 0.896                                       | 0.114  | 9.751        |
|                            | HAR /<br>HAR-ELMO          | N-H                  | as above   | 1.004                                       | 0.017  | 1.904        |
|                            |                            | C-H                  | as above   | 0.997                                       | 0.008  | 1.002        |
| <b>Gly-L-Ala<br/>295 K</b> | Neutron<br>reference       | N-H                  | 1.040(11)  | N/A   | N/A  | N/A          |
|                            |                            | C-H                  | 1.085(10)  | N/A   | N/A  | N/A          |
|                            | HAR/ Neutron               | N-H                  | 1.026(11)  | 0.987                                       | 0.014  | 1.331        |
|                            |                            | C-H                  | 1.084(22)  | 0.998                                       | 0.009  | 0.835        |
|                            | HAR-ELMO/<br>Neutron       | N-H                  | 1.024(17)  | 0.985                                       | 0.026  | 2.271        |
|                            |                            | C-H                  | 1.084(28)  | 0.999                                       | 0.015  | 1.366        |
|                            | IAM/ Neutron               | N-H                  | 0.883(36)  | 0.849                                       | 0.157  | 11.291       |
|                            |                            | C-H                  | 0.990(47)  | 0.913                                       | 0.095  | 7.308        |
|                            | HAR /<br>HAR-ELMO          | N-H                  | as above   | 1.002                                       | 0.019  | 2.010        |
|                            |                            | C-H                  | as above   | 1.000                                       | 0.009  | 0.894        |

Table S12: continued.

| Compound                     | Method (A / B)       | Bond type | $\langle r(\text{X—H}) \rangle$ (method A) | $\langle r_A/r_B \rangle$ | $\langle  \Delta r_{A-B}  \rangle$ | wRMSD |
|------------------------------|----------------------|-----------|--|---------------------------|------------------------------------|-------|
| <b>L-Ala</b><br><b>23 K</b>  | Neutron reference    | N-H       | 1.044(10)                                  | N/A                       | N/A                                | N/A   |
|                              |                      | C-H       | 1.095(4)                                   | N/A                       | N/A                                | N/A   |
|                              | HAR/ Neutron         | N-H       | 1.028(13)                                  | 0.984                     | 0.016                              | 2.437 |
|                              |                      | C-H       | 1.091(8)                                   | 0.996                     | 0.006                              | 1.304 |
|                              | HAR-ELMO/<br>Neutron | N-H       | 1.000(27)                                  | 0.958                     | 0.044                              | 5.296 |
|                              |                      | C-H       | 1.079(12)                                  | 0.985                     | 0.017                              | 2.624 |
|                              | IAM/ Neutron         | N-H       | 0.965(68)                                  | 0.924                     | 0.079                              | 8.923 |
|                              |                      | C-H       | 0.998(20)                                  | 0.911                     | 0.098                              | 9.178 |
|                              | HAR /<br>HAR-ELMO    | N-H       | as above                                   | 1.028                     | 0.027                              | 2.775 |
|                              |                      | C-H       | as above                                   | 1.011                     | 0.012                              | 1.572 |
| <b>L-Ala</b><br><b>100 K</b> | Neutron reference    | N-H       | -  | -                         | -                                  | -     |
|                              |                      | C-H       | -  | -                         | -                                  | -     |
|                              | HAR/ Neutron         | N-H       | 1.036(15)                                  | -                         | -                                  | -     |
|                              |                      | C-H       | 1.088(11)                                  | -                         | -                                  | -     |
|                              | HAR-ELMO/<br>Neutron | N-H       | 1.023(11)                                  | -                         | -                                  | -     |
|                              |                      | C-H       | 1.076(3)                                   | -                         | -                                  | -     |
|                              | IAM/ Neutron         | N-H       | 0.927(22)                                  | -                         | -                                  | -     |
|                              |                      | C-H       | 0.981(27)                                  | -                         | -                                  | -     |
|                              | HAR /<br>HAR-ELMO    | N-H       | as above                                   | 1.012                     | 0.013                              | 2.103 |
|                              |                      | C-H       | as above                                   | 1.011                     | 0.012                              | 2.481 |
| <b>L-Ala</b><br><b>150 K</b> | Neutron reference    | N-H       | 1.042(10)                                  | N/A                       | N/A                                | N/A   |
|                              |                      | C-H       | 1.091(5)                                   | N/A                       | N/A                                | N/A   |
|                              | HAR/ Neutron         | N-H       | 1.035(13)                                  | 0.993                     | 0.013                              | 1.490 |
|                              |                      | C-H       | 1.087(5)                                   | 0.996                     | 0.006                              | 0.892 |
|                              | HAR-ELMO/<br>Neutron | N-H       | 1.020(19)                                  | 0.979                     | 0.022                              | 2.486 |
|                              |                      | C-H       | 1.073(8)                                   | 0.983                     | 0.018                              | 2.104 |
|                              | IAM/ Neutron         | N-H       | 0.938(41)                                  | 0.899                     | 0.105                              | 9.548 |
|                              |                      | C-H       | 0.985(31)                                  | 0.903                     | 0.106                              | 9.870 |
|                              | HAR /<br>HAR-ELMO    | N-H       | as above                                   | 1.014                     | 0.014                              | 1.145 |
|                              |                      | C-H       | as above                                   | 1.013                     | 0.014                              | 1.309 |

**Table S13:** Intermolecular hydrogen bonds of Gly-*L*-Ala. For atomic labels, see the CIFs deposited with the Cambridge Database and with this journal as Supporting Information

| <b>.D-H..A</b>           | <b>Model</b> | <b>12 K</b> | <b>50 K</b> | <b>100 K</b> | <b>150 K</b> | <b>295 K</b> |
|--------------------------|--------------|-------------|-------------|--------------|--------------|--------------|
| <b>D-H Distance in Å</b> |              |             |             |              |              |              |
| N1-H11<br>...O1          | Neutron      | 1.022(4)    | 1.018(4)    | -            | 1.025(4)     | 1.023(6)     |
|                          | HAR          | 0.997(7)    | 1.007(9)    | 1.002(6)     | 1.008(6)     | 1.009(7)     |
|                          | HAR-ELMO     | 1.020(7)    | 1.027(9)    | 1.025(6)     | 1.034(6)     | 1.045(7)     |
|                          | IAM          | 0.854(12)   | 0.889(13)   | 0.880(11)    | 0.859(11)    | 0.834(11)    |
| N2-H12<br>...O2          | Neutron      | 1.044(5)    | 1.045(5)    | -            | 1.040(5)     | 1.042(7)     |
|                          | HAR          | 1.047(7)    | 1.058(9)    | 1.039(7)     | 1.045(7)     | 1.034(8)     |
|                          | HAR-ELMO     | 1.029(7)    | 1.042(9)    | 1.021(8)     | 1.031(7)     | 1.023(9)     |
|                          | IAM          | 0.893(11)   | 0.903(14)   | 0.909(11)    | 0.909(11)    | 0.901(12)    |
| N2-H22<br>...O1          | Neutron      | 1.045(5)    | 1.041(5)    | -            | 1.053(5)     | 1.043(7)     |
|                          | HAR          | 1.039(8)    | 1.046(9)    | 1.024(9)     | 1.028(8)     | 1.030(9)     |
|                          | HAR-ELMO     | 1.015(9)    | 1.029(9)    | 1.003(10)    | 1.009(9)     | 1.007(11)    |
|                          | IAM          | 0.923(13)   | 0.914(12)   | 0.923(14)    | 0.913(13)    | 0.916(14)    |
| N2-H32<br>...O2          | Neutron      | 1.044(5)    | 1.042(4)    | -            | 1.041(5)     | 1.049(7)     |
|                          | HAR          | 1.039(7)    | 1.039(9)    | 1.045(8)     | 1.039(7)     | 1.029(9)     |
|                          | HAR-ELMO     | 1.037(8)    | 1.031(9)    | 1.042(9)     | 1.031(8)     | 1.021(10)    |
|                          | IAM          | 0.884(10)   | 0.895(12)   | 0.894(11)    | 0.883(10)    | 0.881(11)    |

**Table S13:** continued.

| <b>D-H..A</b>              | <b>Model</b> | <b>12 K</b> | <b>50 K</b> | <b>100 K</b> | <b>150 K</b> | <b>295 K</b> |
|----------------------------|--------------|-------------|-------------|--------------|--------------|--------------|
| <b>H...A Distance in Å</b> |              |             |             |              |              |              |
| N1-H11<br>...O1            | Neutron      | 1.869(5)    | 1.865(4)    | -            | 1.868(5)     | 1.892(7)     |
|                            | HAR          | 1.894(7)    | 1.887(8)    | 1.892(6)     | 1.891(6)     | 1.907(7)     |
|                            | HAR-ELMO     | 1.871(7)    | 1.866(9)    | 1.868(6)     | 1.865(6)     | 1.873(7)     |
|                            | IAM          | 2.037(12)   | 2.010(13)   | 2.013(11)    | 2.037(11)    | 2.076(11)    |
| N2-H12<br>...O2            | Neutron      | 1.712(5)    | 1.713(5)    | -            | 1.721(5)     | 1.737(8)     |
|                            | HAR          | 1.717(7)    | 1.706(9)    | 1.727(7)     | 1.724(7)     | 1.750(8)     |
|                            | HAR-ELMO     | 1.734(7)    | 1.719(9)    | 1.744(7)     | 1.738(7)     | 1.761(9)     |
|                            | IAM          | 1.855(11)   | 1.845(14)   | 1.844(11)    | 1.847(11)    | 1.871(12)    |
| N2-H22<br>...O1            | Neutron      | 1.686(5)    | 1.694(5)    | -            | 1.682(5)     | 1.685(8)     |
|                            | HAR          | 1.696(9)    | 1.692(9)    | 1.715(9)     | 1.709(9)     | 1.714(10)    |
|                            | HAR-ELMO     | 1.719(9)    | 1.707(9)    | 1.733(10)    | 1.727(9)     | 1.736(12)    |
|                            | IAM          | 1.810(13)   | 1.825(12)   | 1.814(15)    | 1.824(13)    | 1.826(14)    |
| N2-H32<br>...O2            | Neutron      | 1.728(5)    | 1.735(5)    | -            | 1.740(5)     | 1.744(8)     |
|                            | HAR          | 1.738(7)    | 1.739(10)   | 1.739(8)     | 1.742(7)     | 1.766(9)     |
|                            | HAR-ELMO     | 1.739(9)    | 1.747(11)   | 1.741(9)     | 1.748(9)     | 1.769(10)    |
|                            | IAM          | 1.885(11)   | 1.882(13)   | 1.881(11)    | 1.891(11)    | 1.906(11)    |
| <b>D...A Distance in Å</b> |              |             |             |              |              |              |
| N1-H11<br>...O1            | Neutron      | 2.876(2)    | 2.870(2)    | -            | 2.879(2)     | 2.904(4)     |
|                            | HAR          | 2.8745(4)   | 2.8752(8)   | 2.8773(8)    | 2.8813(9)    | 2.8969(9)    |
|                            | HAR-ELMO     | 2.8745(5)   | 2.8746(8)   | 2.8776(9)    | 2.8815(9)    | 2.8972(9)    |
|                            | IAM          | 2.8761(8)   | 2.8759(11)  | 2.8778(10)   | 2.8827(11)   | 2.8989(12)   |
| N2-H12<br>...O2            | Neutron      | 2.747(3)    | 2.751(3)    | -            | 2.754(3)     | 2.772(4)     |
|                            | HAR          | 2.7489(5)   | 2.7488(8)   | 2.7519(8)    | 2.7551(8)    | 2.7696(9)    |
|                            | HAR-ELMO     | 2.7495(5)   | 2.7493(9)   | 2.7526(8)    | 2.7558(9)    | 2.7705(10)   |
|                            | IAM          | 2.7465(8)   | 2.7457(12)  | 2.7498(10)   | 2.7529(11)   | 2.7671(12)   |
| N2-H22<br>...O1            | Neutron      | 2.716(2)    | 2.721(2)    | -            | 2.718(3)     | 2.713(4)     |
|                            | HAR          | 2.7161(5)   | 2.7175(7)   | 2.7168(8)    | 2.7182(8)    | 2.7219(9)    |
|                            | HAR-ELMO     | 2.7163(5)   | 2.7179(7)   | 2.7168(9)    | 2.7184(9)    | 2.7233(10)   |
|                            | IAM          | 2.7169(9)   | 2.7180(9)   | 2.7178(11)   | 2.7201(11)   | 2.7248(13)   |
| N2-H32<br>...O2            | Neutron      | 2.723(2)    | 2.726(2)    | -            | 2.728(3)     | 2.739(4)     |
|                            | HAR          | 2.7253(5)   | 2.7250(8)   | 2.7244(8)    | 2.7277(8)    | 2.7360(9)    |
|                            | HAR-ELMO     | 2.7256(5)   | 2.7255(8)   | 2.7247(8)    | 2.7280(9)    | 2.7368(9)    |
|                            | IAM          | 2.7239(8)   | 2.7242(10)  | 2.7230(10)   | 2.7265(11)   | 2.7358(12)   |

**Table S13:** continued.

| <b>.D-H..A</b>  | <b>Model</b> | <b>12 K</b>               | <b>50 K</b> | <b>100 K</b> | <b>150 K</b> | <b>295 K</b> |
|-----------------|--------------|---------------------------|-------------|--------------|--------------|--------------|
|                 |              | <b>D-H...A Angle in °</b> |             |              |              |              |
| N1-H11<br>...O1 | Neutron      | 167.8(4)                  | 168.3(3)    | -            | 168.3(4)     | 169.3(5)     |
|                 | HAR          | 167.2(6)                  | 166.2(8)    | 167.1(5)     | 166.7(5)     | 166.3(6)     |
|                 | HAR-ELMO     | 167.4(6)                  | 166.4(9)    | 167.5(5)     | 166.8(6)     | 166.0(7)     |
|                 | IAM          | 167.4(12)                 | 164.3(13)   | 167.4(11)    | 168.0(12)    | 168.8(12)    |
| N2-H12<br>...O2 | Neutron      | 170.8(4)                  | 171.5(4)    | -            | 171.4(4)     | 171.3(7)     |
|                 | HAR          | 167.8(8)                  | 167.9(8)    | 168.0(7)     | 168.1(6)     | 167.8(7)     |
|                 | HAR-ELMO     | 168.5(8)                  | 169.1(8)    | 168.7(7)     | 168.5(7)     | 168.3(8)     |
|                 | IAM          | 175.6(10)                 | 175.1(11)   | 174.4(11)    | 174.3(10)    | 172.7(11)    |
| N2-H22<br>...O1 | Neutron      | 167.6(4)                  | 167.7(4)    | -            | 167.1(4)     | 167.4(6)     |
|                 | HAR          | 166.2(7)                  | 165.6(9)    | 165.0(7)     | 166.0(7)     | 165.1(8)     |
|                 | HAR-ELMO     | 166.7(7)                  | 166.5(9)    | 165.8(8)     | 166.5(7)     | 166.0(9)     |
|                 | IAM          | 166.7(11)                 | 164.9(12)   | 165.7(12)    | 166.8(12)    | 166.4(12)    |
| N2-H32<br>...O2 | Neutron      | 157.6(4)                  | 157.1(4)    | -            | 157.1(5)     | 156.8(7)     |
|                 | HAR          | 157.1(7)                  | 156.8(10)   | 155.5(7)     | 156.7(6)     | 155.5(8)     |
|                 | HAR-ELMO     | 157.4(8)                  | 156.9(11)   | 155.7(8)     | 157.3(8)     | 156.7(9)     |
|                 | IAM          | 157.8(10)                 | 156.2(14)   | 156.2(10)    | 157.2(10)    | 156.4(11)    |

**Table S14:** Intermolecular hydrogen bonds for *L*-alanine. For atomic labels and symmetry codes, see the CIFs deposited with the Cambridge Database and with this journal as Supporting Information.

| <b>D-H..A</b>            | <b>Model</b> | <b>12 K</b> | <b>100 K</b> | <b>150 K</b> |
|--------------------------|--------------|-------------|--------------|--------------|
| <b>D-H Distance in Å</b> |              |             |              |              |
| N1-H1...O1               | Neutron      | 1.0352(17)  | -            | 1.035(2)     |
|                          | HAR          | 1.024(7)    | 1.052(4)     | 1.042(10)    |
|                          | HAR-ELMO     | 0.973(9)    | 1.035(5)     | 1.023(11)    |
|                          | IAM          | 0.935(11)   | 0.917(7)     | 0.914(13)    |
| N1-H2...O2               | Neutron      | 1.0441(19)  | -            | 1.040(2)     |
|                          | HAR          | 1.018(7)    | 1.031(4)     | 1.021(8)     |
|                          | HAR-ELMO     | 1.000(8)    | 1.017(5)     | 1.001(9)     |
|                          | IAM          | 0.917(10)   | 0.914(6)     | 0.914(10)    |
| N1-H3...O1               | Neutron      | 1.0534(13)  | -            | 1.0524(19)   |
|                          | HAR          | 1.042(7)    | 1.024(4)     | 1.042(9)     |
|                          | HAR-ELMO     | 1.027(8)    | 1.017(5)     | 1.037(9)     |
|                          | IAM          | 1.040(12)   | -            | 0.984(11)    |
| N1-H3...O2               | Neutron      | 1.0534(13)  | -            | 1.0524(19)   |
|                          | HAR          | 1.042(7)    | 1.024(4)     | 1.042(9)     |
|                          | HAR-ELMO     | 1.027(8)    | 1.017(5)     | 1.037(9)     |
|                          | IAM          | 1.040(12)   | 0.952(6)     | 0.984(11)    |

**Table S14:** continued.

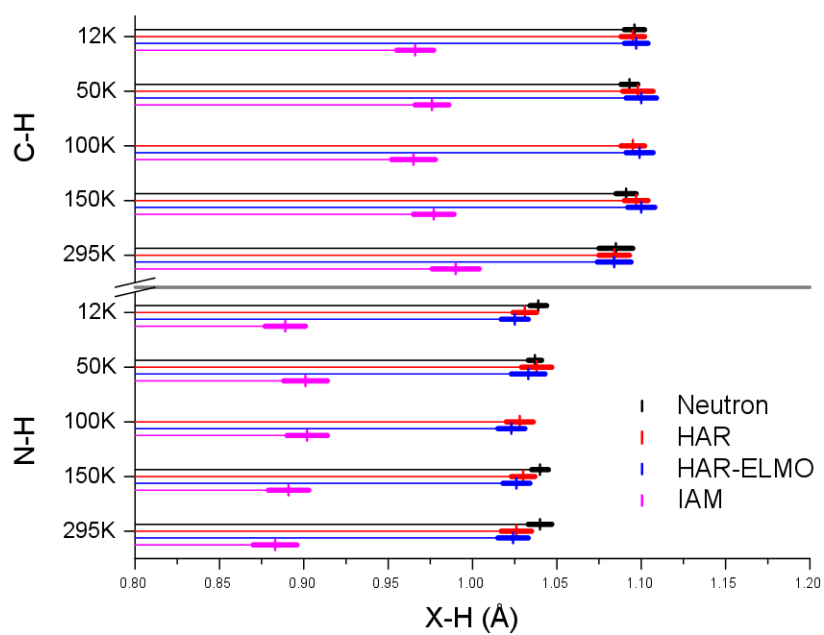
| <b>D-H..A</b>              | <b>Model</b> | <b>12 K</b> | <b>100 K</b> | <b>150 K</b> |
|----------------------------|--------------|-------------|--------------|--------------|
| <b>H...A Distance in Å</b> |              |             |              |              |
| N1-H1...O1                 | Neutron      | 1.8355(18)  | -            | 1.841(2)     |
|                            | HAR          | 1.855(7)    | 1.836(4)     | 1.845(10)    |
|                            | HAR-ELMO     | 1.900(9)    | 1.847(5)     | 1.858(11)    |
|                            | IAM          | 1.918(11)   | 1.941(7)     | 1.945(13)    |
| N1-H2...O2                 | Neutron      | 1.802(2)    | -            | 1.809(3)     |
|                            | HAR          | 1.831(6)    | 1.820(4)     | 1.833(9)     |
|                            | HAR-ELMO     | 1.847(7)    | 1.832(5)     | 1.850(10)    |
|                            | IAM          | 1.937(10)   | 1.937(6)     | 1.940(10)    |
| N1-H3...O1                 | Neutron      | 2.5496(15)  | -            | 2.541(2)     |
|                            | HAR          | 2.573(7)    | 2.578(4)     | 2.580(9)     |
|                            | HAR-ELMO     | 2.577(8)    | 2.575(5)     | 2.579(9)     |
|                            | IAM          | 2.558(12)   | -            | 2.596(12)    |
| N1-H3...O2                 | Neutron      | 1.7495(15)  | -            | 1.756(2)     |
|                            | HAR          | 1.757(7)    | 1.779(4)     | 1.759(9)     |
|                            | HAR-ELMO     | 1.773(8)    | 1.787(4)     | 1.766(9)     |
|                            | IAM          | 1.764(12)   | 1.854(6)     | 1.822(11)    |
| <b>D...A Distance in Å</b> |              |             |              |              |
| N1-H1...O1                 | Neutron      | 2.8354(9)   | -            | 2.8402(11)   |
|                            | HAR          | 2.8348(6)   | 2.8391(2)    | 2.8394(4)    |
|                            | HAR-ELMO     | 2.8353(6)   | 2.8398(2)    | 2.8397(5)    |
|                            | IAM          | 2.8321(8)   | 2.8372(4)    | 2.8373(6)    |
| N1-H2...O2                 | Neutron      | 2.8153(9)   | -            | 2.8199(12)   |
|                            | HAR          | 2.8149(6)   | 2.8194(2)    | 2.8205(4)    |
|                            | HAR-ELMO     | 2.8151(6)   | 2.8199(3)    | 2.8208(5)    |
|                            | IAM          | 2.8145(8)   | 2.8185(4)    | 2.8188(6)    |
| N1-H3...O1                 | Neutron      | 3.3371(9)   | -            | 3.3326(11)   |
|                            | HAR          | 3.3364(7)   | 3.3299(2)    | 3.3314(4)    |
|                            | HAR-ELMO     | 3.3368(7)   | 3.3301(3)    | 3.3315(4)    |
|                            | IAM          | 3.3358(9)   | -            | 3.3326(6)    |
| N1-H3...O2                 | Neutron      | 2.7922(9)   | -            | 2.7971(10)   |
|                            | HAR          | 2.7918(6)   | 2.7955(2)    | 2.7964(4)    |
|                            | HAR-ELMO     | 2.7919(6)   | 2.7955(2)    | 2.7965(4)    |
|                            | IAM          | 2.7910(8)   | 2.7956(4)    | 2.7965(6)    |

**Table S14:** continued.

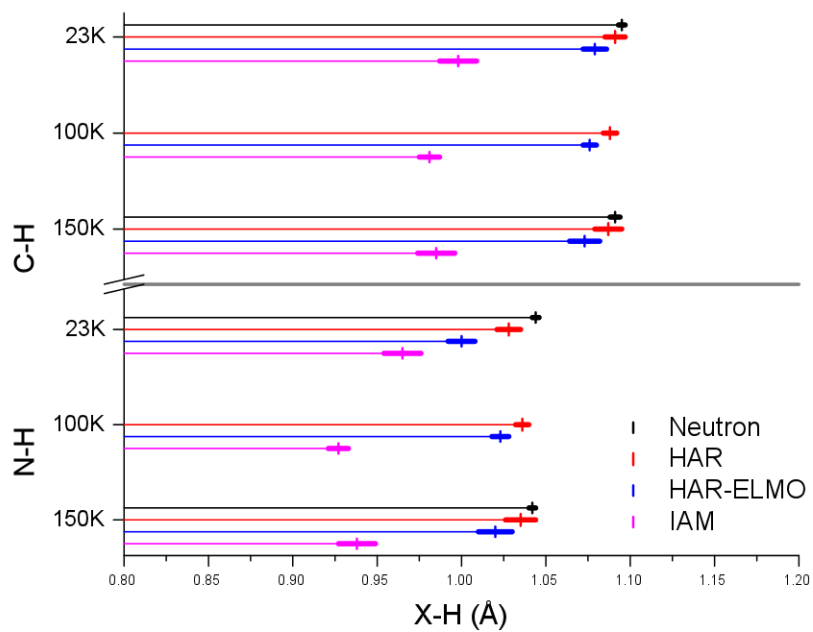
| <b>D-H..A</b>             | <b>Model</b> | <b>12 K</b> | <b>100 K</b> | <b>150 K</b> |
|---------------------------|--------------|-------------|--------------|--------------|
| <b>D-H...A Angle in °</b> |              |             |              |              |
| N1-H1...O1                | Neutron      | 161.25(15)  | -            | 161.3(2)     |
|                           | HAR          | 159.1(7)    | 158.2(4)     | 158.3(9)     |
|                           | HAR-ELMO     | 160.3(8)    | 159.5(4)     | 159.7(10)    |
|                           | IAM          | 165.1(11)   | 165.4(6)     | 164.6(11)    |
| N1-H2...O2                | Neutron      | 162.59(16)  | -            | 162.8(2)     |
|                           | HAR          | 161.4(6)    | 162.2(3)     | 161.8(7)     |
|                           | HAR-ELMO     | 162.1(7)    | 162.9(4)     | 162.6(8)     |
|                           | IAM          | 159.6(9)    | 161.4(6)     | 160.7(9)     |
| N1-H3...O1                | Neutron      | 131.02(13)  | -            | 131.47(17)   |
|                           | HAR          | 129.7(5)    | 130.0(3)     | 128.6(6)     |
|                           | HAR-ELMO     | 130.5(5)    | 130.8(3)     | 129.2(6)     |
|                           | IAM          | 131.1(8)    | -            | 131.7(8)     |
| N1-H3...O2                | Neutron      | 169.62(15)  | -            | 169.26(19)   |
|                           | HAR          | 171.5(6)    | 171.7(3)     | 172.8(7)     |
|                           | HAR-ELMO     | 170.9(7)    | 170.9(4)     | 172.4(8)     |
|                           | IAM          | 168.6(10)   | 169.5(6)     | 170.2(10)    |

**Table S15:** Symmetry operations for intermolecular hydrogen bonds of Gly-*L*-Ala and *L*-Ala.

| <b>Compound</b>    | <b>D-H..A</b> | <b>Symmetry operation</b> |
|--------------------|---------------|---------------------------|
| Gly- <i>L</i> -Ala | N1-H11...O1   | $1/2-x, 2-y, -1/2+z$      |
|                    | N2-H12...O2   | $3/2-x, 2-y, -1/2+z$      |
|                    | N2-H22...O1   | $1/2+x, 3/2-y, 1-z$       |
|                    | N2-H32...O2   | $1-x, 1/2+y, 3/2-z$       |
| <i>L</i> -Ala      | N1-H1...O1    | $3/2-x, -y, -1/2+z$       |
|                    | N1-H2...O2    | $1/2+x, 1/2-y, 1-z$       |
|                    | N1-H3...O1    | $x, y, -1+z$              |
|                    | N1-H3...O2    | $x, y, -1+z$              |



**Figure S3:** Graphical representation of Table S12 for X-H bond lengths in Gly-*L*-Ala.



**Figure S4:** Graphical representation of Table S12 for X-H bond lengths in *L*-Ala.

## Comparison of hydrogen ADPs

**Table S16:** Statistical results for hydrogen atom ADPs for Gly-*L*-Ala, units of differences are Å<sup>2</sup>.

| Method (A/B)   | 12 K   | 50 K   | 100 K  | 150 K  | 295 K  |
|--|--------|--------|--------|--------|--------|
| <b>wRMSD</b>   |        |        |        |        |        |
| HAR/neutron  | 1.363  | 1.342  | -      | 2.262  | 1.629  |
| HAR-ELMO/neutron   | 1.466  | 1.263  | -      | 2.144  | 1.658  |
| HAR-ELMO/HAR   | 0.779  | 0.699  | 0.812  | 0.870  | 0.713  |
| <b>&lt;   U<sup>ij</sup><sub>A</sub> - U<sup>ij</sup><sub>B</sub>   &gt;</b> |        |        |        |        |        |
| HAR/neutron  | 0.0053 | 0.0048 | -      | 0.0078 | 0.0096 |
| HAR-ELMO/neutron   | 0.0058 | 0.0055 | -      | 0.0079 | 0.0109 |
| HAR-ELMO/HAR   | 0.0034 | 0.0033 | 0.0034 | 0.0036 | 0.0047 |
| <b>&lt;   U<sup>ii</sup><sub>A</sub> - U<sup>ii</sup><sub>B</sub>   &gt;</b> |        |        |        |        |        |
| HAR/neutron  | 0.0067 | 0.0053 | -      | 0.0051 | 0.0106 |
| HAR-ELMO/neutron   | 0.0071 | 0.0064 | -      | 0.0063 | 0.0121 |
| HAR-ELMO/HAR   | 0.0040 | 0.0043 | 0.0045 | 0.0049 | 0.0059 |
| <b>&lt; U<sup>ii</sup><sub>A</sub> / U<sup>ii</sup><sub>B</sub> &gt;</b>     |        |        |        |        |        |
| HAR/neutron  | 1.060  | 1.021  | -      | 1.056  | 1.116  |
| HAR-ELMO/neutron   | 1.147  | 1.104  | -      | 1.102  | 1.147  |
| HAR-ELMO/HAR   | 1.108  | 1.119  | 1.063  | 1.053  | 1.030  |

**Table S17:** Statistical results for hydrogen atom ADPs for *L*-Ala, units of differences are Å<sup>2</sup>.

| Method (A/B)  | 23 K   | 100 K  | 150 K  |
|---|--------|--------|--------|
| <b>wRMSD</b>  |        |        |        |
| HAR/neutron   | 1.958  | -      | 1.283  |
| HAR-ELMO/neutron  | 2.311  | -      | 1.586  |
| HAR-ELMO/HAR  | 0.991  | 1.571  | 0.656  |
| <b><math>\langle  U^{ij}_A - U^{ij}_B  \rangle</math></b> |        |        |        |
| HAR/neutron   | 0.0063 | -      | 0.0047 |
| HAR-ELMO/neutron  | 0.0082 | -      | 0.0063 |
| HAR-ELMO/HAR  | 0.0043 | 0.0035 | 0.0030 |
| <b><math>\langle  U^{ii}_A - U^{ii}_B  \rangle</math></b> |        |        |        |
| HAR/neutron   | 0.0069 | -      | 0.0056 |
| HAR-ELMO/neutron  | 0.0100 | -      | 0.0077 |
| HAR-ELMO/HAR  | 0.0049 | 0.0037 | 0.0032 |
| <b><math>\langle U^{ii}_A / U^{ii}_B \rangle</math></b>   |        |        |        |
| HAR/neutron   | 1.328  | -      | 1.042  |
| HAR-ELMO/neutron  | 1.441  | -      | 1.110  |
| HAR-ELMO/HAR  | 1.044  | 1.070  | 1.063  |

## Comparison of non-hydrogen ADPs

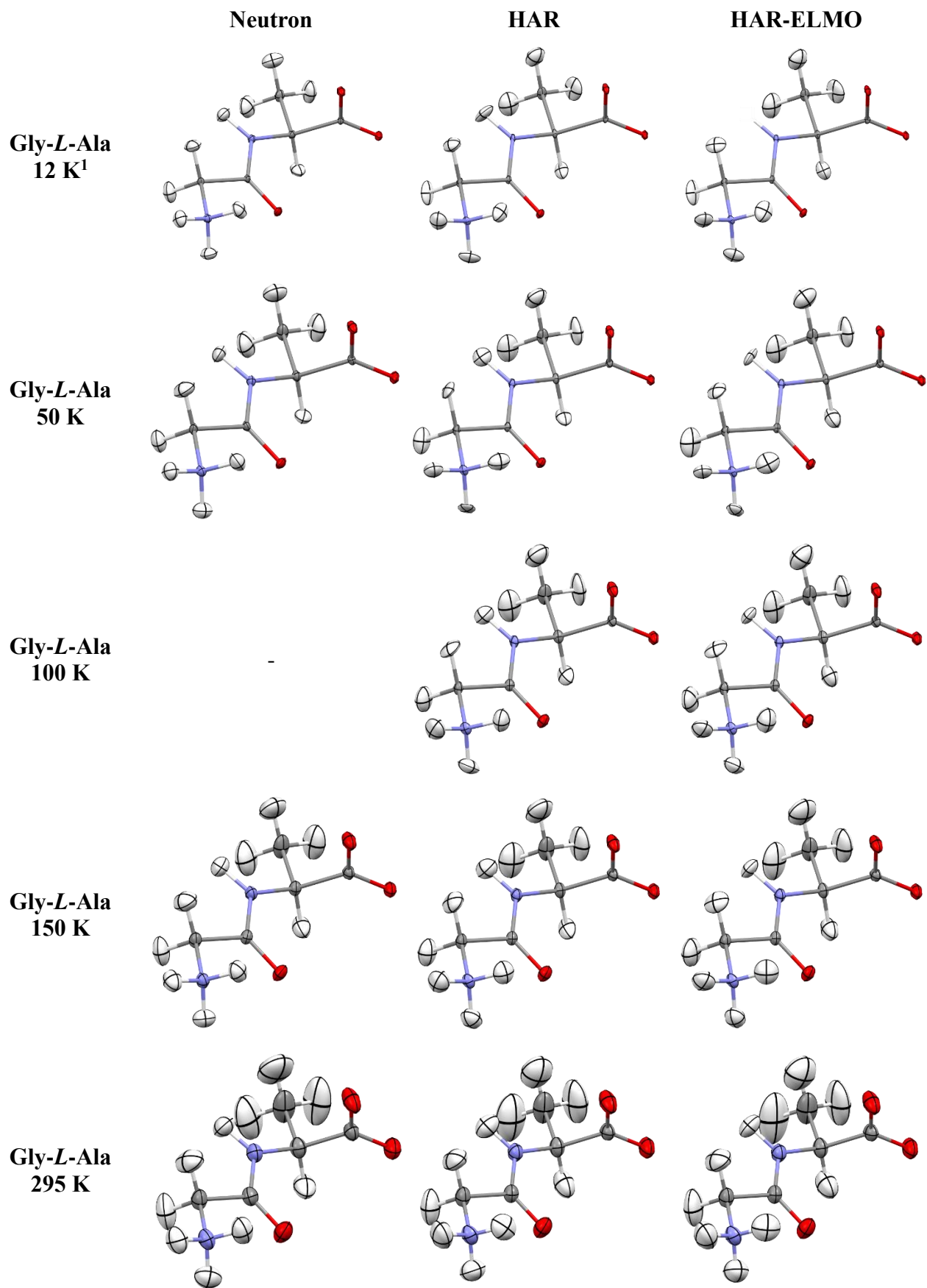
MADs (mean absolute differences) of non-hydrogen ADPs between independent X-ray and neutron measurements are often used as a quality control for the data and the refinements methods. For very high-quality data, MADs for non-hydrogen ADPs are expected to be in the range 0.0002 to 0.0005 Å<sup>2</sup>.<sup>S11-S13</sup> For the Gly-*L*-Ala data used here it is known that the results for the non-H ADPs are inferior (MADs in the range 0.0010 to 0.0014 Å<sup>2</sup>).<sup>S7</sup> It is believed that this is due to missing oblique-incidence correction.

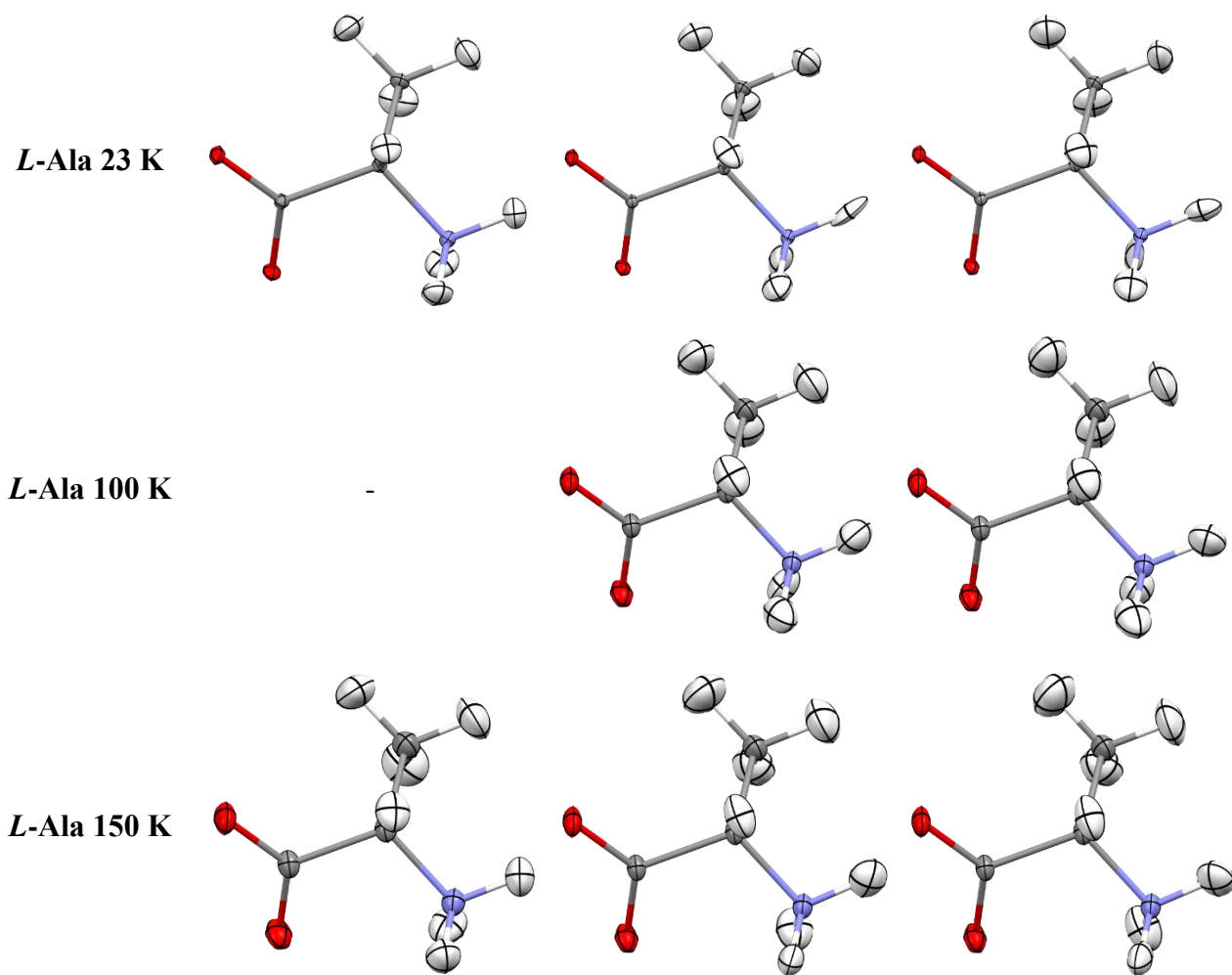
**Table S18:** Statistical results for non-hydrogen atom ADPs of Gly-*L*-Ala, units of differences are Å<sup>2</sup>.

| Method (A/B)   | 12 K    | 50 K    | 100 K   | 150 K   | 295 K   |
|--|---------|---------|---------|---------|---------|
| <b>wRMSD</b>   |         |         |         |         |         |
| IAM/neutron  | 2.273   | 2.212   | -       | 2.068   | 1.468   |
| HAR/neutron  | 2.578   | 2.669   | -       | 2.251   | 1.468   |
| HAR-ELMO/neutron   | 2.715   | 2.755   | -       | 2.357   | 1.526   |
| HAR-ELMO/HAR   | 1.559   | 1.374   | 1.570   | 1.583   | 1.536   |
| <b>&lt;   U<sup>ij</sup><sub>A</sub> - U<sup>ij</sup><sub>B</sub>   &gt;</b> |         |         |         |         |         |
| IAM/neutron  | 0.00108 | 0.00107 | -       | 0.00122 | 0.00147 |
| HAR/neutron  | 0.00110 | 0.00122 | -       | 0.00118 | 0.00133 |
| HAR-ELMO/neutron   | 0.00119 | 0.00129 | -       | 0.00125 | 0.00136 |
| HAR-ELMO/HAR   | 0.00020 | 0.00022 | 0.00019 | 0.00021 | 0.00029 |
| <b>&lt;   U<sup>ii</sup><sub>A</sub> - U<sup>ii</sup><sub>B</sub>   &gt;</b> |         |         |         |         |         |
| IAM/neutron  | 0.00140 | 0.00144 | -       | 0.00149 | 0.00177 |
| HAR/neutron  | 0.00167 | 0.00178 | -       | 0.00168 | 0.00149 |
| HAR-ELMO/neutron   | 0.00177 | 0.00189 | -       | 0.00176 | 0.00161 |
| HAR-ELMO/HAR   | 0.00019 | 0.00021 | 0.00018 | 0.00019 | 0.00028 |
| <b>&lt; U<sup>ii</sup><sub>A</sub> / U<sup>ii</sup><sub>B</sub> &gt;</b>     |         |         |         |         |         |
| IAM/neutron  | 0.863   | 0.889   | -       | 0.937   | 1.011   |
| HAR/neutron  | 0.749   | 0.784   | -       | 0.891   | 0.966   |
| HAR-ELMO/neutron   | 0.735   | 0.773   | -       | 0.885   | 0.958   |
| HAR-ELMO/HAR   | 0.977   | 0.984   | 0.990   | 0.993   | 0.992   |

**Table S19:** Statistical results for non-hydrogen atom ADPs for *L*-Ala units of differences are Å<sup>2</sup>.

| Method (A/B)   | 23 K    | 100 K   | 150 K   |
|--|---------|---------|---------|
| <b>wRMSD</b>   |         |         |         |
| IAM/neutron  | 3.667   | -       | 51.759  |
| HAR/neutron  | 2.832   | -       | 8.419   |
| HAR-ELMO/neutron   | 2.936   | -       | 8.385   |
| HAR-ELMO/HAR   | 1.018   | 2.278   | 1.012   |
| <b>&lt;   U<sup>ij</sup><sub>A</sub> - U<sup>ij</sup><sub>B</sub>   &gt;</b> |         |         |         |
| IAM/neutron  | 0.00032 | -       | 0.00156 |
| HAR/neutron  | 0.00034 | -       | 0.00162 |
| HAR-ELMO/neutron   | 0.00036 | -       | 0.00163 |
| HAR-ELMO/HAR   | 0.00008 | 0.00012 | 0.00010 |
| <b>&lt;   U<sup>ii</sup><sub>A</sub> - U<sup>ii</sup><sub>B</sub>   &gt;</b> |         |         |         |
| IAM/neutron  | 0.00043 | -       | 0.00272 |
| HAR/neutron  | 0.00058 | -       | 0.00295 |
| HAR-ELMO/neutron   | 0.00060 | -       | 0.00297 |
| HAR-ELMO/HAR   | 0.00009 | 0.00013 | 0.00011 |
| <b>&lt; U<sup>ii</sup><sub>A</sub> / U<sup>ii</sup><sub>B</sub> &gt;</b>     |         |         |         |
| IAM/neutron  | 0.967   | -       | 0.821   |
| HAR/neutron  | 0.913   | -       | 0.805   |
| HAR-ELMO/neutron   | 0.909   | -       | 0.804   |
| HAR-ELMO/HAR   | 0.995   | 0.999   | 0.998   |





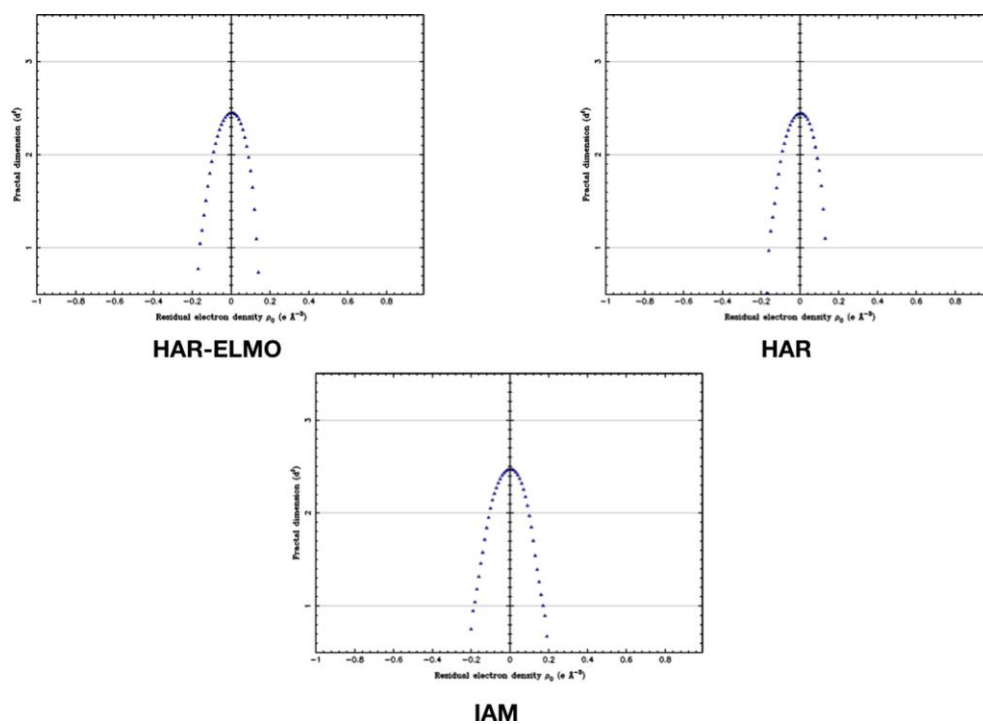
**Figure S5:** Molecular representations of the refined structures with 50% probability ADPs for Gly-*L*-Ala and *L*-Ala at all temperatures.

<sup>1</sup>For Gly-*L*-Ala 12 K, H(11) is non-positive definite (NPD), but this is only due to the small ADPs. Except for  $U_{33}$ , the values are still matching the  $U_{ij}$ s resulting from HAR, which are not NPD, within one standard deviation. The H(11)  $U_{ij}$ s ( $U_{11}$   $U_{22}$   $U_{33}$   $U_{23}$   $U_{13}$   $U_{12}$ , respectively) resulting from the HAR and HAR-ELMO refinements are:

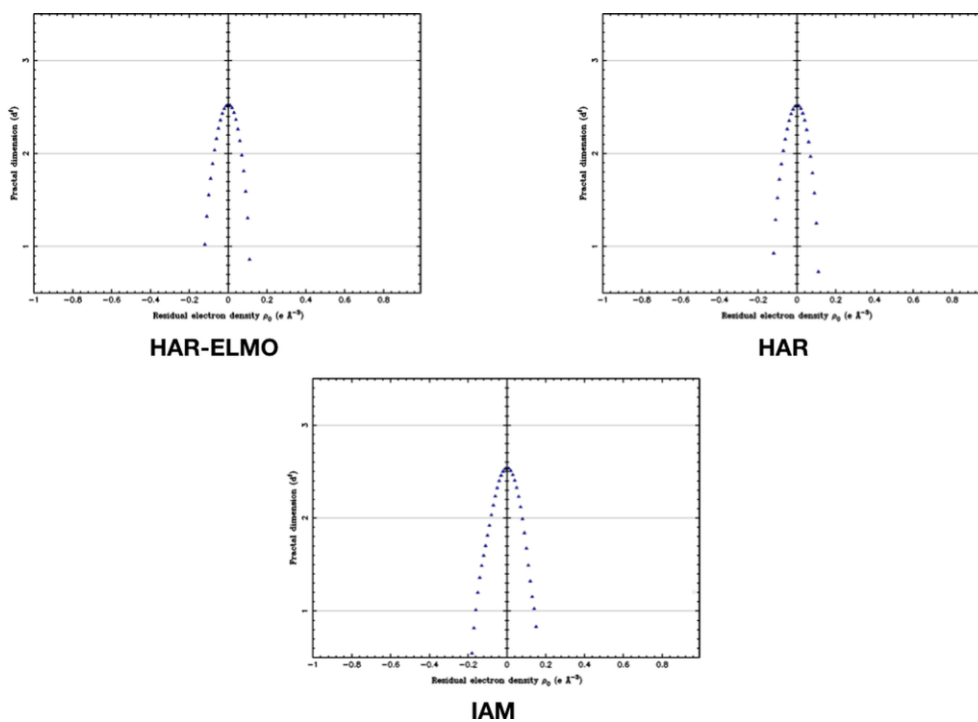
HAR:                0.019(4) 0.021(5) 0.024(3) 0.006(4) -0.014(3) 0.008(4) Å<sup>2</sup>  
HAR-ELMO:        0.011(4) 0.020(5) 0.013(3) 0.000(4) -0.017(3) 0.004(4) Å<sup>2</sup>

## Comparison of Fractal Dimension plots

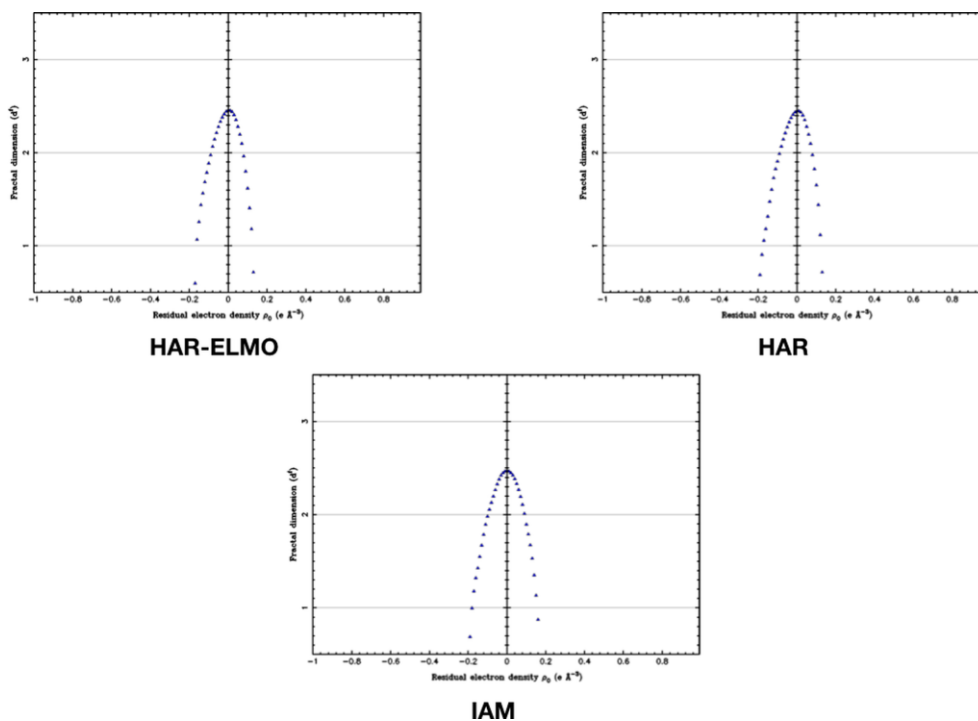
Gly-*L*-Ala – Fractal Dimension plots according to Meindl & Henn<sup>S14</sup>



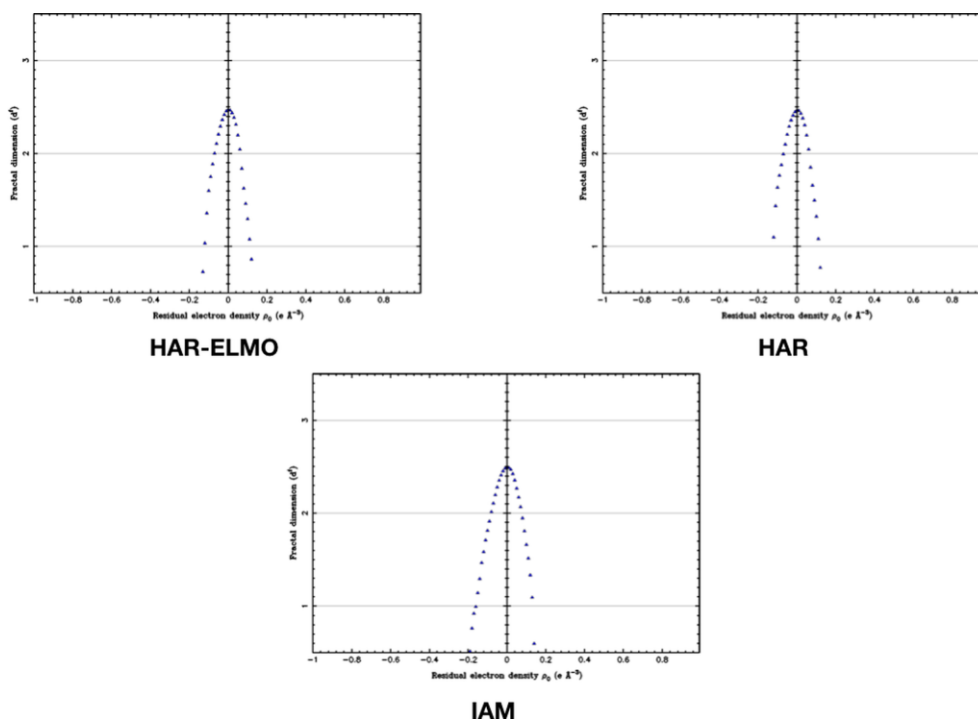
**Figure S6:** Fractal dimension plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 12 K.



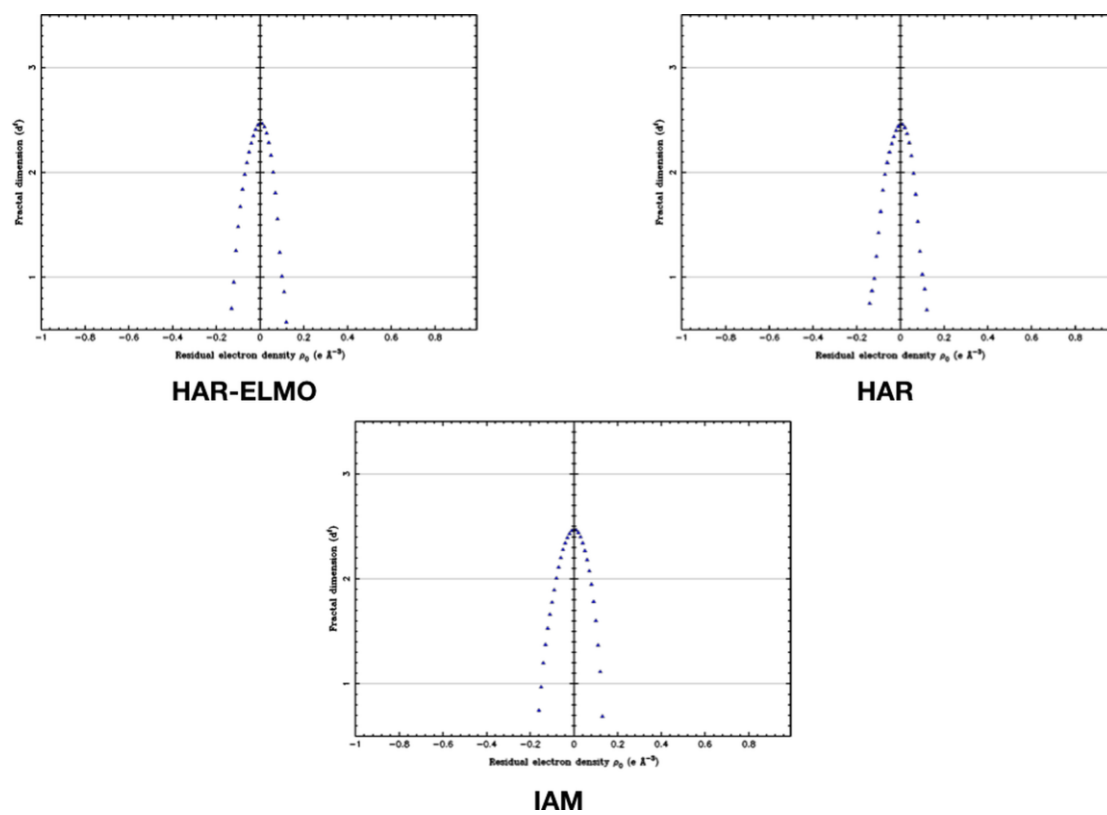
**Figure S7:** Fractal dimension plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 50 K.



**Figure S8:** Fractal dimension plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 100 K.

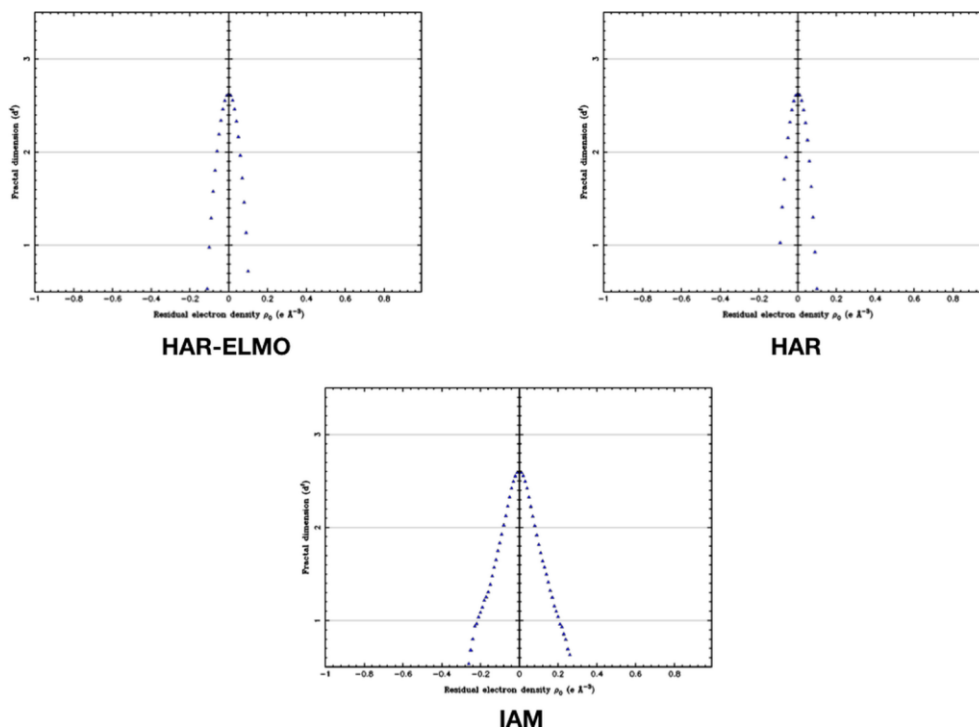


**Figure S9:** Fractal dimension plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 150 K.

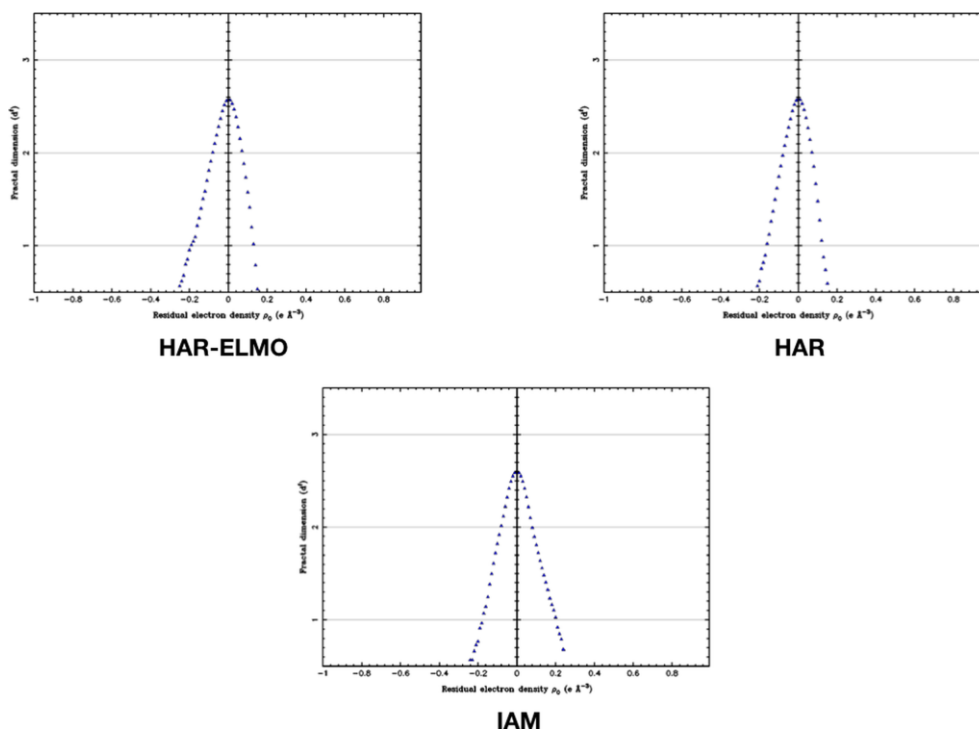


**Figure S10:** Fractal dimension plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 295 K.

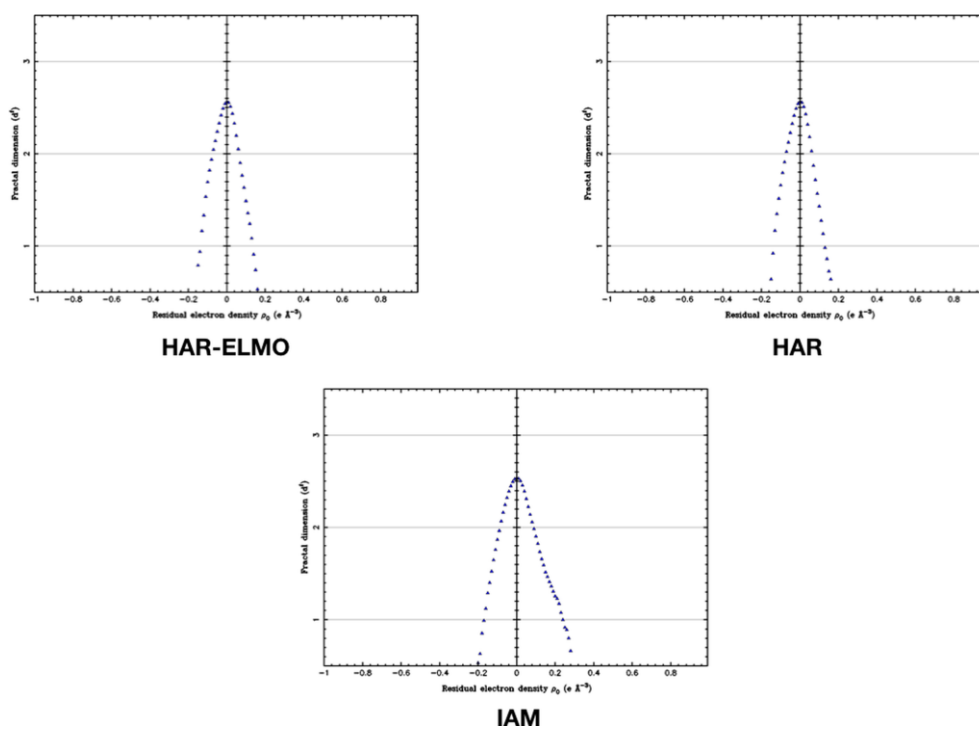
***L*-Alanine – Fractal Dimension plots according to Meindl & Henn<sup>S14</sup>**



**Figure S11:** Fractal dimension plots for the HAR-ELMO, HAR and IAM refinements of *L*-Ala at 23 K.



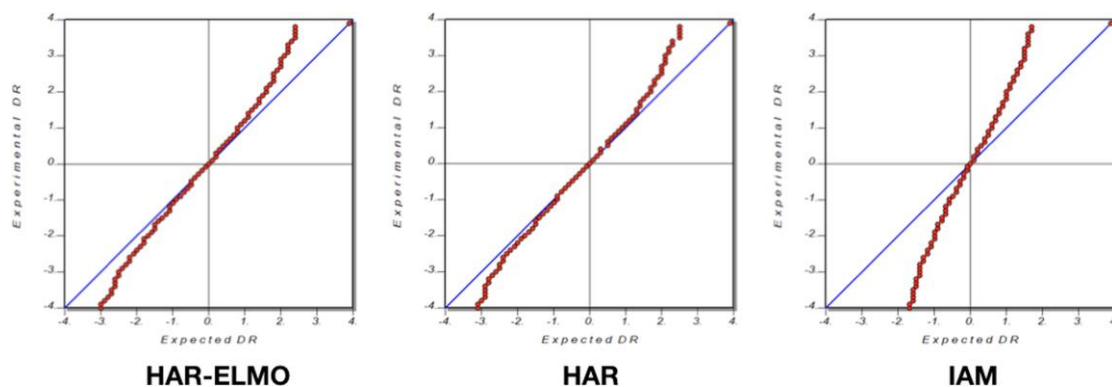
**Figure S12:** Fractal dimension plots for the HAR-ELMO, HAR and IAM refinements of *L*-Ala at 100 K.



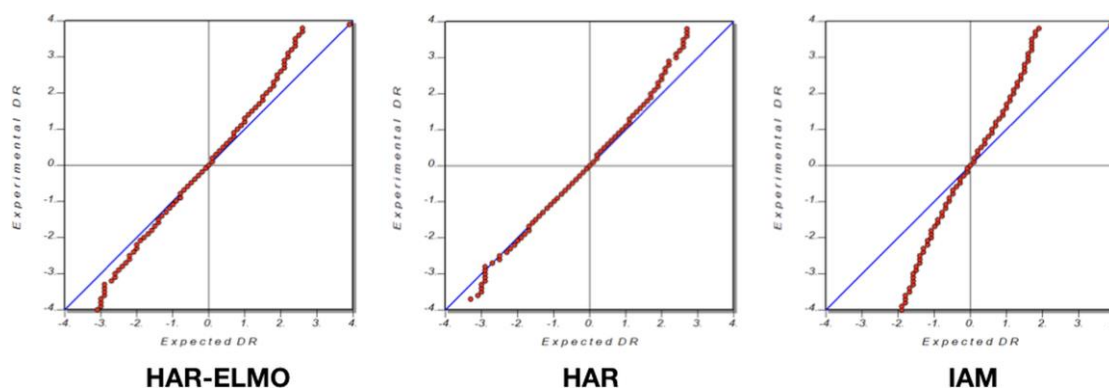
**Figure S13:** Fractal dimension plots for the HAR-ELMO, HAR and IAM refinements of *L*-Ala at 150 K.

## Comparison of Normal Probability plots

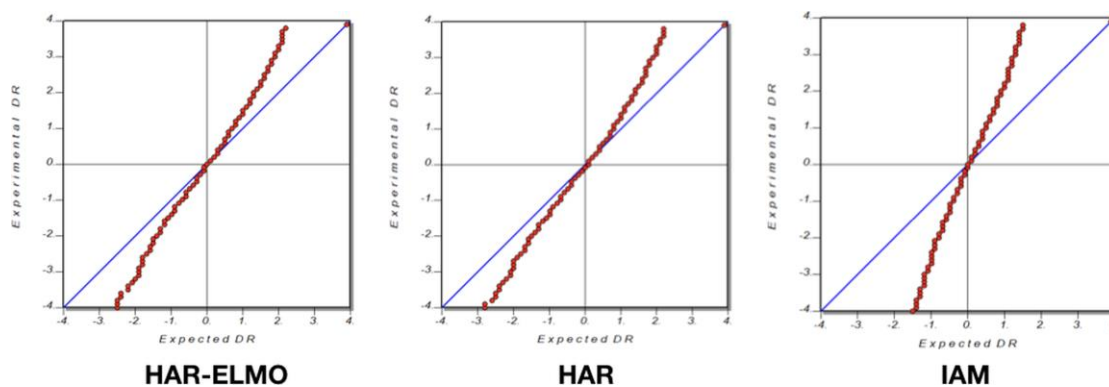
### Gly-*L*-Ala – Normal Probability plots



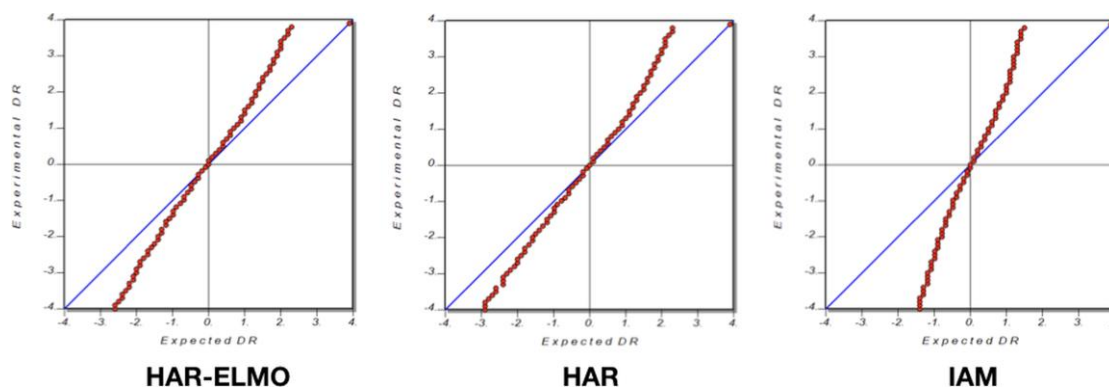
**Figure S14:** Normal probability plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 12 K.



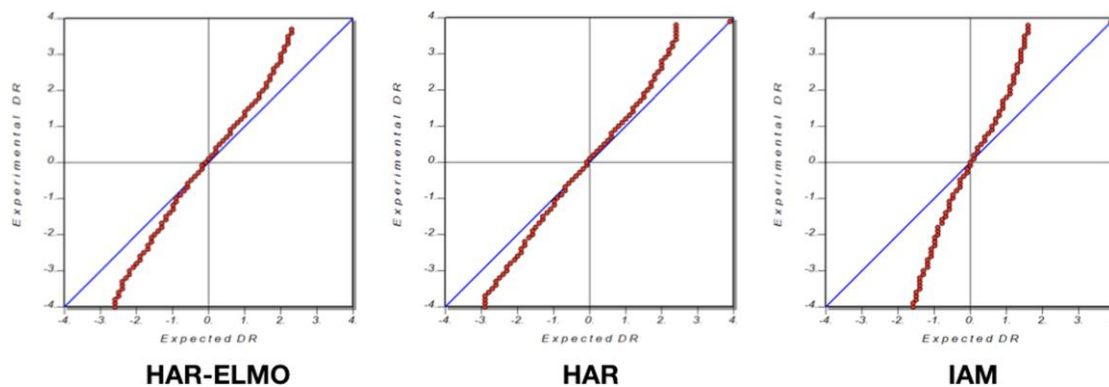
**Figure S15:** Normal probability plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 50 K.



**Figure S16:** Normal probability plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 100 K.

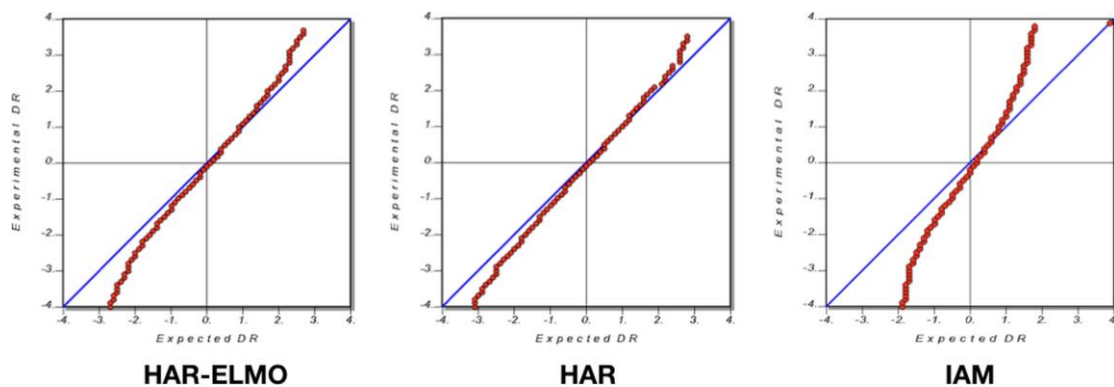


**Figure S17:** Normal probability plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 150 K.

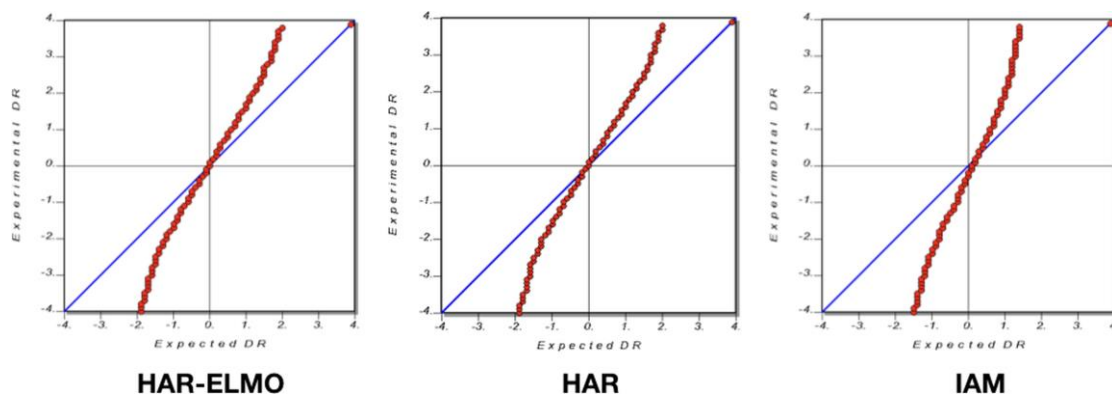


**Figure S18:** Normal probability plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 295 K.

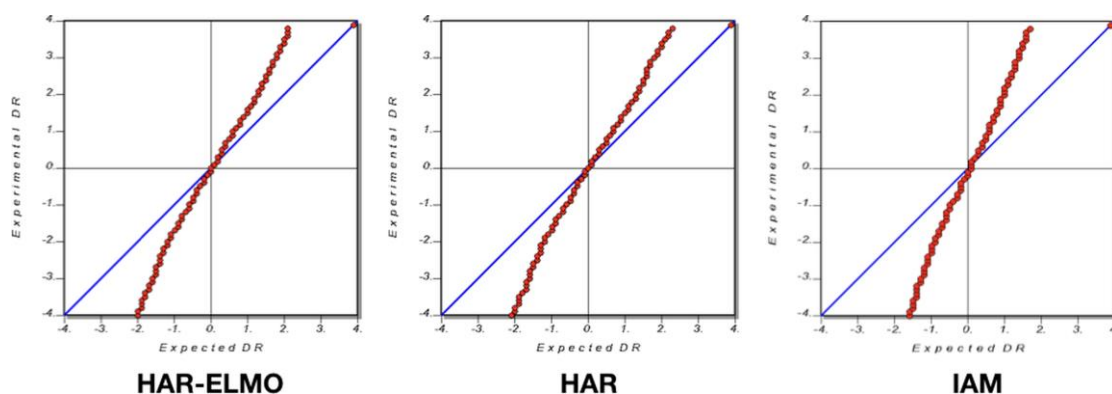
## L-Alanine – Normal Probability plots



**Figure S19:** Normal probability plots for the HAR-ELMO, HAR and IAM refinements of L-Ala at 23 K.



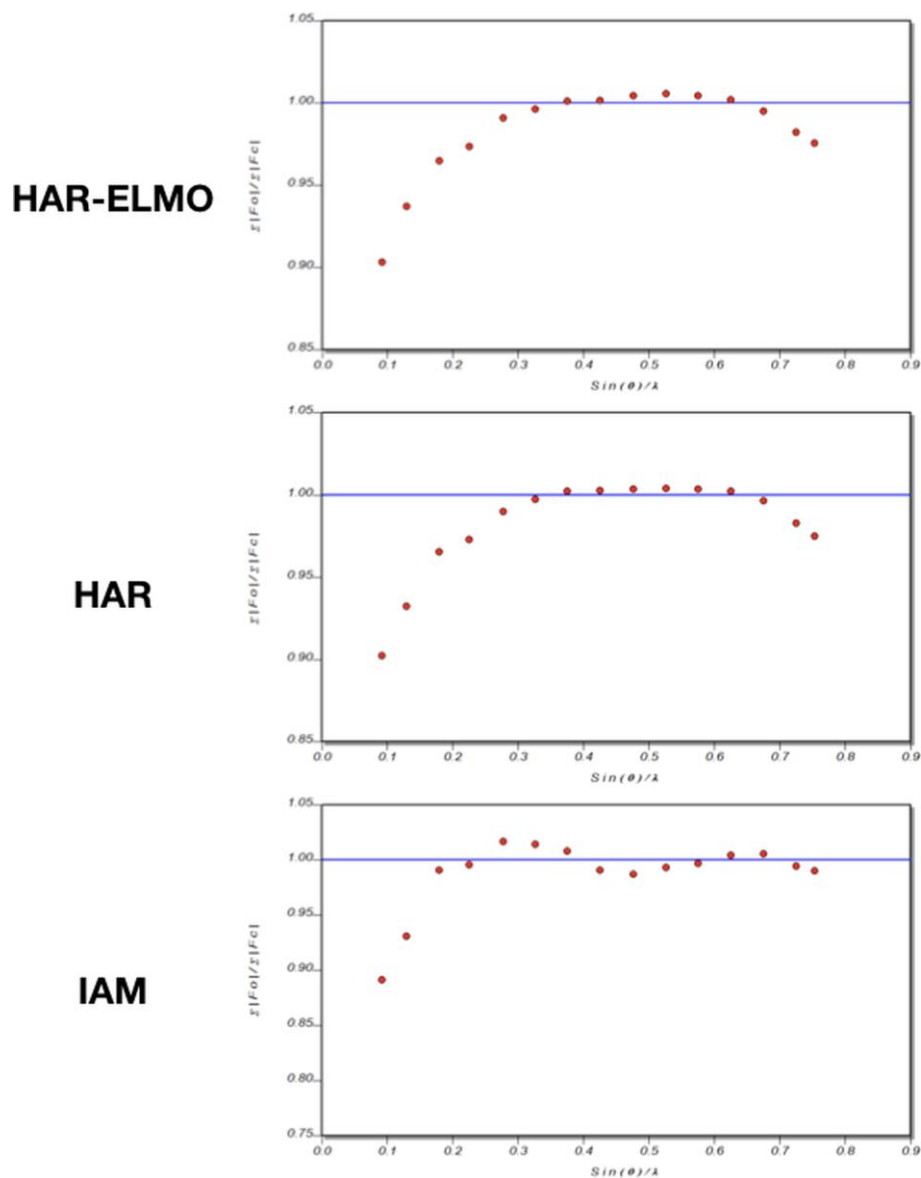
**Figure S20:** Normal probability plots for the HAR-ELMO, HAR and IAM refinements of L-Ala at 100 K.



**Figure S21:** Normal probability plots for the HAR-ELMO, HAR and IAM refinements of L-Ala at 150 K.

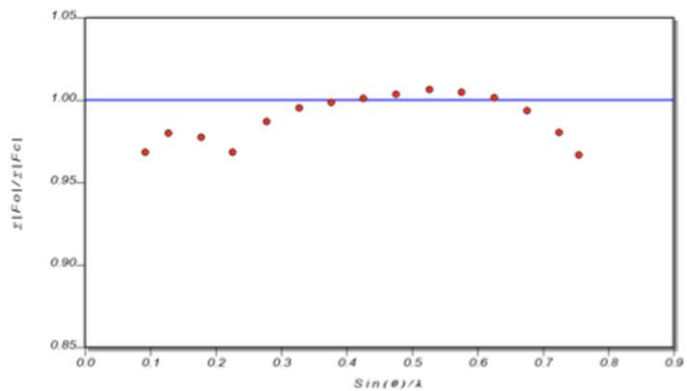
## Comparison of Averaged-K-curve plots

### Gly-*L*-Ala – Averaged K-curve plots

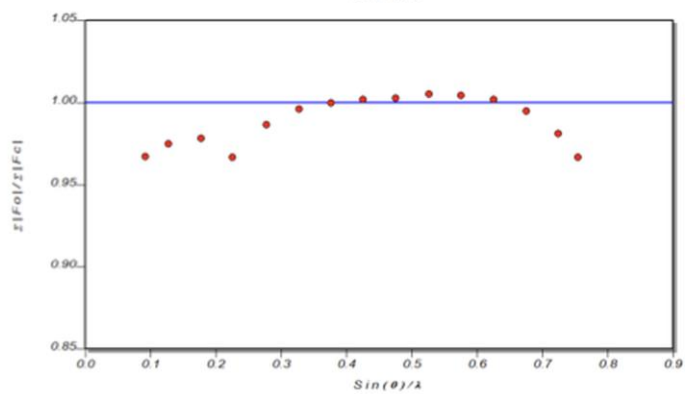


**Figure S22:** Averaged K-curve plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 12 K.

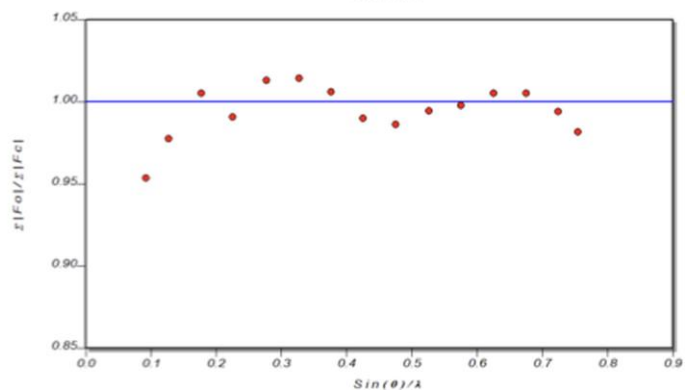
**HAR-ELMO**



**HAR**

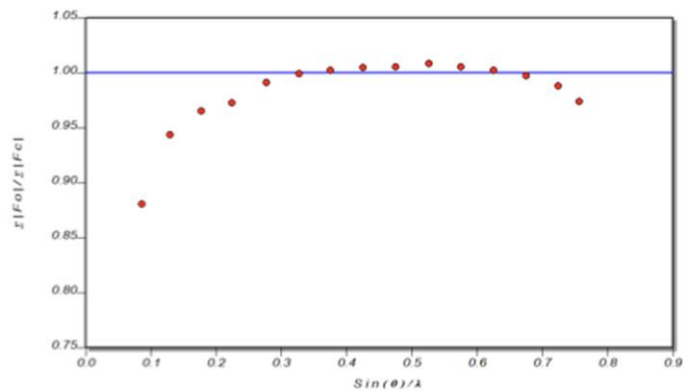


**IAM**

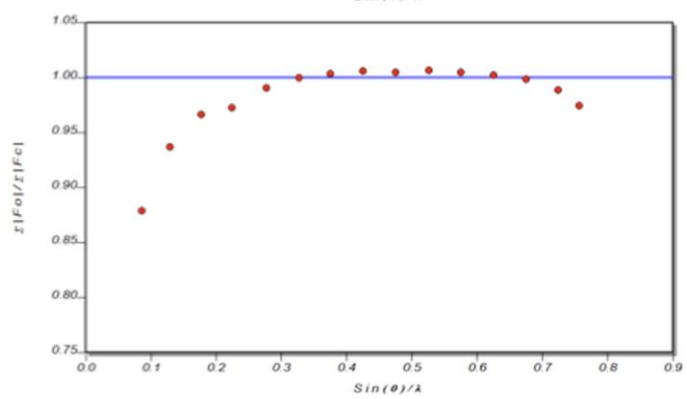


**Figure S23:** Averaged K-curve plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 50 K.

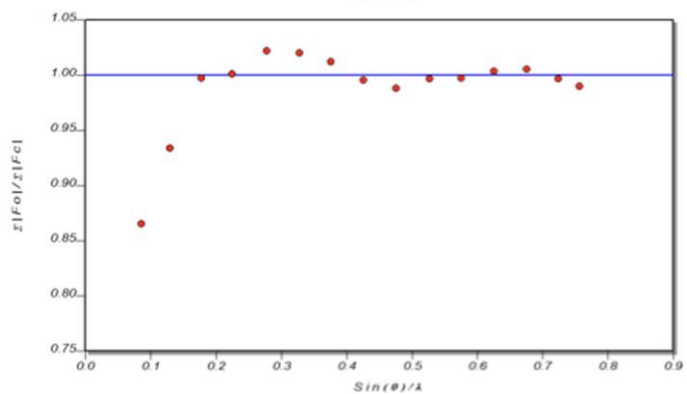
**HAR-ELMO**



**HAR**

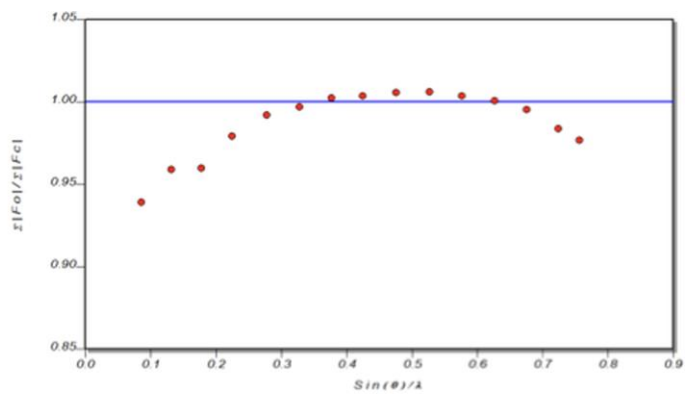


**IAM**

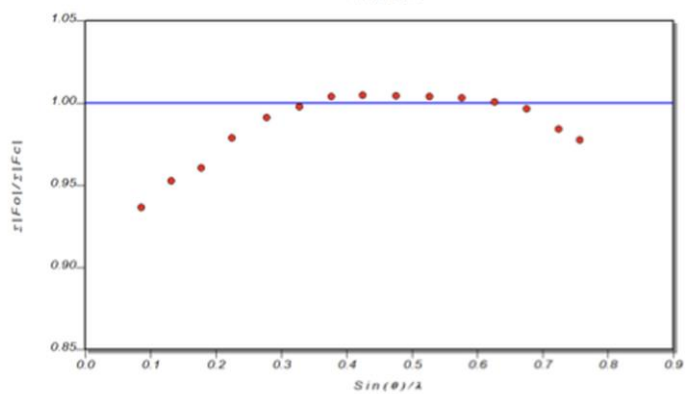


**Figure S24:** Averaged K-curve plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 100 K.

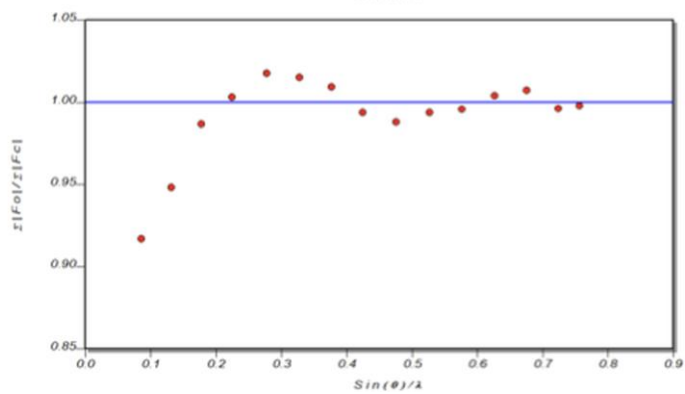
**HAR-ELMO**



**HAR**

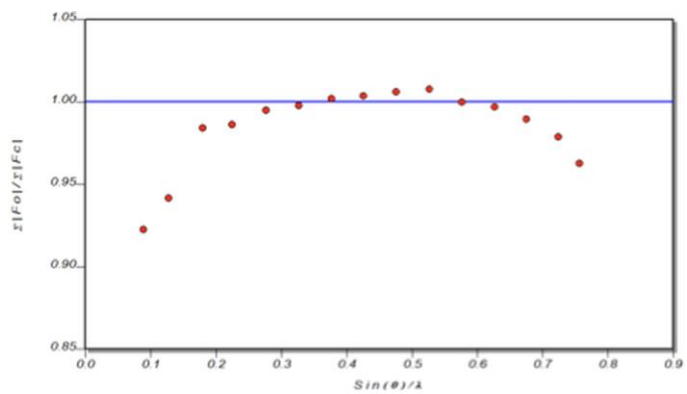


**IAM**

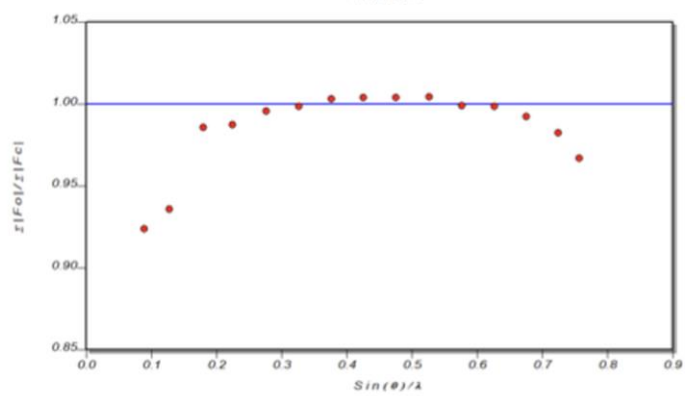


**Figure S25:** Averaged K-curve plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 150 K.

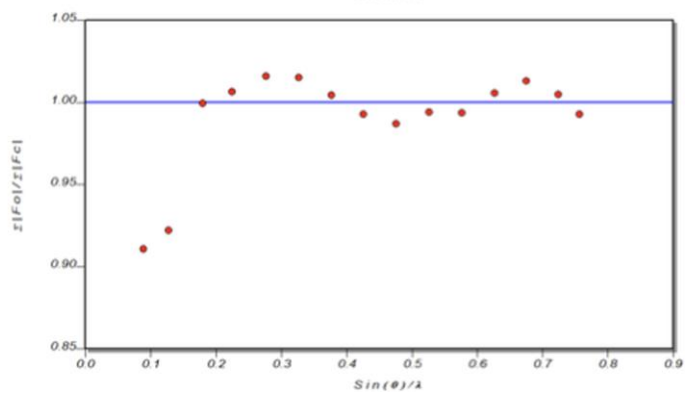
**HAR-ELMO**



**HAR**

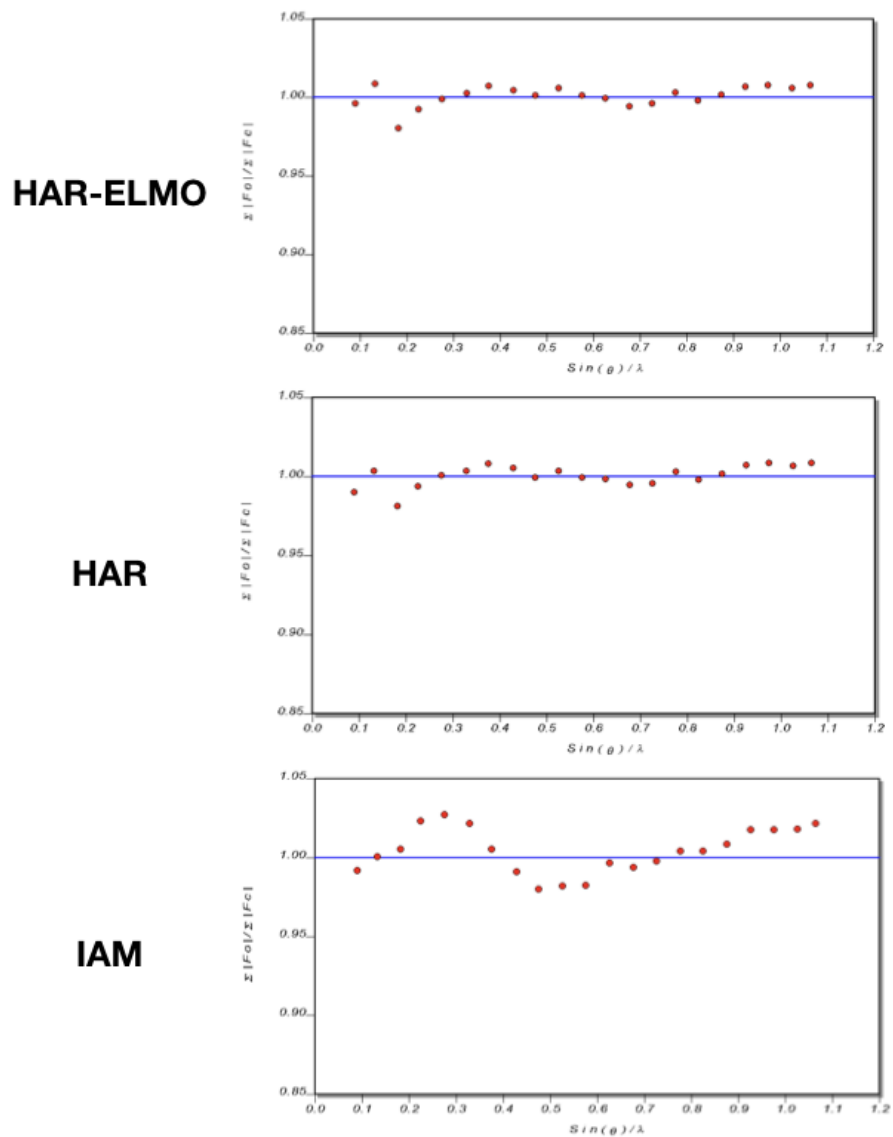


**IAM**



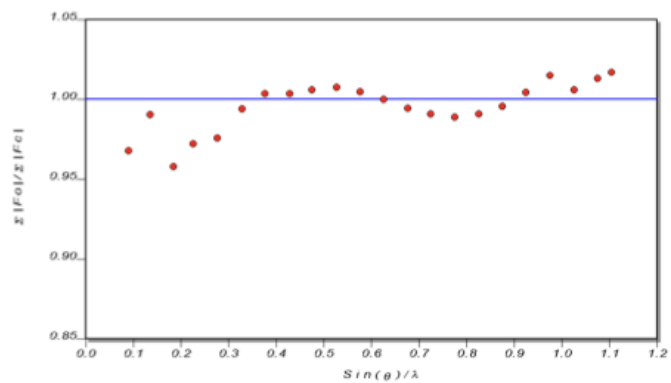
**Figure S26:** Averaged K-curve plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 295 K.

## L-Alanine – Averaged K-curve plots

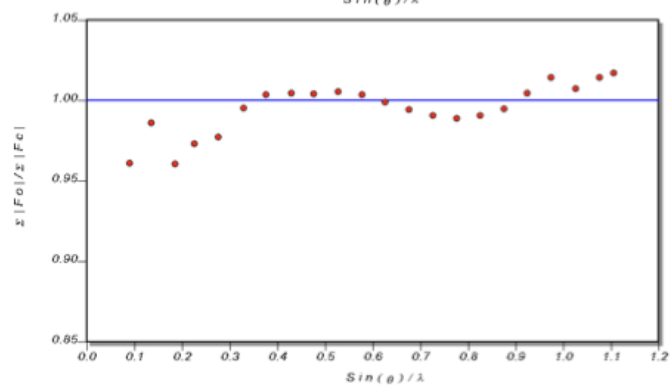


**Figure S27:** Averaged K-curve plots for the HAR-ELMO, HAR and IAM refinements of *L*-Ala at 23 K.

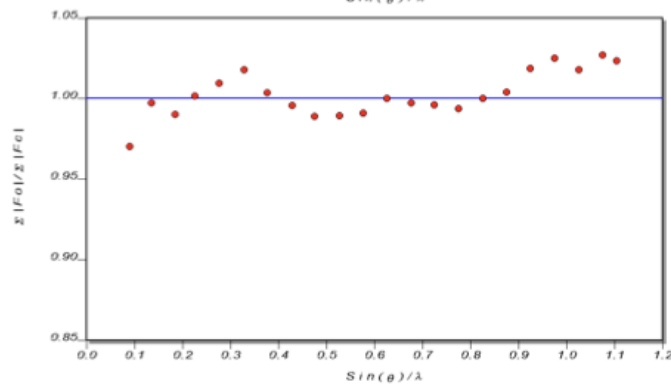
**HAR-ELMO**



**HAR**

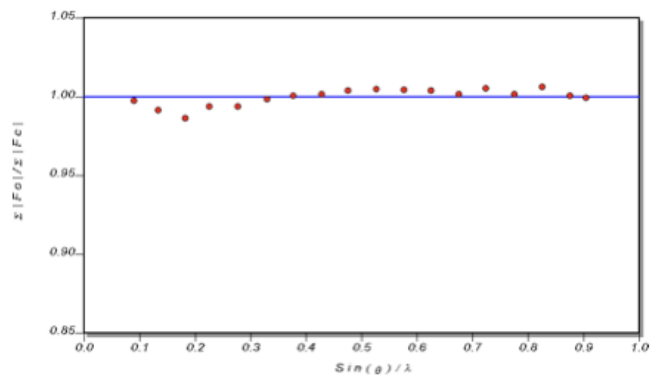


**IAM**

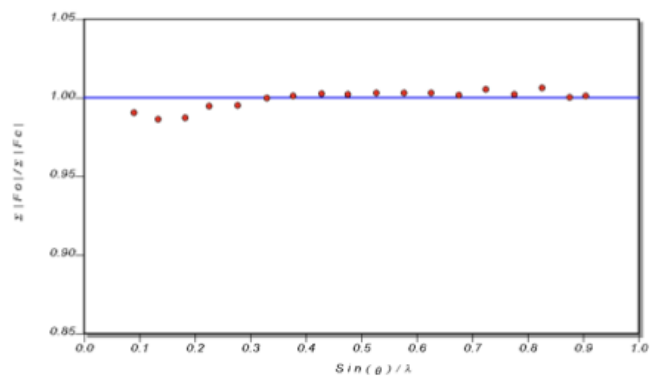


**Figure S28:** Averaged K-curve plots for the HAR-ELMO, HAR and IAM refinements of *L*-Ala at 100 K.

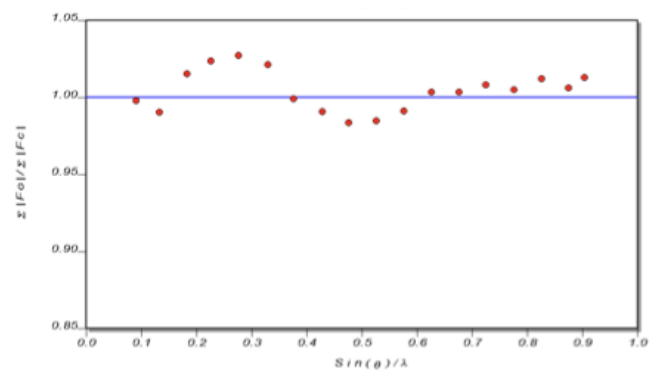
**HAR-ELMO**



**HAR**



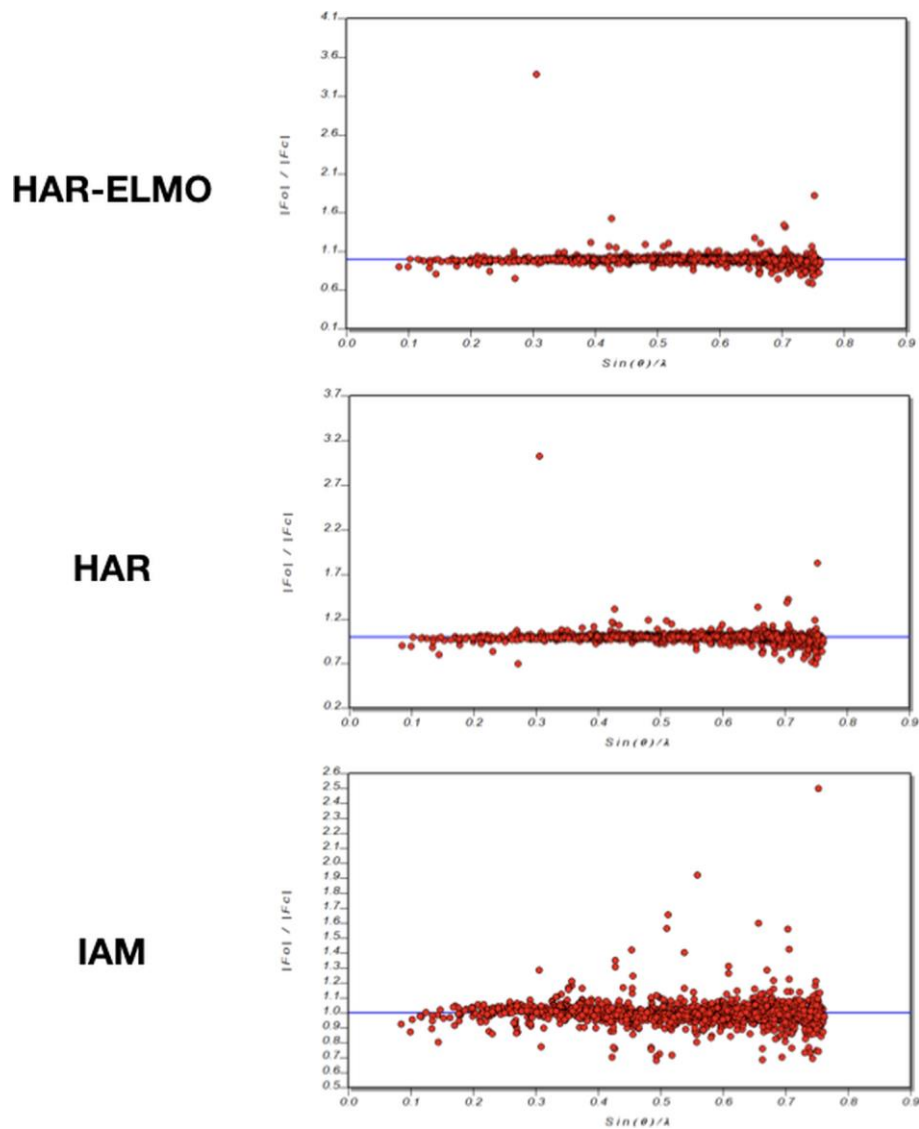
**IAM**



**Figure S29:** Averaged K-curve plots for the HAR-ELMO, HAR and IAM refinements of *L*-Ala at 150 K.

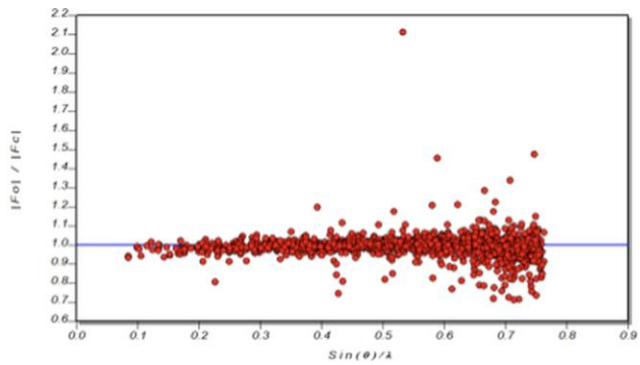
# Comparison of Complete-K-curve plots

## Gly-*L*-Ala – Complete K-curve plots

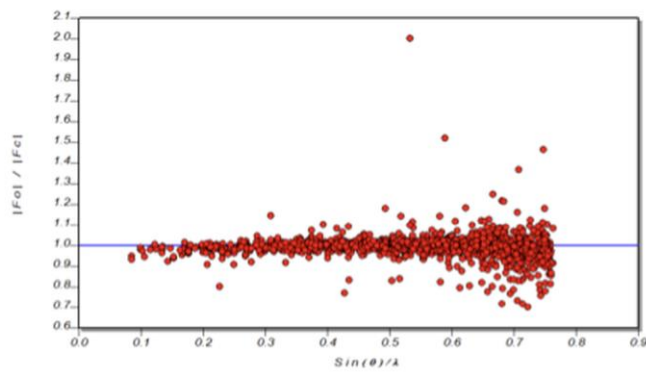


**Figure S30:** Complete K-curve plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 12 K.

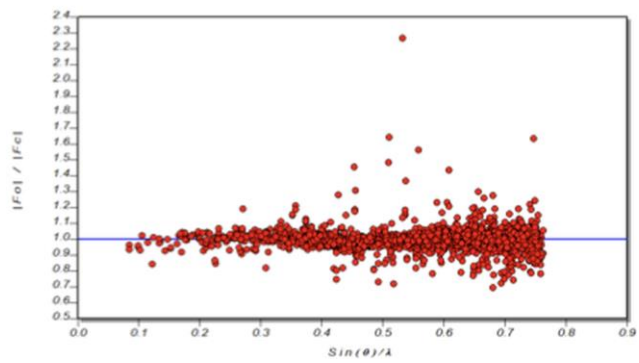
**HAR-ELMO**



**HAR**

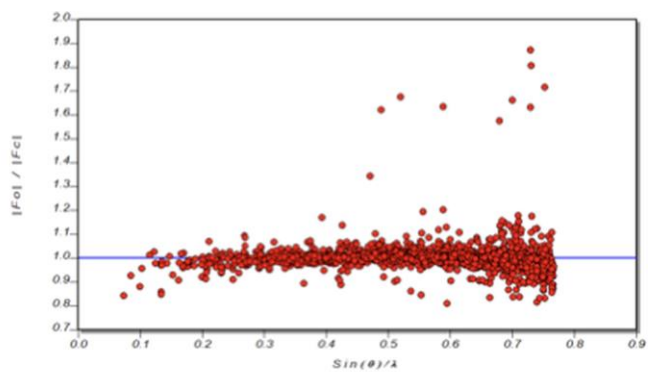


**IAM**

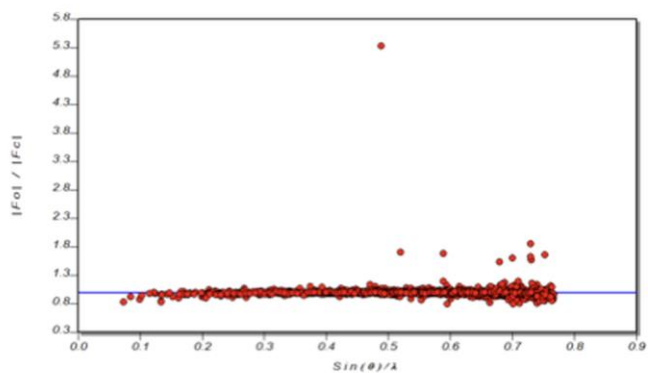


**Figure S31:** Complete K-curve plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 50 K.

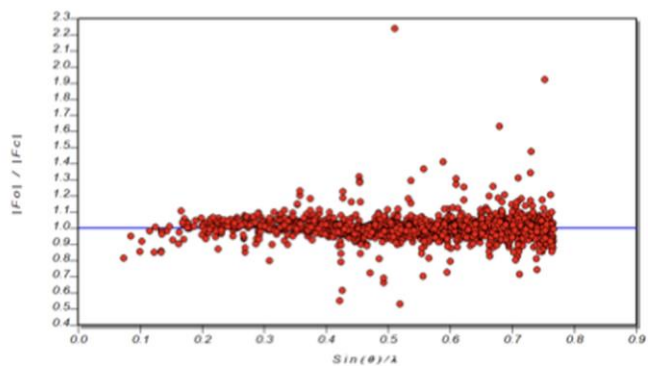
**HAR-ELMO**



**HAR**

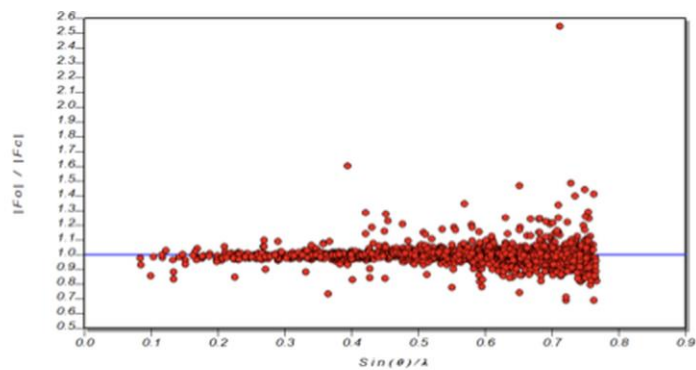


**IAM**

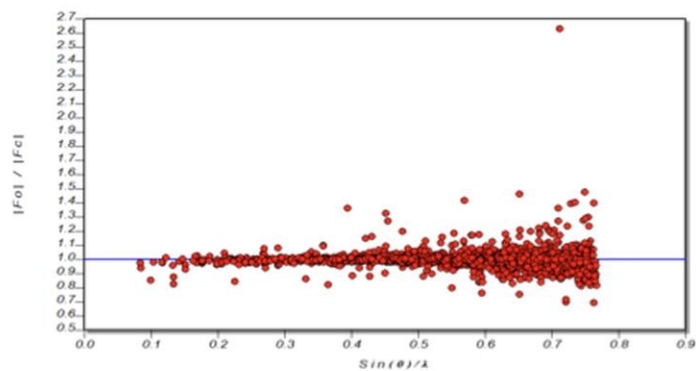


**Figure S32:** Complete K-curve plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 100 K.

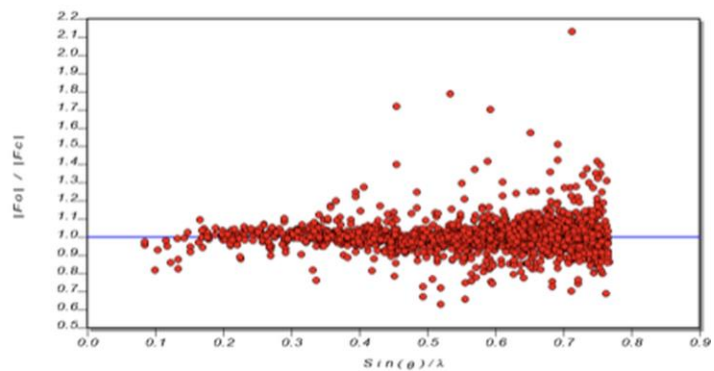
**HAR-ELMO**



**HAR**

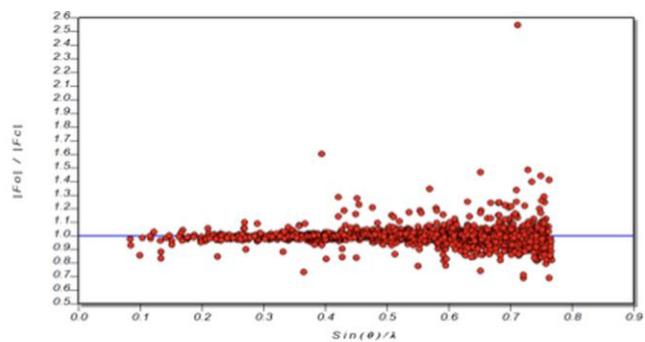


**IAM**

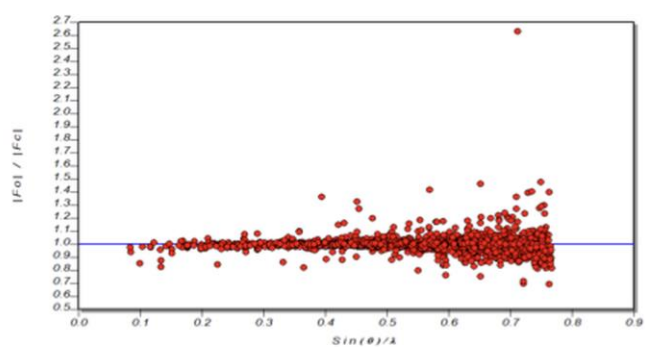


**Figure S33:** Complete K-curve plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 150 K.

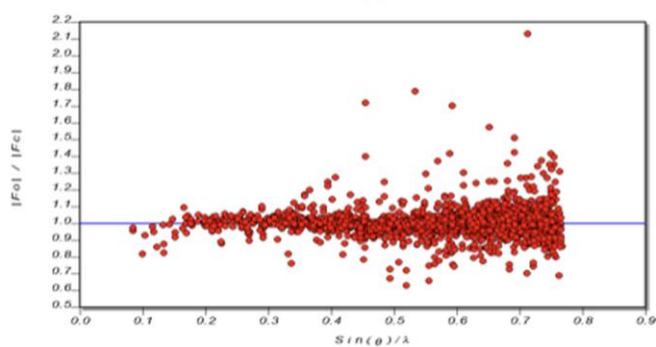
**HAR-ELMO**



**HAR**

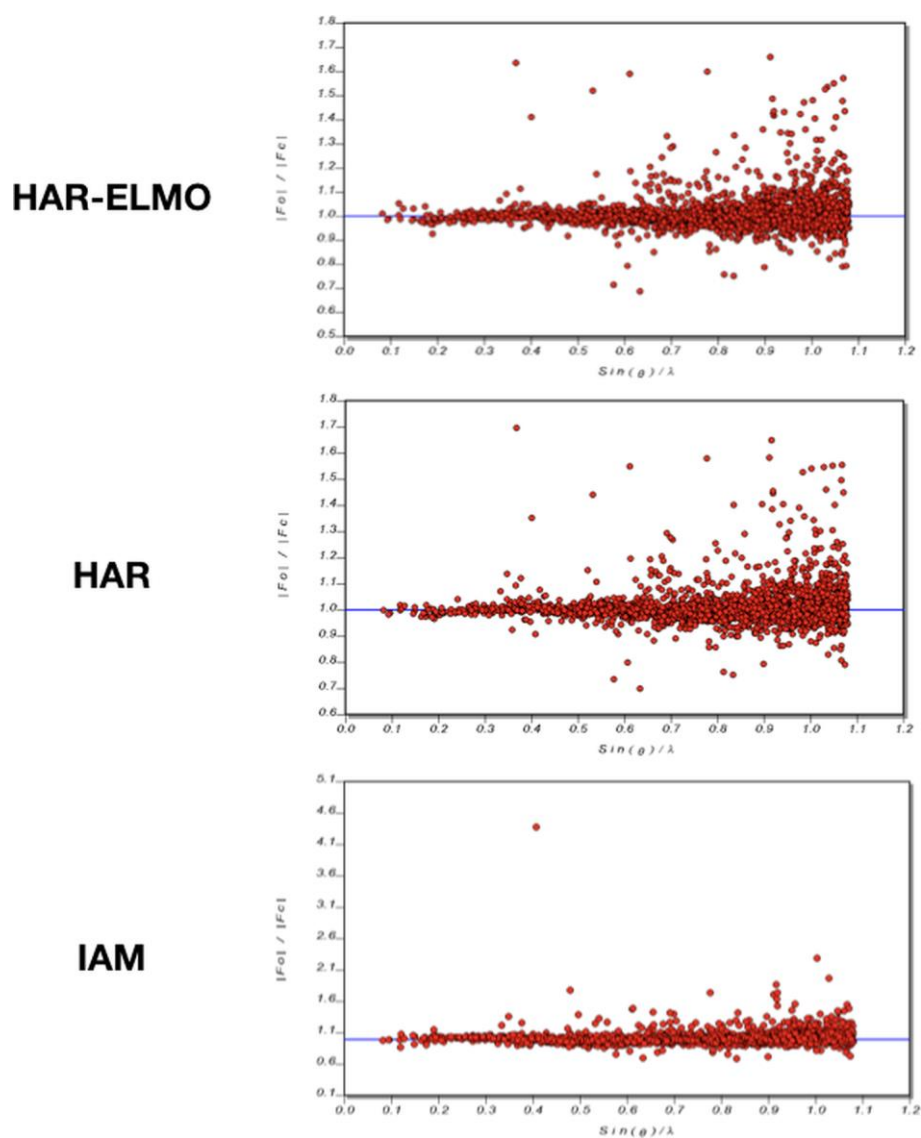


**IAM**



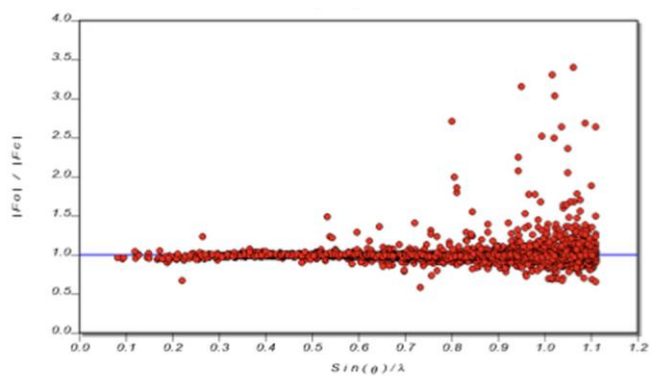
**Figure S34:** Complete K-curve plots for the HAR-ELMO, HAR and IAM refinements of Gly-*L*-Ala at 295 K.

## *L*-Alanine – Complete K-curve plots

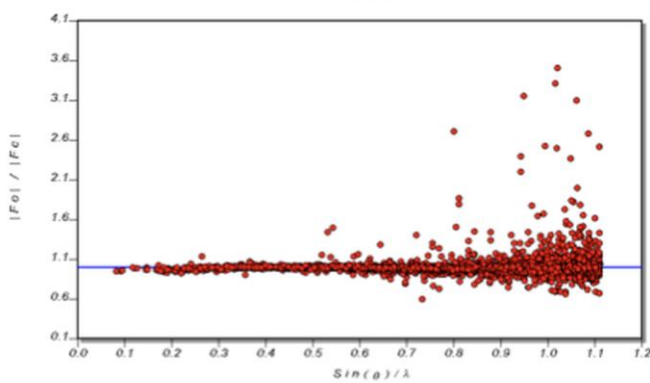


**Figure S35:** Complete K-curve plots for the HAR-ELMO, HAR and IAM refinements of *L*-Ala at 23 K.

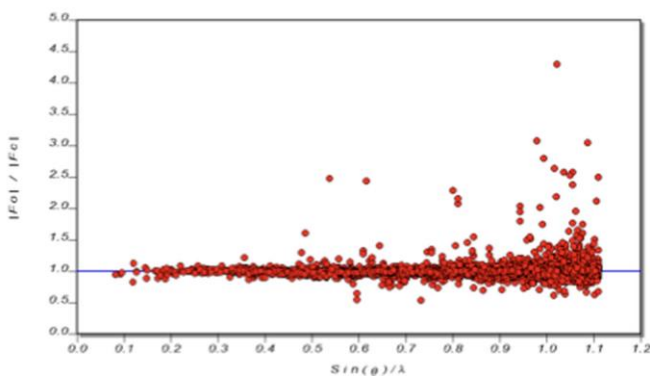
**HAR-ELMO**



**HAR**

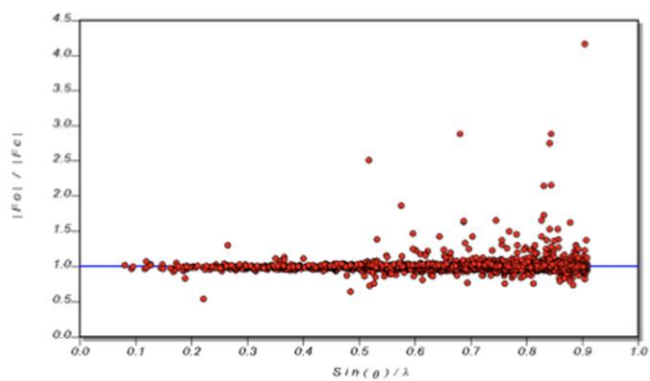


**IAM**

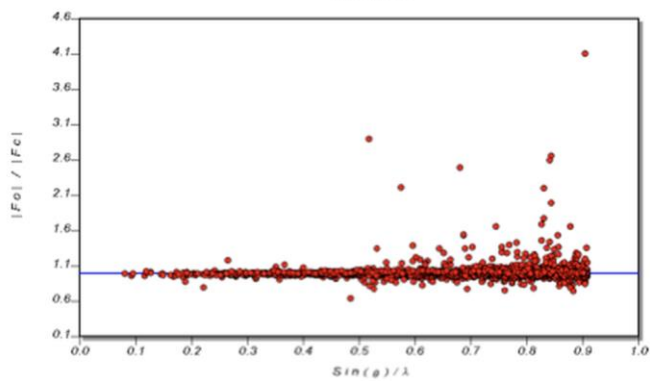


**Figure S36:** Complete K-curve plots for the HAR-ELMO, HAR and IAM refinements of *L*-Ala at 100 K.

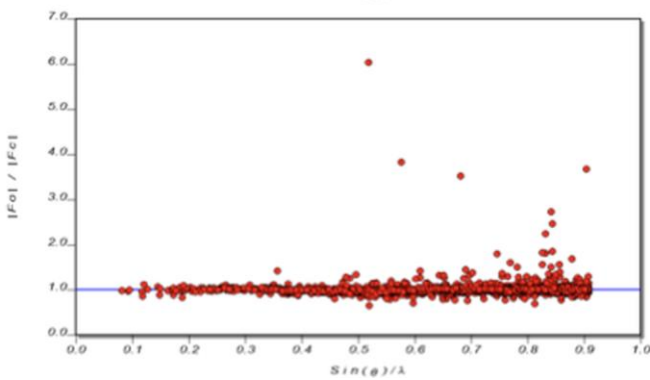
**HAR-ELMO**



**HAR**



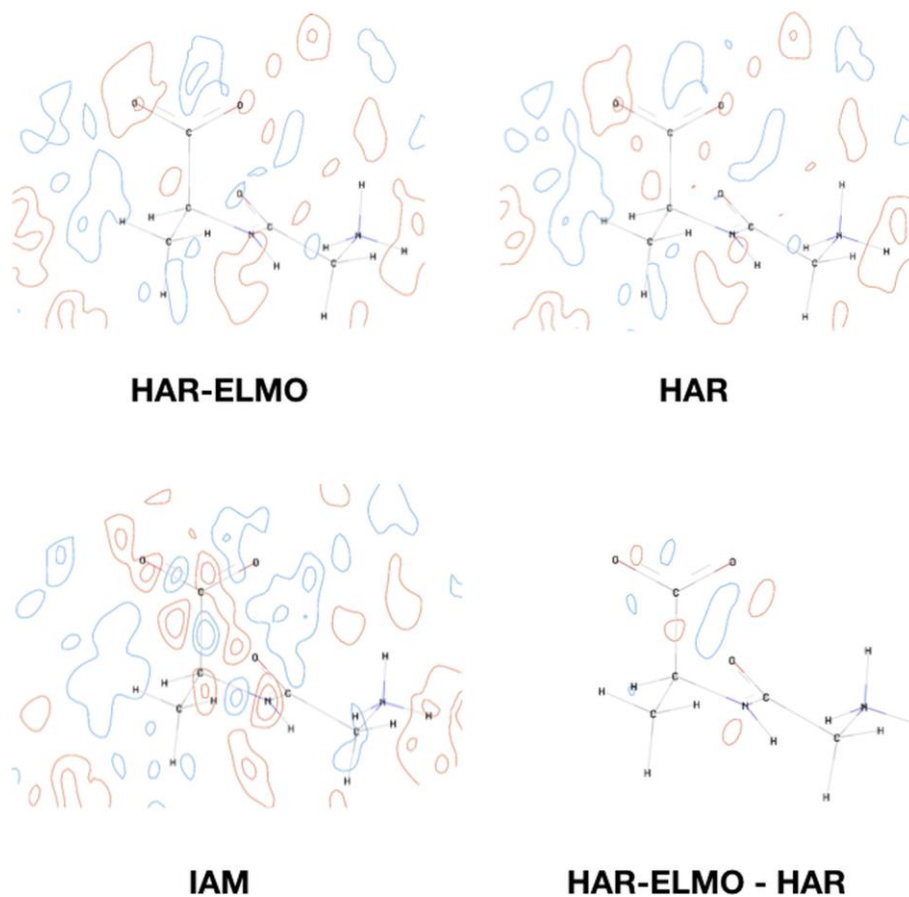
**IAM**



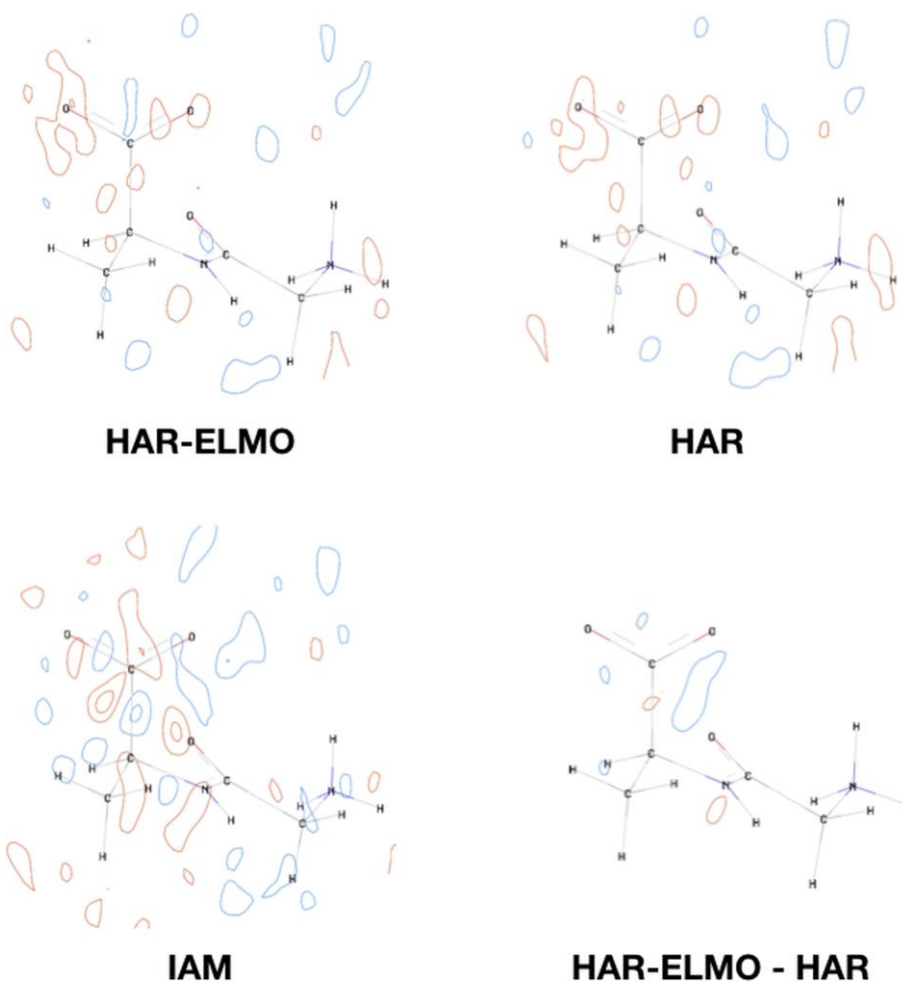
**Figure S37:** Complete K-curve plots for the HAR-ELMO, HAR and IAM refinements of *L*-Ala at 150 K.

## Comparison of residual and deformation densities

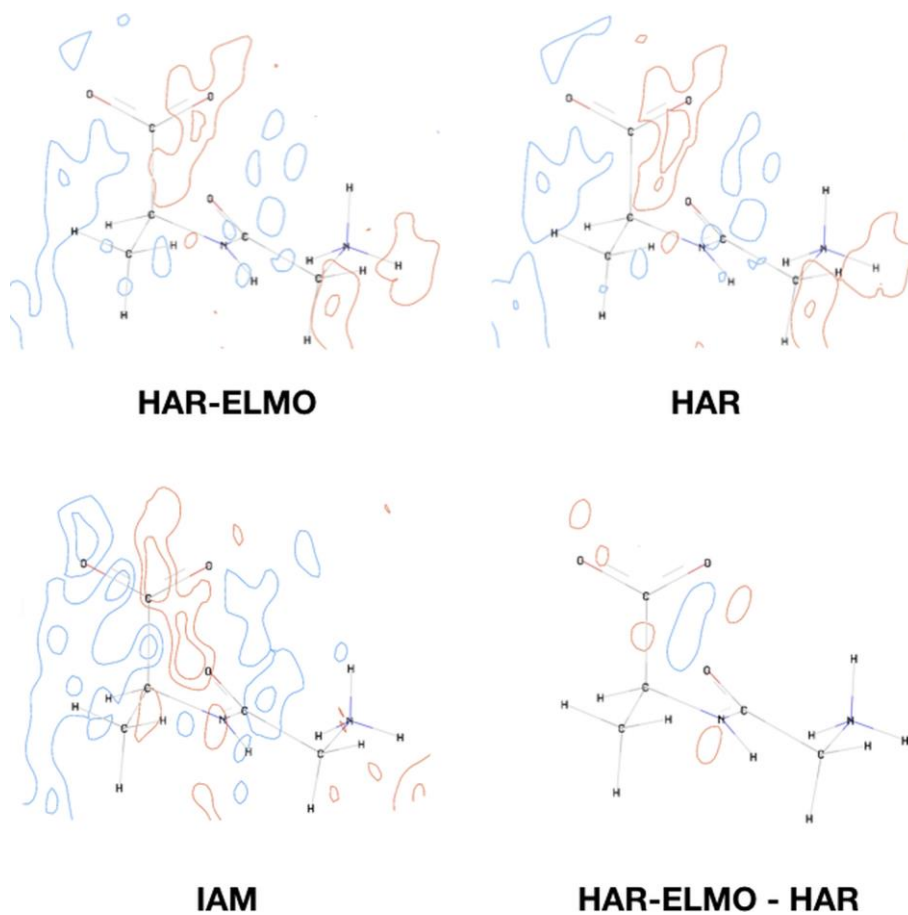
### Gly-*L*-Ala – Residual Densities (carboxylate group plane)



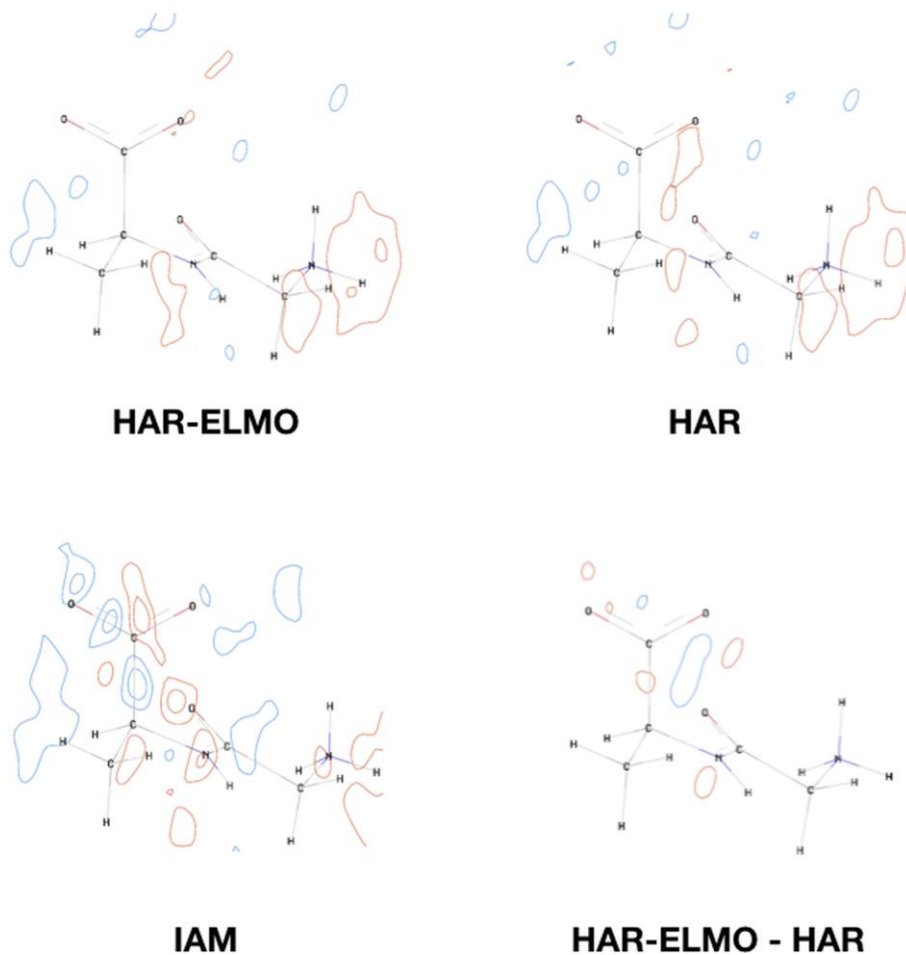
**Figure S38:** Residual density maps for Gly-*L*-Ala in the plane of the carboxylic group for the HAR-ELMO, HAR and IAM refinements at 12 K. The difference between the HAR-ELMO and HAR residual density maps is also shown. Contour levels: 0.05 and 0.10 eÅ<sup>-3</sup> for the HAR-ELMO, HAR and IAM maps and 0.02 eÅ<sup>-3</sup> for the HAR-ELMO – HAR difference map. Colours in the residual density maps: blue (positive) and red (negative).



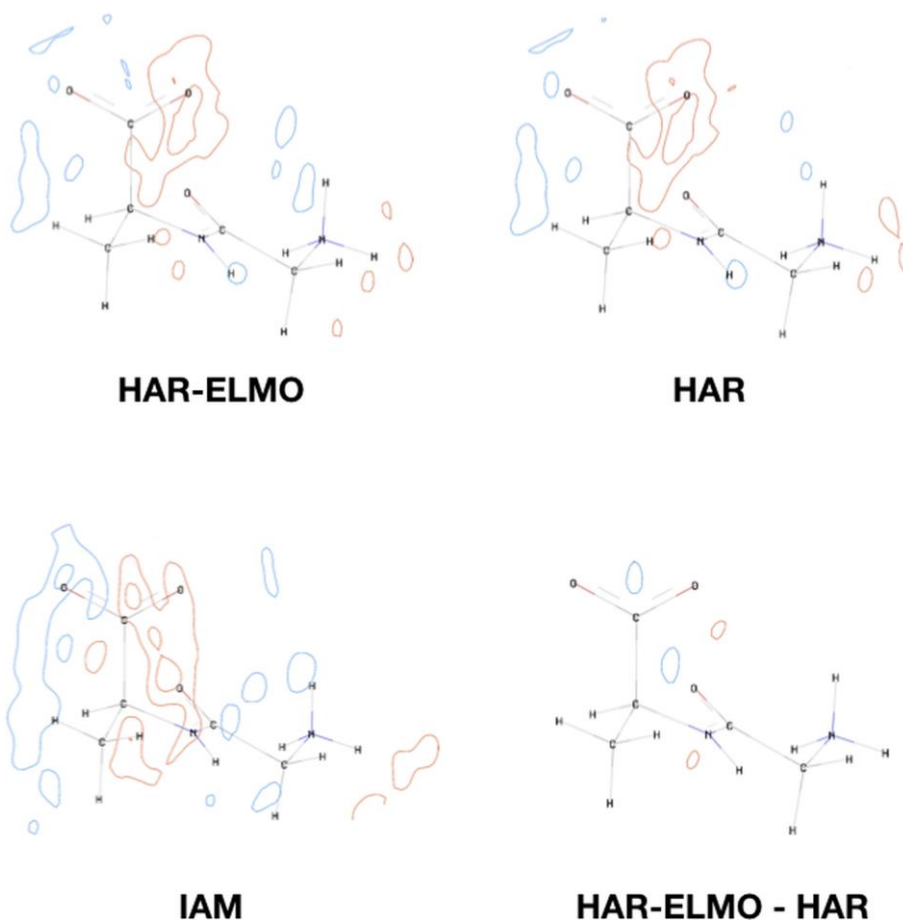
**Figure S39:** Residual density maps for Gly-*L*-Ala in the plane of the carboxylic group for the HAR-ELMO, HAR and IAM refinements at 50 K. The difference between the HAR-ELMO and HAR residual density maps is also shown. Contour levels: 0.05 and 0.10 eÅ<sup>-3</sup> for the HAR-ELMO, HAR and IAM maps and 0.025 eÅ<sup>-3</sup> for the HAR-ELMO – HAR difference map. Colours in the residual density maps: blue (positive) and red (negative).



**Figure S40:** Residual density maps for Gly-*L*-Ala in the plane of the carboxylic group for the HAR-ELMO, HAR and IAM refinements at 100 K. The difference between the HAR-ELMO and HAR residual density maps is also shown. Contour levels: 0.05 and 0.10 eÅ<sup>-3</sup> for the HAR-ELMO, HAR and IAM maps and 0.02 eÅ<sup>-3</sup> for the HAR-ELMO – HAR difference map. Colours in the residual density maps: blue (positive) and red (negative).

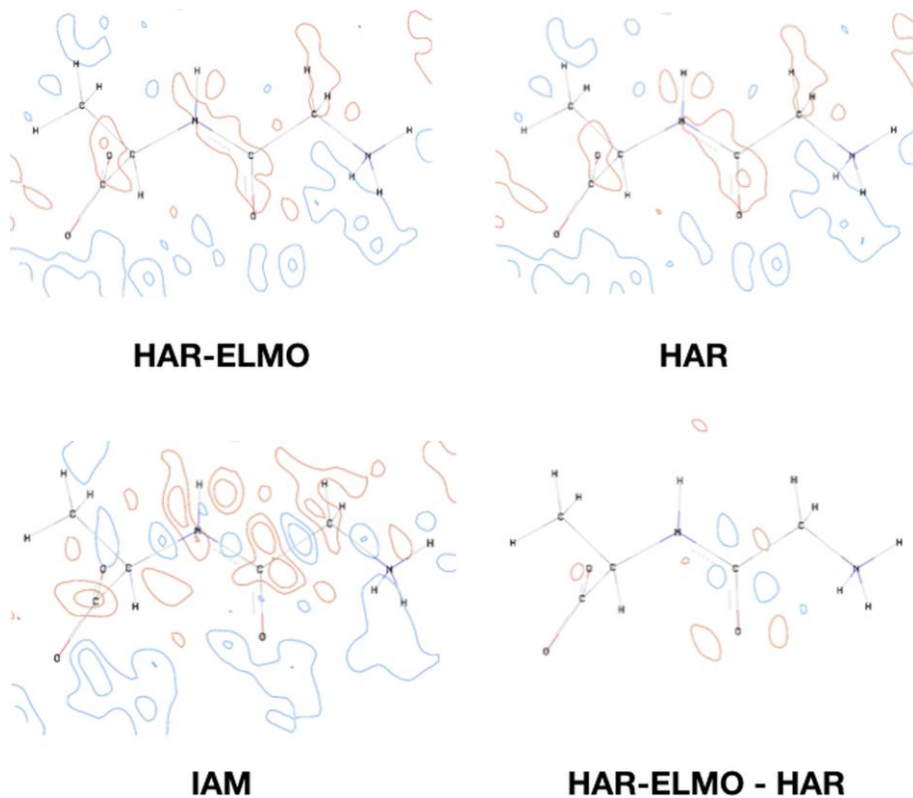


**Figure S41:** Residual density maps for Gly-*L*-Ala in the plane of the carboxylic group for the HAR-ELMO, HAR and IAM refinements at 150 K. The difference between the HAR-ELMO and HAR residual density maps is also shown. Contour levels: 0.05 and 0.10 eÅ<sup>-3</sup> for the HAR-ELMO, HAR and IAM maps and 0.02 eÅ<sup>-3</sup> for the HAR-ELMO – HAR difference map. Colours in the residual density maps: blue (positive) and red (negative).

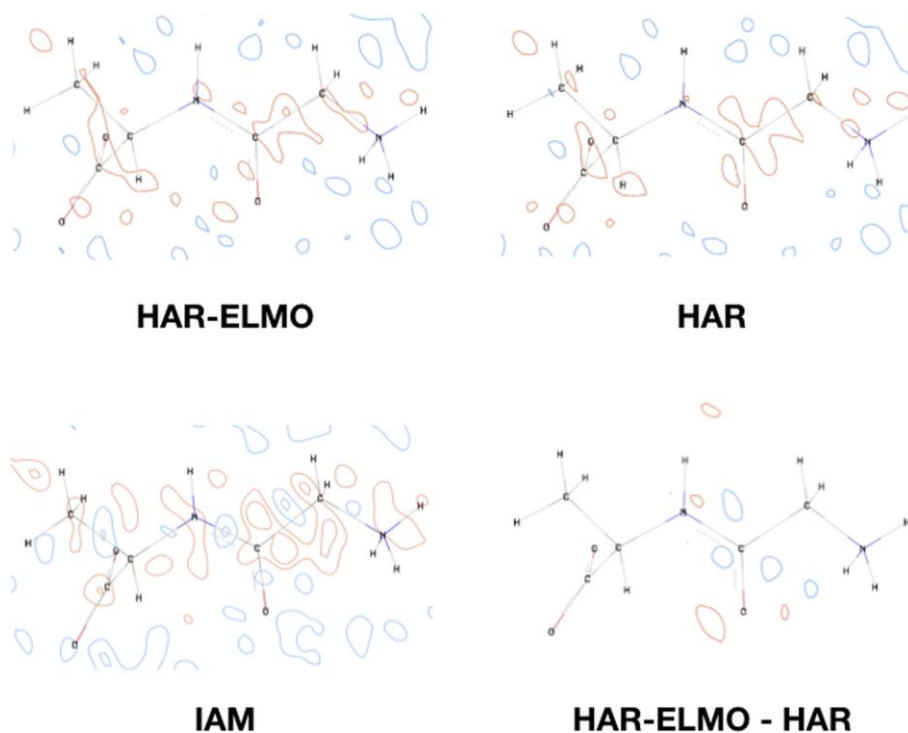


**Figure S42:** Residual density maps for Gly-*L*-Ala in the plane of the carboxylic group for the HAR-ELMO, HAR and IAM refinements at 295 K. The difference between the HAR-ELMO and HAR residual density maps is also shown. Contour levels: 0.05 and 0.10 eÅ<sup>-3</sup> for the HAR-ELMO, HAR and IAM maps and 0.02 eÅ<sup>-3</sup> for the HAR-ELMO – HAR difference map. Colours in the residual density maps: blue (positive) and red (negative).

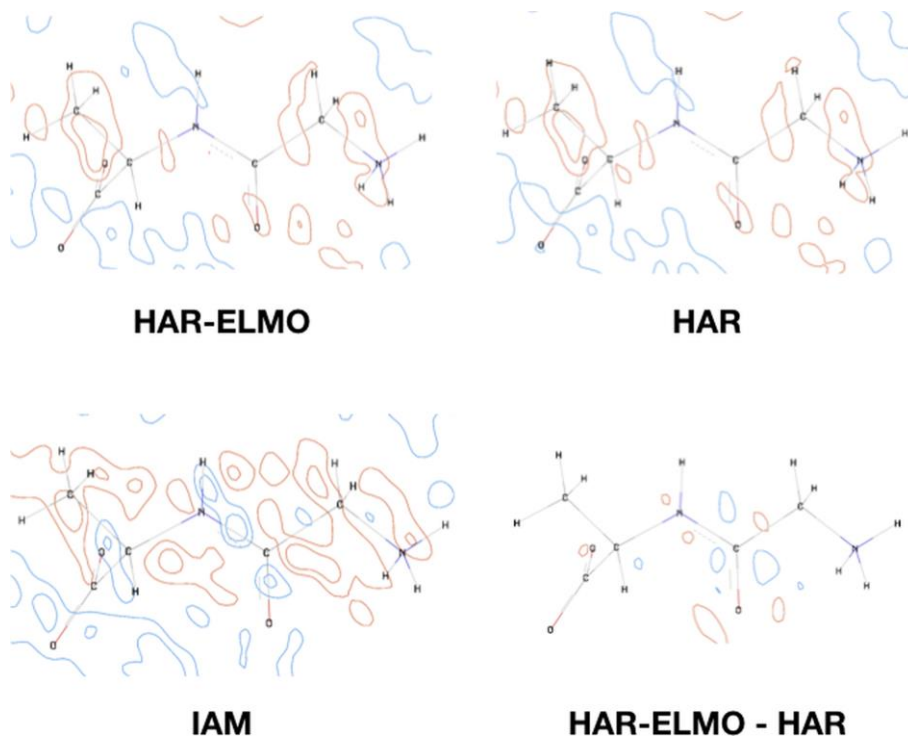
## Gly-*L*-Ala – Residual Densities (peptide bond plane)



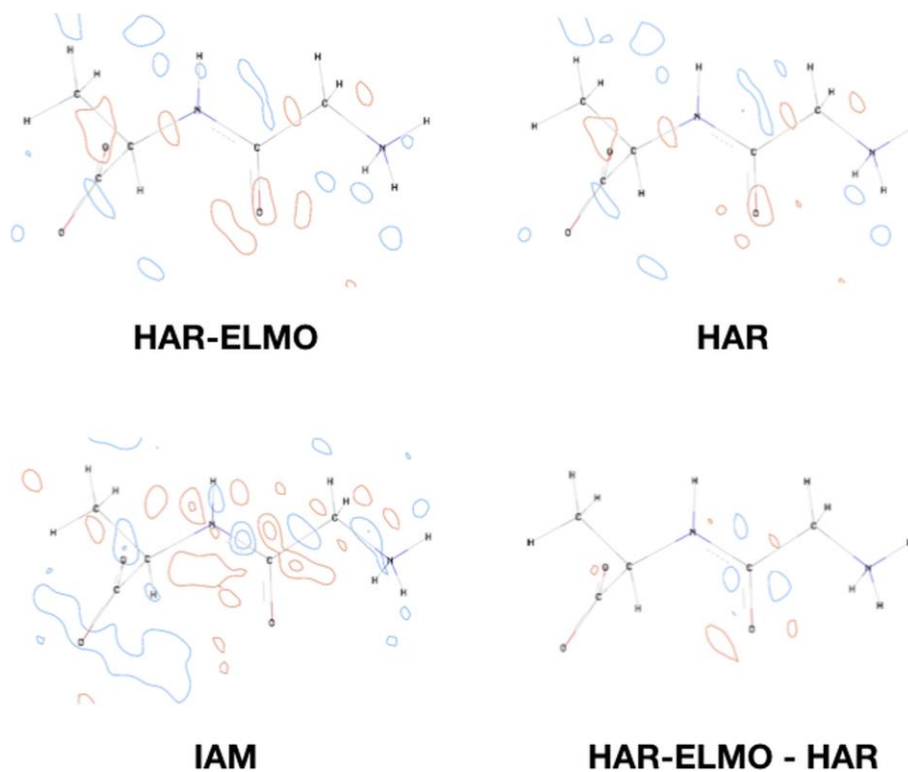
**Figure S43:** Residual density maps for Gly-*L*-Ala in the plane of the peptide bond for the HAR-ELMO, HAR and IAM refinements at 12 K. The difference between the HAR-ELMO and HAR residual density maps is also shown. Contour levels: 0.05 and 0.10 eÅ<sup>-3</sup> for the HAR-ELMO, HAR and IAM maps and 0.02 eÅ<sup>-3</sup> for the HAR-ELMO – HAR difference map. Colours in the residual density maps: blue (positive) and red (negative).



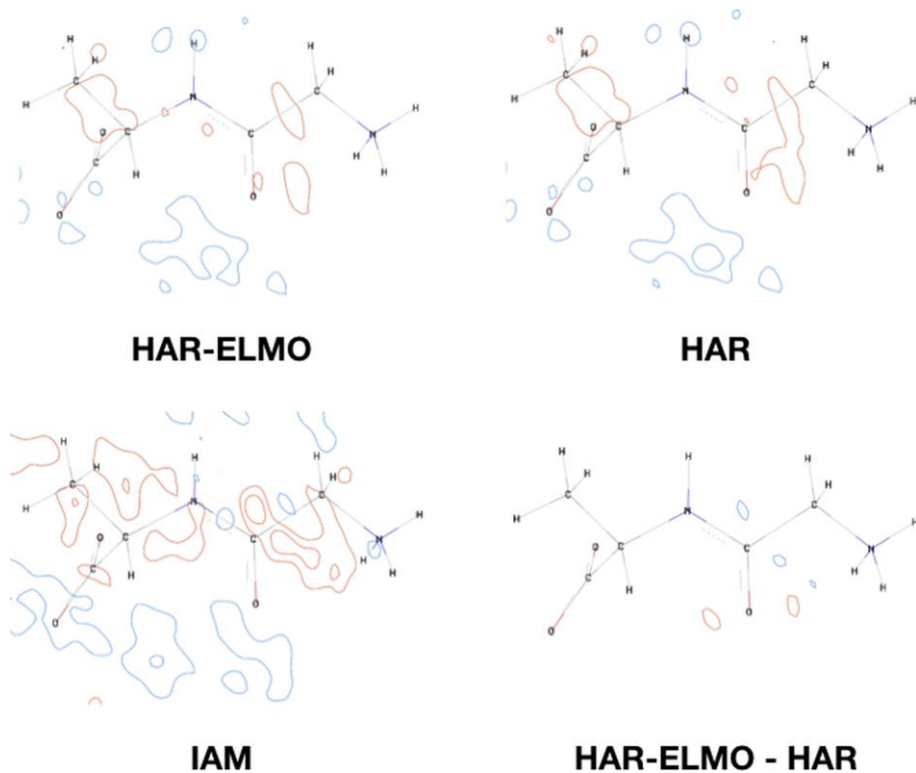
**Figure S44:** Residual density maps for Gly-*L*-Ala in the plane of the peptide bond for the HAR-ELMO, HAR and IAM refinements at 50 K. The difference between the HAR-ELMO and HAR residual density maps is also shown. Contour levels: 0.05 and 0.10 eÅ<sup>-3</sup> for the HAR-ELMO, HAR and IAM maps and 0.025 eÅ<sup>-3</sup> for the HAR-ELMO – HAR difference map. Colours in the residual density maps: blue (positive) and red (negative).



**Figure S45:** Residual density maps for Gly-*L*-Ala in the plane of the peptide bond for the HAR-ELMO, HAR and IAM refinements at 100 K. The difference between the HAR-ELMO and HAR residual density maps is also shown. Contour levels: 0.05 and 0.10 eÅ<sup>-3</sup> for the HAR-ELMO, HAR and IAM maps and 0.02 eÅ<sup>-3</sup> for the HAR-ELMO – HAR difference map. Colours in the residual density maps: blue (positive) and red (negative).

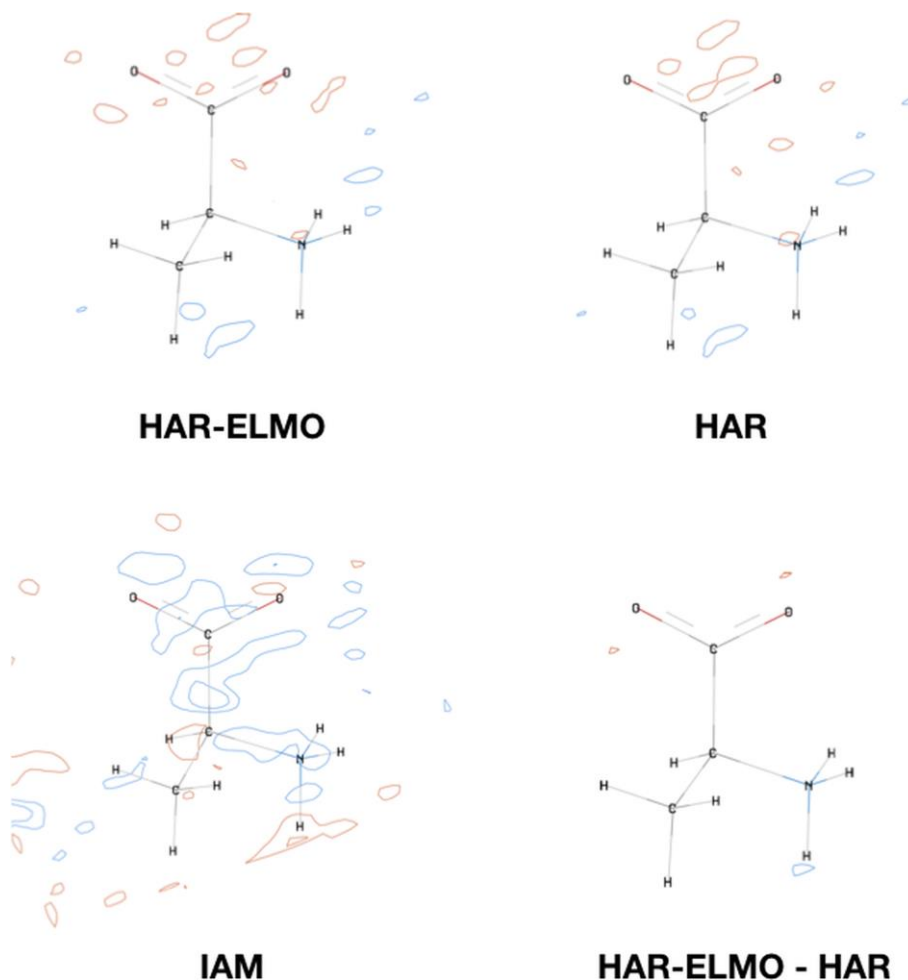


**Figure S46:** Residual density maps for Gly-*L*-Ala in the plane of the peptide bond for the HAR-ELMO, HAR and IAM refinements at 150 K. The difference between the HAR-ELMO and HAR residual density maps is also shown. Contour levels: 0.05 and 0.10 eÅ<sup>-3</sup> for the HAR-ELMO, HAR and IAM maps and 0.02 eÅ<sup>-3</sup> for the HAR-ELMO – HAR difference map. Colours in the residual density maps: blue (positive) and red (negative).

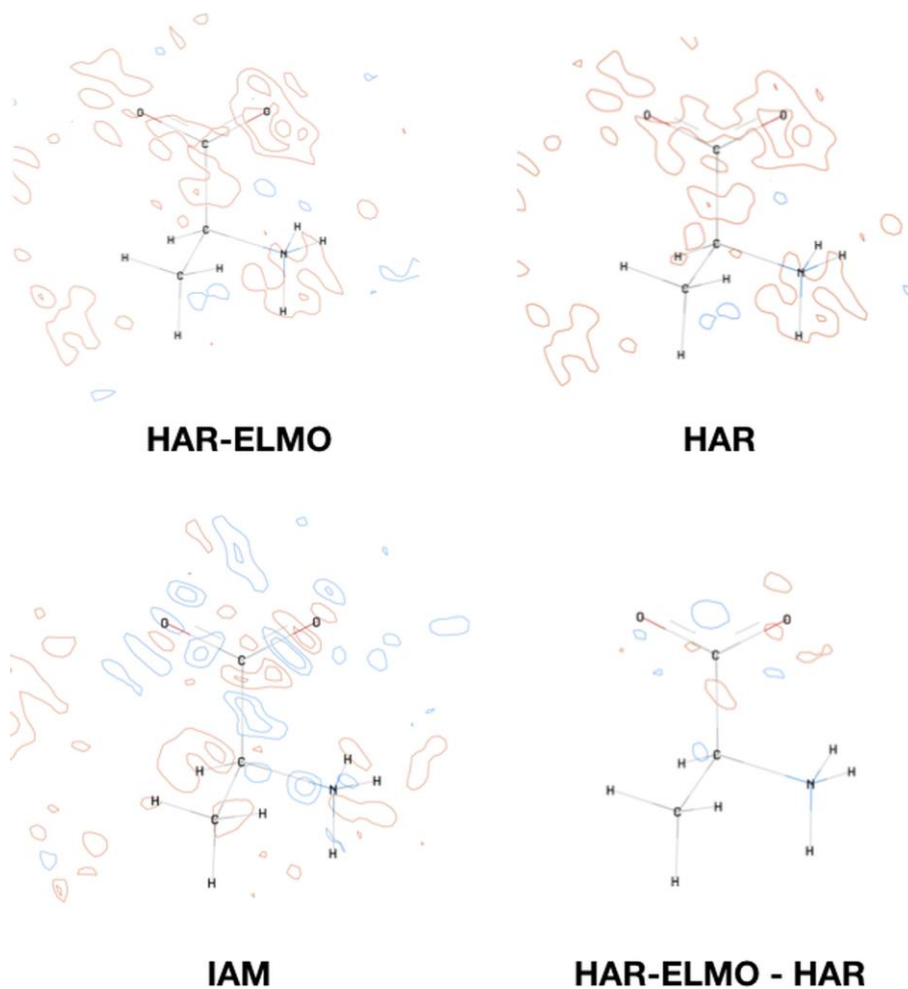


**Figure S47:** Residual density maps for Gly-*L*-Ala in the plane of the peptide bond for the HAR-ELMO, HAR and IAM refinements at 295 K. The difference between the HAR-ELMO and HAR residual density maps is also shown. Contour levels: 0.05 and 0.10 eÅ<sup>-3</sup> for the HAR-ELMO, HAR and IAM maps and 0.02 eÅ<sup>-3</sup> for the HAR-ELMO – HAR difference map. Colours in the residual density maps: blue (positive) and red (negative).

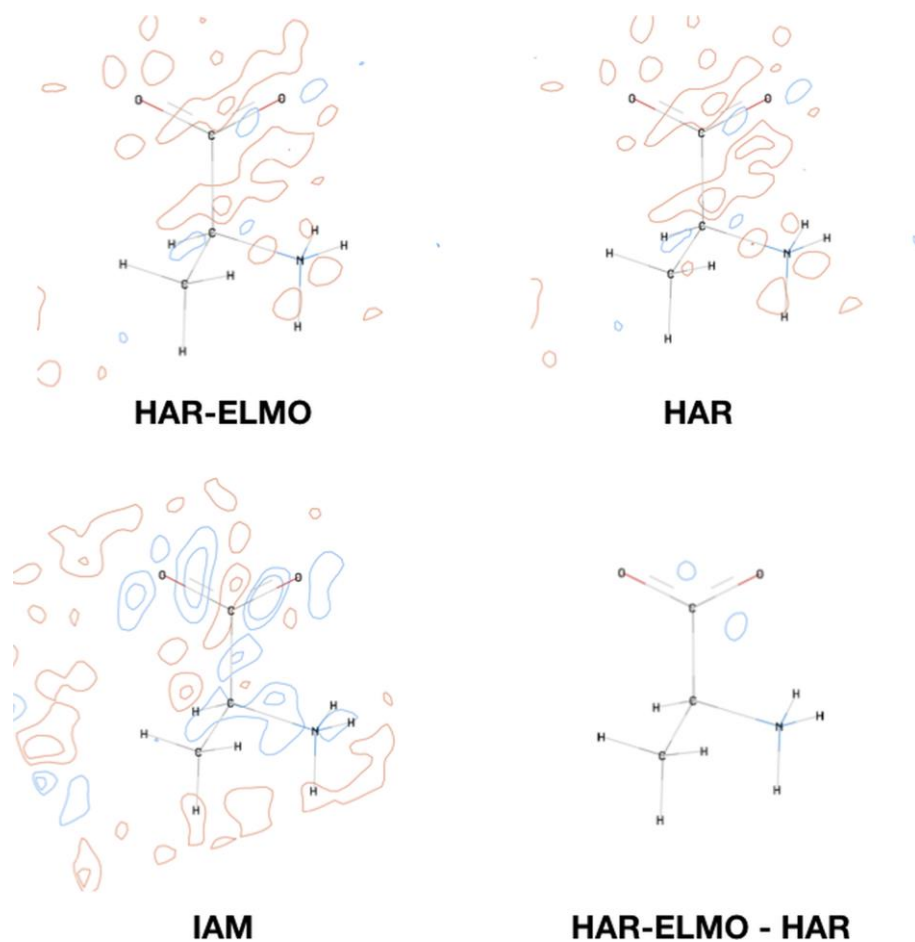
## *L*-alanine – Residual Densities (carboxylate group plane)



**Figure S48:** Residual density maps for *L*-Ala in the plane of the carboxylic group for the HAR-ELMO, HAR and IAM refinements at 23 K. The difference between the HAR-ELMO and HAR residual density maps is also shown. Contour levels: 0.05 and 0.10 eÅ<sup>-3</sup> for the HAR-ELMO, HAR and IAM maps and 0.025 eÅ<sup>-3</sup> for the HAR-ELMO – HAR difference map. Colours in the residual density maps: blue (positive) and red (negative).

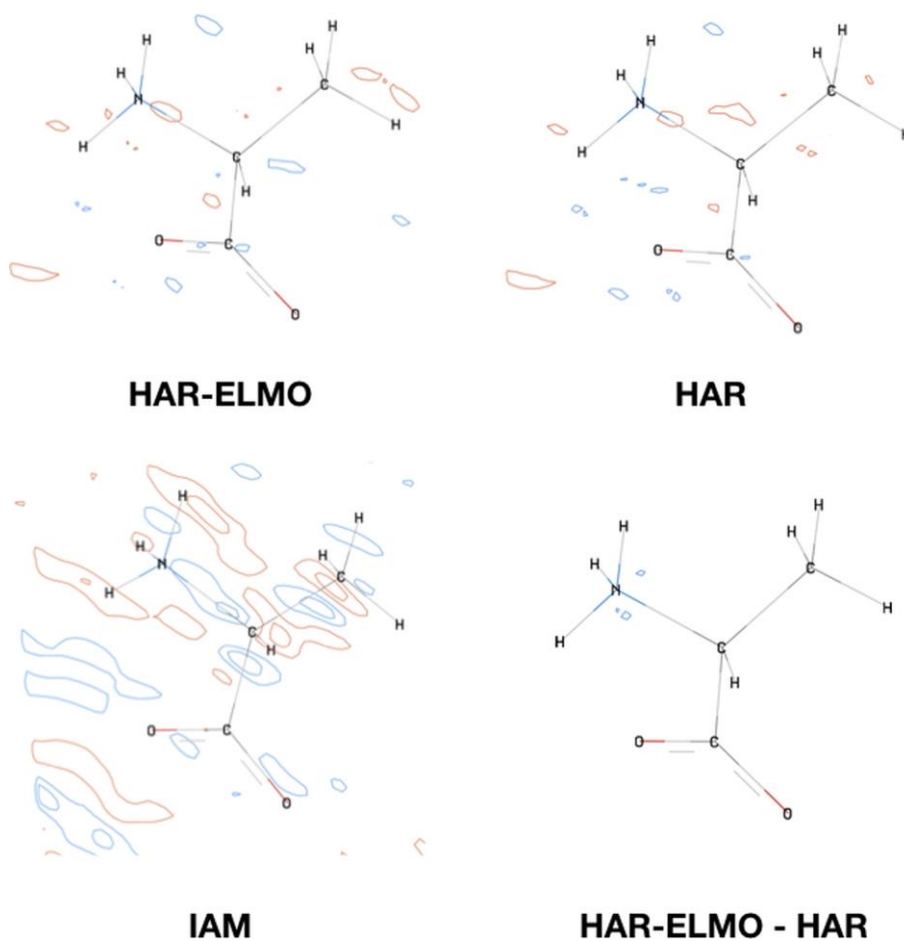


**Figure S49:** Residual density maps for *L*-Ala in the plane of the carboxylic group for the HAR-ELMO, HAR and IAM refinements at 100 K. The difference between the HAR-ELMO and HAR residual density maps is also shown. Contour levels: 0.05 and 0.10 eÅ<sup>-3</sup> for the HAR-ELMO, HAR and IAM maps and 0.025 eÅ<sup>-3</sup> for the HAR-ELMO – HAR difference map. Colours in the residual density maps: blue (positive) and red (negative).

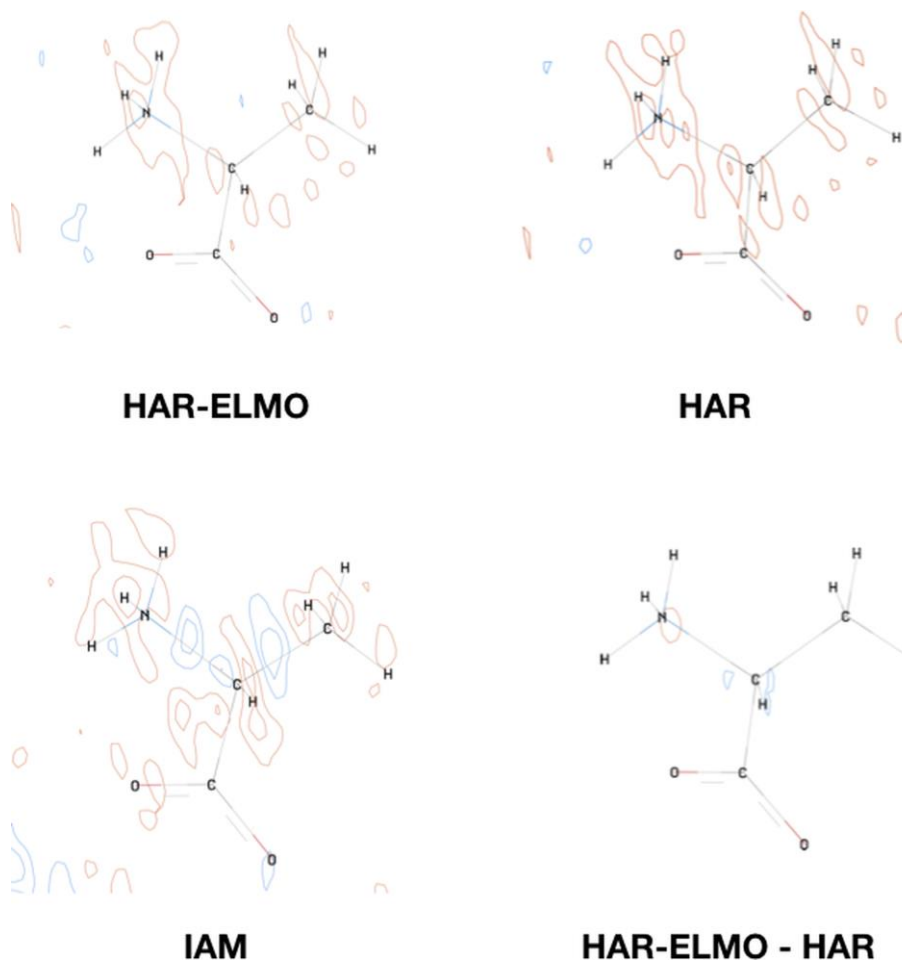


**Figure S50:** Residual density maps for *L*-Ala in the plane of the carboxylic group for the HAR-ELMO, HAR and IAM refinements at 150 K. The difference between the HAR-ELMO and HAR residual density maps is also shown. Contour levels: 0.05 and 0.10 eÅ<sup>-3</sup> for the HAR-ELMO, HAR and IAM maps and 0.025 eÅ<sup>-3</sup> for the HAR-ELMO – HAR difference map. Colours in the residual density maps: blue (positive) and red (negative).

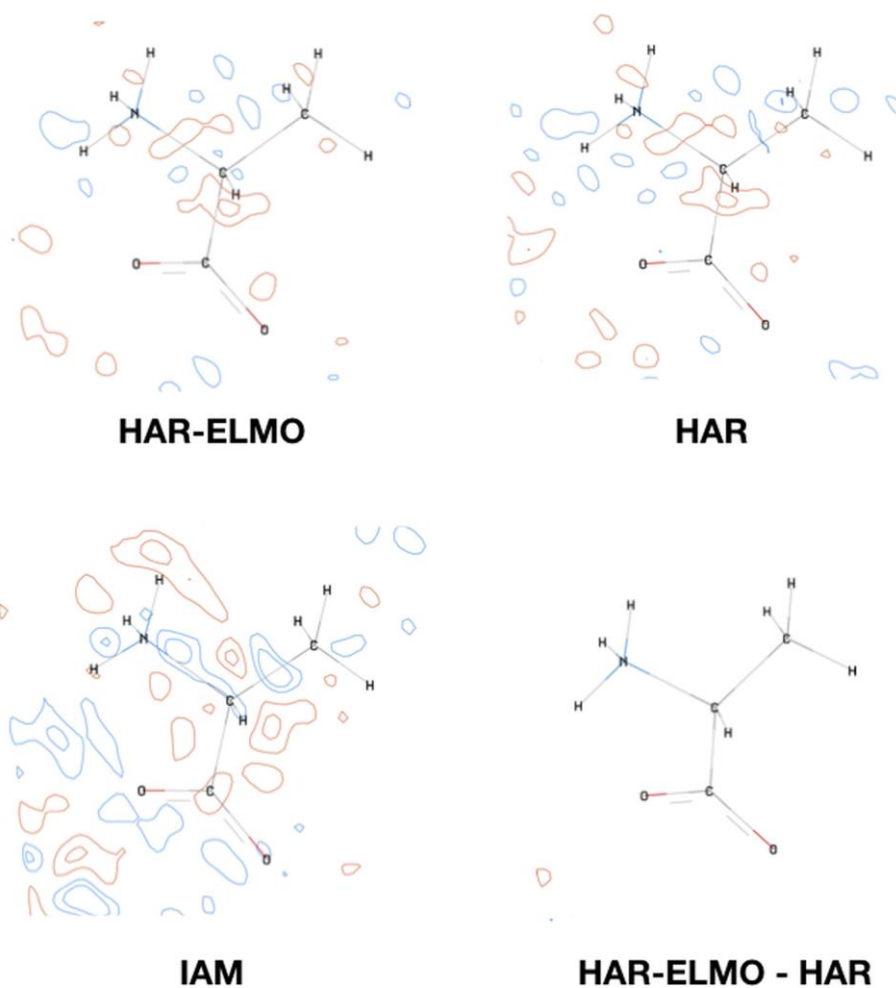
### *L*-alanine – Residual Densities (NCC plane)



**Figure S51:** Residual density maps for *L*-Ala in the N-C $\alpha$ -C $\beta$  plane for the HAR-ELMO, HAR and IAM refinements at 23 K. The difference between the HAR-ELMO and HAR residual density maps is also shown. Contour levels: 0.05 and 0.10 e $\text{\AA}^{-3}$  for the HAR-ELMO, HAR and IAM maps and 0.025 e $\text{\AA}^{-3}$  for the HAR-ELMO – HAR difference map. Colours in the residual density maps: blue (positive) and red (negative).



**Figure S52:** Residual density maps for *L*-Ala in the N-C $\alpha$ -C $\beta$  plane for the HAR-ELMO, HAR and IAM refinements at 100 K. The difference between the HAR-ELMO and HAR residual density maps is also shown. Contour levels: 0.05 and 0.10 e $\text{\AA}^{-3}$  for the HAR-ELMO, HAR and IAM maps and 0.025 e $\text{\AA}^{-3}$  for the HAR-ELMO – HAR difference map. Colours in the residual density maps: blue (positive) and red (negative).

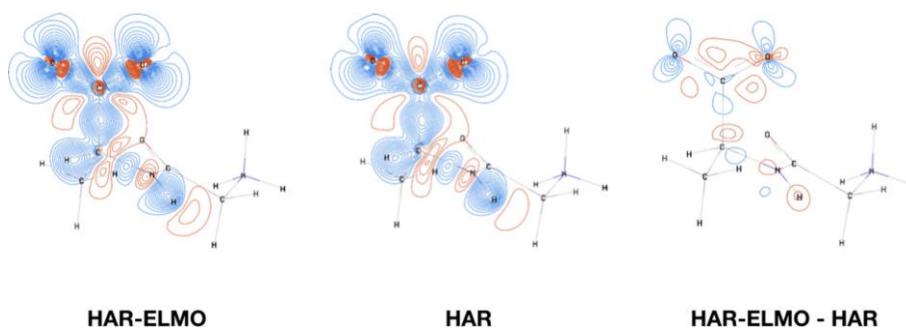


**Figure S53:** Residual density maps for *L*-Ala in the N-C $\alpha$ -C $\beta$  plane for the HAR-ELMO, HAR and IAM refinements at 150 K. The difference between the HAR-ELMO and HAR residual density maps is also shown. Contour levels: 0.05 and 0.10 e $\text{\AA}^{-3}$  for the HAR-ELMO, HAR and IAM maps and 0.025 e $\text{\AA}^{-3}$  for the HAR-ELMO – HAR difference map. Colours in the residual density maps: blue (positive) and red (negative).

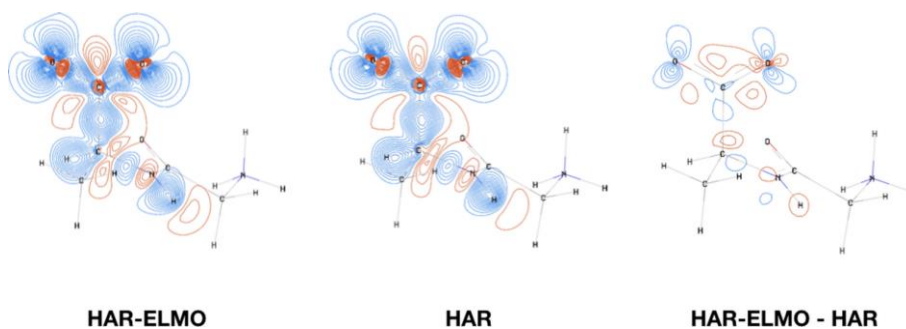
## Deformation Densities

The difference between HAR-ELMO and HAR deformation densities for all structures (compare Figure S54 to Figure S77) clearly accentuates some systematic features in the regions of oxygen lone pairs and of the most polarizable hydrogen atoms. This is most likely due to the strict localization applied in the construction of the ELMO wavefunction, in contrast to maximal electron delocalization of the wavefunction used in the traditional HAR procedure. This will impact on the description of intermolecular interactions and, hence, it is the reason for the differences in the ADPs of the peptide hydrogen atom in Gly-*L*-Ala (compare Figure S5). We will discuss impacts and mitigations of this phenomenon in a separate study.

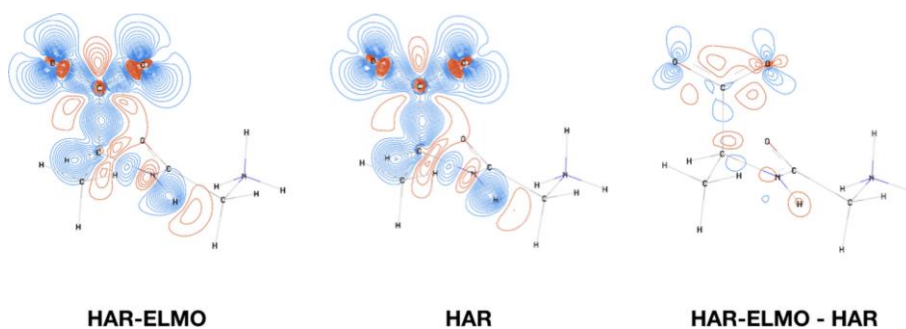
## Gly-*L*-Ala – Deformation Densities (carboxylate group plane)



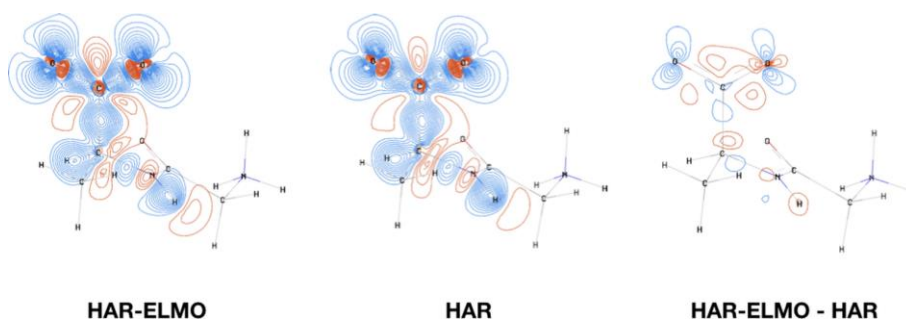
**Figure S54:** Deformation density maps for Gly-*L*-Ala in the plane of the carboxylic group for the HAR-ELMO and HAR refinements at 12 K. The difference between the HAR-ELMO and HAR deformation density maps is also shown. Contour levels: from 0.05 to 1.00 eÅ<sup>-3</sup> with a step of 0.05 eÅ<sup>-3</sup>. Colours in the deformation density maps: blue (positive) and red (negative).



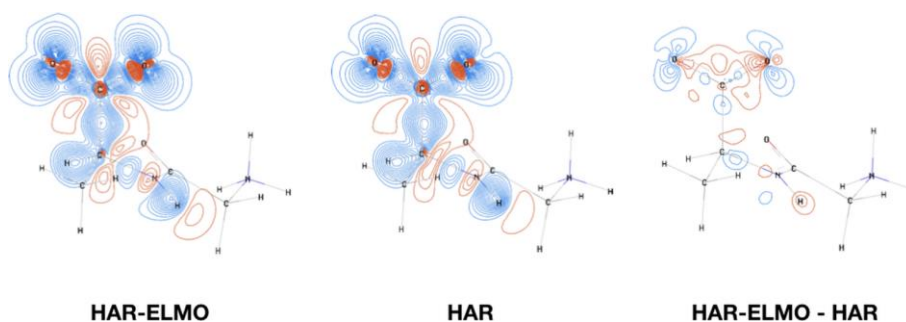
**Figure S55:** Deformation density maps for Gly-*L*-Ala in the plane of the carboxylic group for the HAR-ELMO and HAR refinements at 50 K. The difference between the HAR-ELMO and HAR deformation density maps is also shown. Contour levels: from 0.05 to 1.00 eÅ<sup>-3</sup> with a step of 0.05 eÅ<sup>-3</sup>. Colours in the deformation density maps: blue (positive) and red (negative).



**Figure S56:** Deformation density maps for Gly-*L*-Ala in the plane of the carboxylic group for the HAR-ELMO and HAR refinements at 100 K. The difference between the HAR-ELMO and HAR deformation density maps is also shown. Contour levels: from 0.05 to 1.00 eÅ<sup>-3</sup> with a step of 0.05 eÅ<sup>-3</sup>. Colours in the deformation density maps: blue (positive) and red (negative).

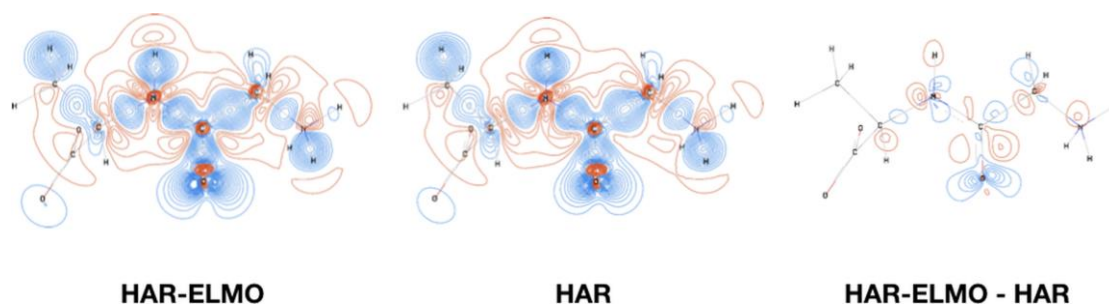


**Figure S57:** Deformation density maps for Gly-*L*-Ala in the plane of the carboxylic group for the HAR-ELMO and HAR refinements at 150 K. The difference between the HAR-ELMO and HAR deformation density maps is also shown. Contour levels: from 0.05 to 1.00 eÅ<sup>-3</sup> with a step of 0.05 eÅ<sup>-3</sup>. Colours in the deformation density maps: blue (positive) and red (negative).

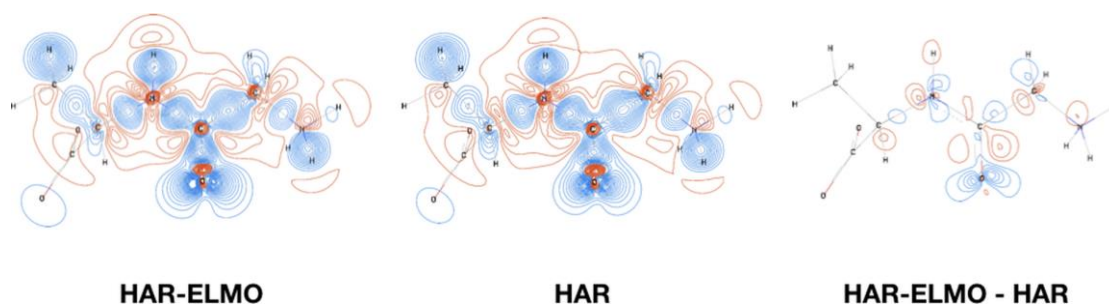


**Figure S58:** Deformation density maps for Gly-*L*-Ala in the plane of the carboxylic group for the HAR-ELMO and HAR refinements at 295 K. The difference between the HAR-ELMO and HAR deformation density maps is also shown. Contour levels: from 0.05 to 1.00 eÅ<sup>-3</sup> with a step of 0.05 eÅ<sup>-3</sup>. Colours in the deformation density maps: blue (positive) and red (negative).

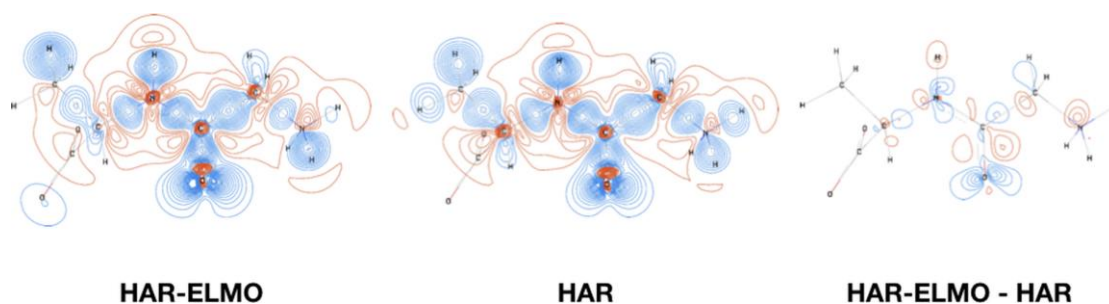
## Gly-*L*-Ala – Deformation Densities (peptide bond plane)



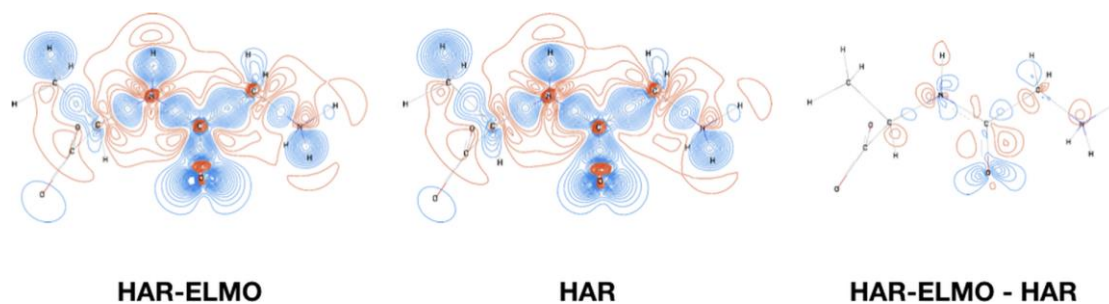
**Figure S59:** Deformation density maps for Gly-*L*-Ala in the plane of the peptide bond for the HAR-ELMO and HAR refinements at 12 K. The difference between the HAR-ELMO and HAR deformation density maps is also shown. Contour levels: from 0.05 to 1.00 eÅ<sup>-3</sup> with a step of 0.05 eÅ<sup>-3</sup>. Colours in the deformation density maps: blue (positive) and red (negative).



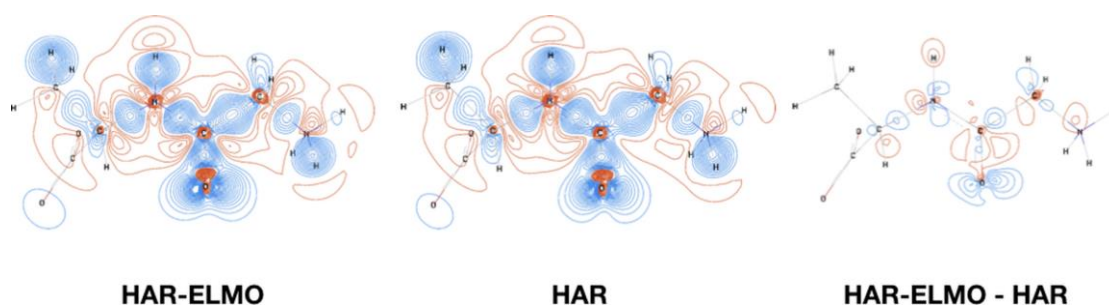
**Figure S60:** Deformation density maps for Gly-*L*-Ala in the plane of the peptide bond for the HAR-ELMO and HAR refinements at 50 K. The difference between the HAR-ELMO and HAR deformation density maps is also shown. Contour levels: from 0.05 to 1.00 eÅ<sup>-3</sup> with a step of 0.05 eÅ<sup>-3</sup>. Colours in the deformation density maps: blue (positive) and red (negative).



**Figure S61:** Deformation density maps for Gly-*L*-Ala in the plane of the peptide bond for the HAR-ELMO and HAR refinements at 100 K. The difference between the HAR-ELMO and HAR deformation density maps is also shown. Contour levels: from 0.05 to 1.00 eÅ<sup>-3</sup> with a step of 0.05 eÅ<sup>-3</sup>. Colours in the deformation density maps: blue (positive) and red (negative).

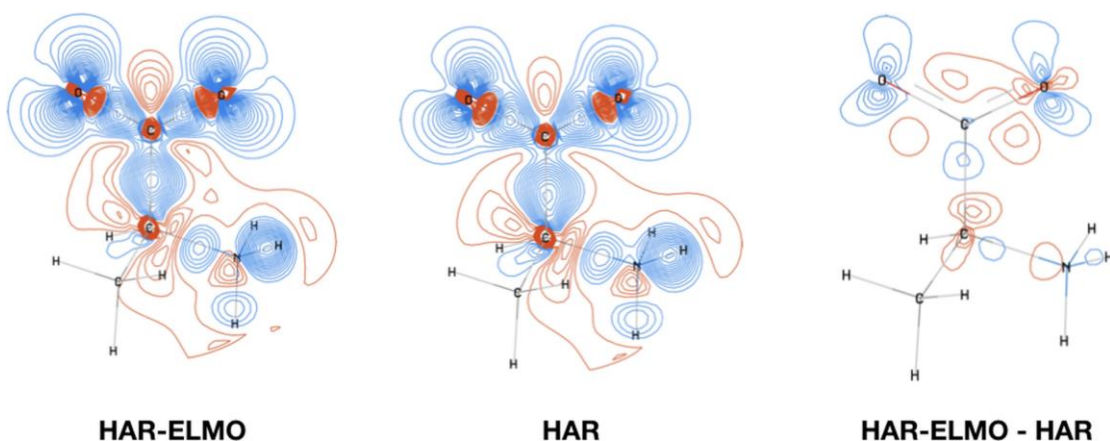


**Figure S62:** Deformation density maps for Gly-*L*-Ala in the plane of the peptide bond for the HAR-ELMO and HAR refinements at 150 K. The difference between the HAR-ELMO and HAR deformation density maps is also shown. Contour levels: from 0.05 to 1.00 eÅ<sup>-3</sup> with a step of 0.05 eÅ<sup>-3</sup>. Colours in the deformation density maps: blue (positive) and red (negative).

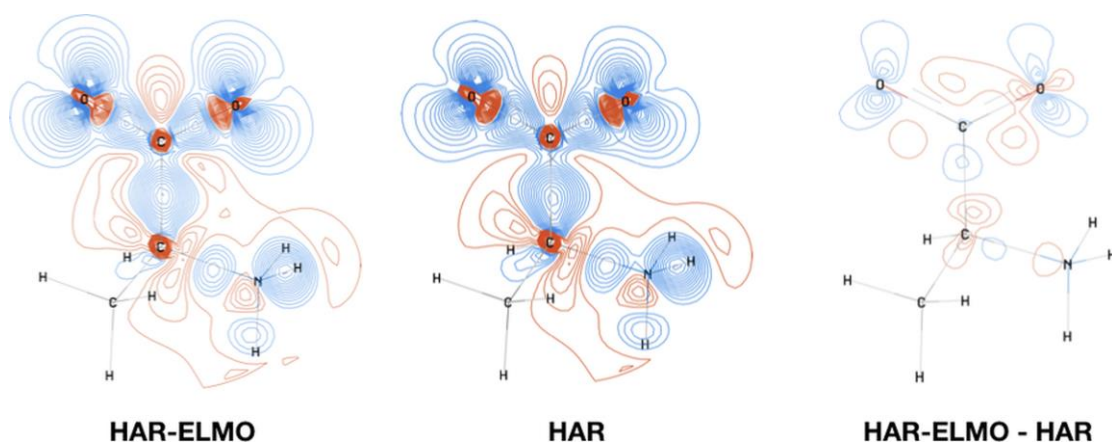


**Figure S63:** Deformation density maps for Gly-*L*-Ala in the plane of the peptide bond for the HAR-ELMO and HAR refinements at 295 K. The difference between the HAR-ELMO and HAR deformation density maps is also shown. Contour levels: from 0.05 to 1.00 eÅ<sup>-3</sup> with a step of 0.05 eÅ<sup>-3</sup>. Colours in the deformation density maps: blue (positive) and red (negative).

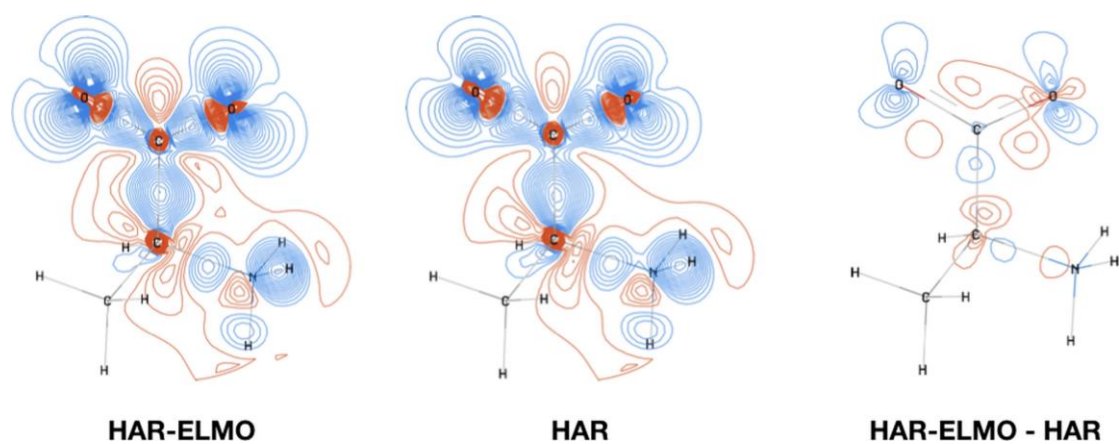
## *L*-alanine – Deformation Densities (carboxylate group plane)



**Figure S64:** Deformation density maps for *L*-Ala in the plane of the carboxylic group for the HAR-ELMO and HAR refinements at 23 K. The difference between the HAR-ELMO and HAR deformation density maps is also shown. Contour levels: from 0.05 to 1.00 eÅ<sup>-3</sup> with a step of 0.05 eÅ<sup>-3</sup>. Colours in the deformation density maps: blue (positive) and red (negative).

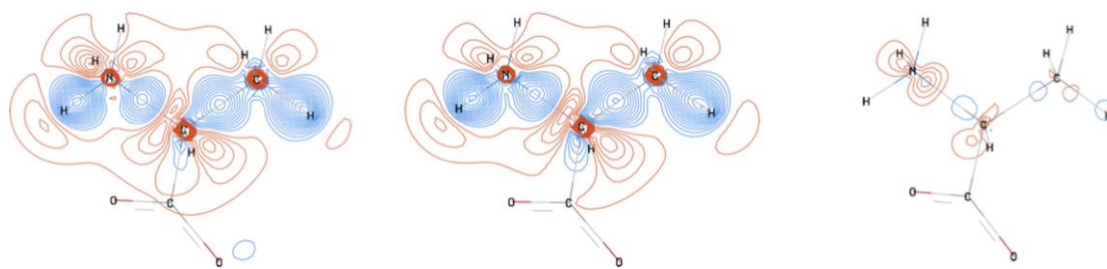


**Figure S65:** Deformation density maps for *L*-Ala in the plane of the carboxylic group for the HAR-ELMO and HAR refinements at 100 K. The difference between the HAR-ELMO and HAR deformation density maps is also shown. Contour levels: from 0.05 to 1.00 eÅ<sup>-3</sup> with a step of 0.05 eÅ<sup>-3</sup>. Colours in the deformation density maps: blue (positive) and red (negative).



**Figure S66:** Deformation density maps for *L*-Ala in the plane of the carboxylic group for the HAR-ELMO and HAR refinements at 150 K. The difference between the HAR-ELMO and HAR deformation density maps is also shown. Contour levels: from 0.05 to 1.00 eÅ<sup>-3</sup> with a step of 0.05 eÅ<sup>-3</sup>. Colours in the deformation density maps: blue (positive) and red (negative).

## *L*-alanine – Deformation Densities (NCC plane)

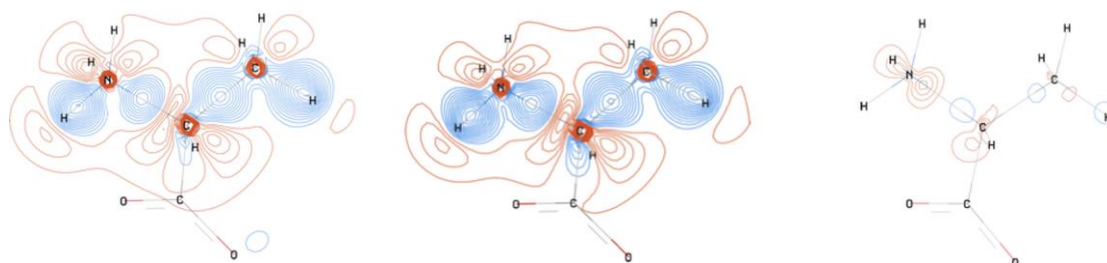


**HAR-ELMO**

**HAR**

**HAR-ELMO - HAR**

**Figure S67:** Deformation density maps for *L*-Ala in the N-C $\alpha$ -C $\beta$  plane for the HAR-ELMO and HAR refinements at 23 K. The difference between the HAR-ELMO and HAR deformation density maps is also shown. Contour levels: from 0.05 to 1.00 e $\text{\AA}^{-3}$  with a step of 0.05 e $\text{\AA}^{-3}$ . Colours in the deformation density maps: blue (positive) and red (negative).

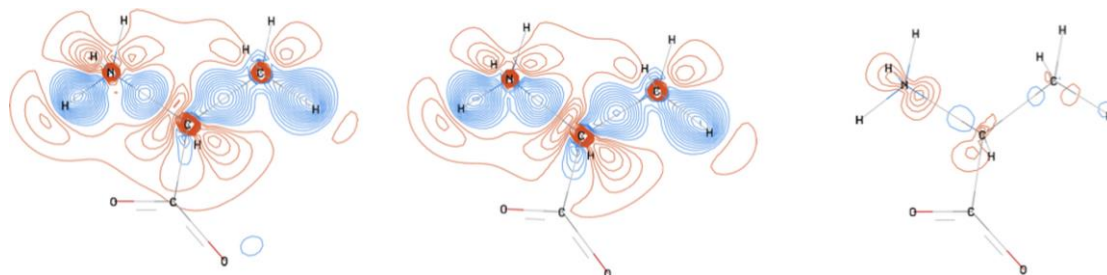


**HAR-ELMO**

**HAR**

**HAR-ELMO - HAR**

**Figure S68:** Deformation density maps for *L*-Ala in the N-C $\alpha$ -C $\beta$  plane for the HAR-ELMO and HAR refinements at 100 K. The difference between the HAR-ELMO and HAR deformation density maps is also shown. Contour levels: from 0.05 to 1.00 e $\text{\AA}^{-3}$  with a step of 0.05 e $\text{\AA}^{-3}$ . Colours in the deformation density maps: blue (positive) and red (negative).



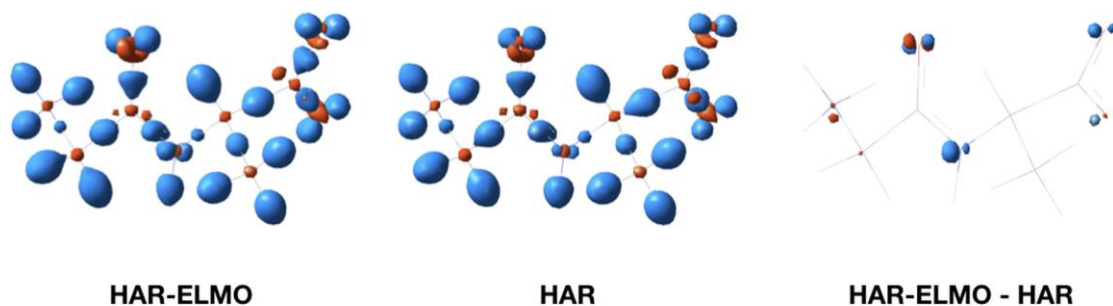
**HAR-ELMO**

**HAR**

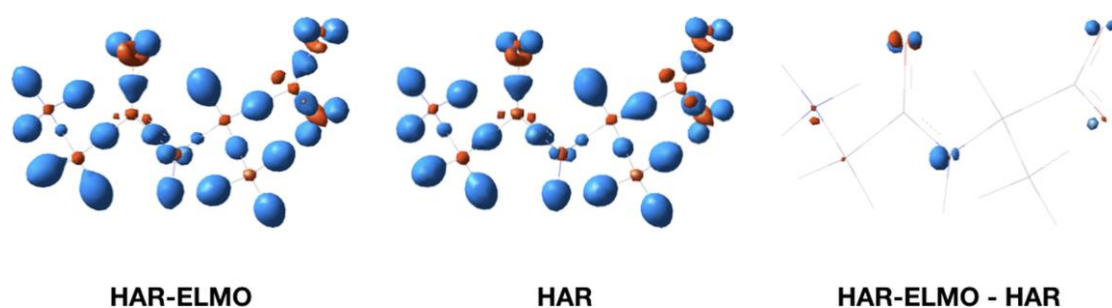
**HAR-ELMO - HAR**

**Figure S69:** Deformation density maps for *L*-Ala in the N-C $\alpha$ -C $\beta$  plane for the HAR-ELMO and HAR refinements at 150 K. The difference between the HAR-ELMO and HAR deformation density maps is also shown. Contour levels: from 0.05 to 1.00 e $\text{\AA}^{-3}$  with a step of 0.05 e $\text{\AA}^{-3}$ . Colours in the deformation density maps: blue (positive) and red (negative).

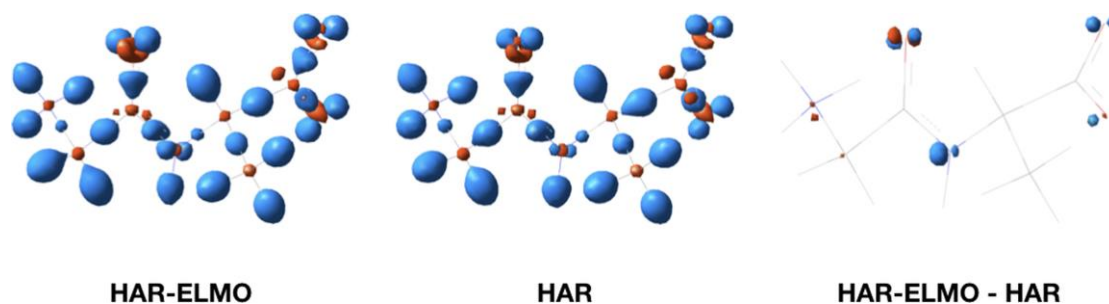
## Gly-*L*-Ala – 3D Deformation Densities



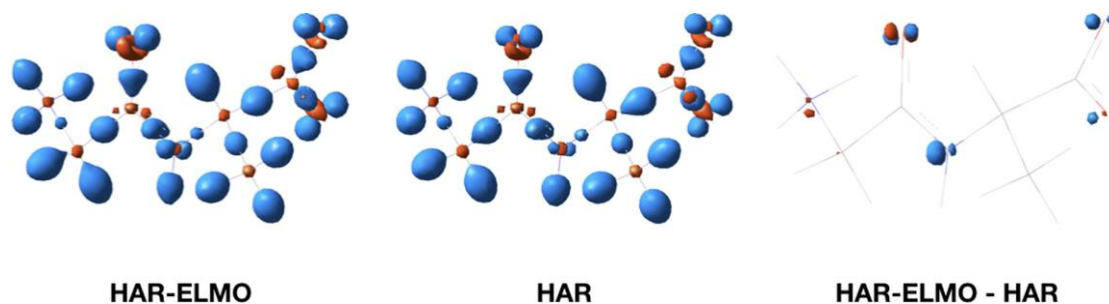
**Figure S70:** Deformation densities of Gly-*L*-Ala corresponding to the HAR-ELMO and HAR refinements at 12 K (isosurface level:  $0.4 \text{ e}\text{\AA}^{-3}$ ). The difference between the HAR-ELMO and HAR deformation densities is also shown (isosurface level:  $0.2 \text{ e}\text{\AA}^{-3}$ ). Colours in the deformation density plots: blue (positive) and red (negative).



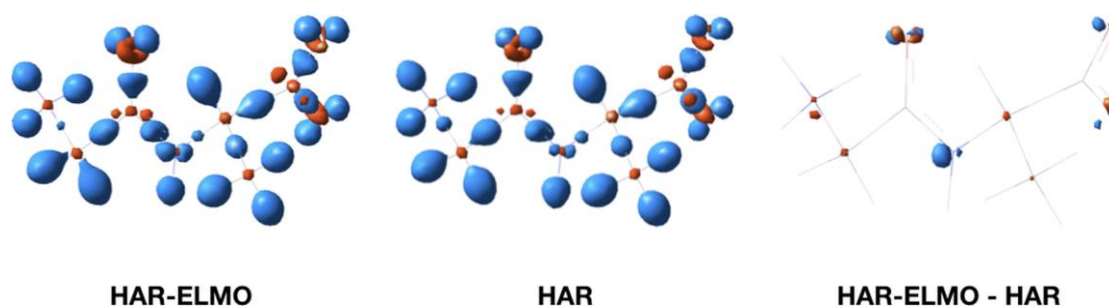
**Figure S71:** Deformation densities of Gly-*L*-Ala corresponding to the HAR-ELMO and HAR refinements at 50 K (isosurface level:  $0.4 \text{ e}\text{\AA}^{-3}$ ). The difference between the HAR-ELMO and HAR deformation densities is also shown (isosurface level:  $0.2 \text{ e}\text{\AA}^{-3}$ ). Colours in the deformation density plots: blue (positive) and red (negative).



**Figure S72:** Deformation densities of Gly-*L*-Ala corresponding to the HAR-ELMO and HAR refinements at 100 K (isosurface level:  $0.4 \text{ e}\text{\AA}^{-3}$ ). The difference between the HAR-ELMO and HAR deformation densities is also shown (isosurface level:  $0.2 \text{ e}\text{\AA}^{-3}$ ). Colours in the deformation density plots: blue (positive) and red (negative).

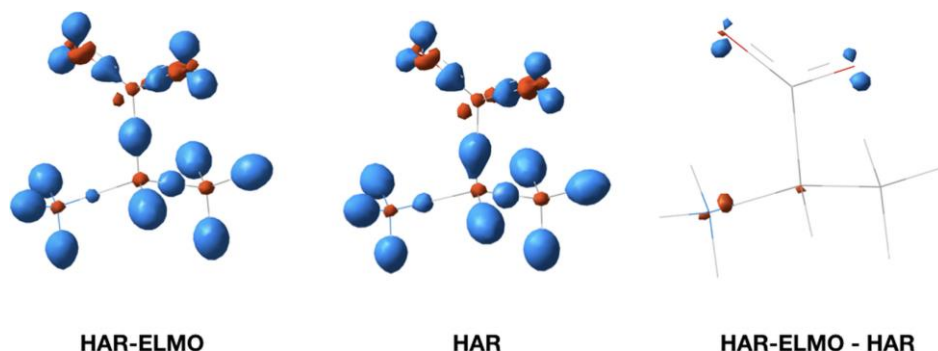


**Figure S73:** Deformation densities of Gly-*L*-Ala corresponding to the HAR-ELMO and HAR refinements at 150 K (isosurface level:  $0.4 \text{ e}\text{\AA}^{-3}$ ). The difference between the HAR-ELMO and HAR deformation densities is also shown (isosurface level:  $0.2 \text{ e}\text{\AA}^{-3}$ ). Colours in the deformation density plots: blue (positive) and red (negative).

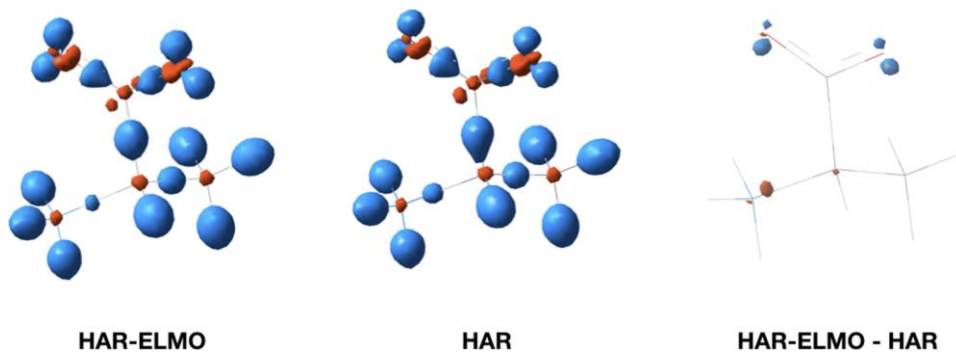


**Figure S74:** Deformation densities of Gly-*L*-Ala corresponding to the HAR-ELMO and HAR refinements at 295 K (isosurface level:  $0.4 \text{ e}\text{\AA}^{-3}$ ). The difference between the HAR-ELMO and HAR deformation densities is also shown (isosurface level:  $0.2 \text{ e}\text{\AA}^{-3}$ ). Colours in the deformation density plots: blue (positive) and red (negative).

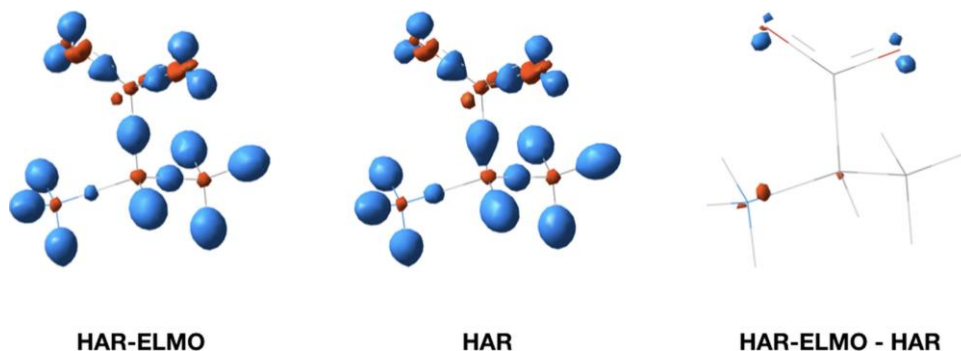
## *L*-alanine – 3D Deformation Densities



**Figure S75:** Deformation densities of *L*-Ala corresponding to the HAR-ELMO and HAR refinements at 23 K (isosurface level:  $0.4 \text{ e}\text{\AA}^{-3}$ ). The difference between the HAR-ELMO and HAR deformation densities is also shown (isosurface level:  $0.2 \text{ e}\text{\AA}^{-3}$ ). Colours in the deformation density plots: blue (positive) and red (negative).



**Figure S76:** Deformation densities of *L*-Ala corresponding to the HAR-ELMO and HAR refinements at 100 K (isosurface level:  $0.4 \text{ e}\text{\AA}^{-3}$ ). The difference between the HAR-ELMO and HAR deformation densities is also shown (isosurface level:  $0.2 \text{ e}\text{\AA}^{-3}$ ). Colours in the deformation density plots: blue (positive) and red (negative).



**Figure S77:** Deformation densities of *L*-Ala corresponding to the HAR-ELMO and HAR refinements at 150 K (isosurface level:  $0.4 \text{ e}\text{\AA}^{-3}$ ). The difference between the HAR-ELMO and HAR deformation densities is also shown (isosurface level:  $0.2 \text{ e}\text{\AA}^{-3}$ ). Colours in the deformation density plots: blue (positive) and red (negative).

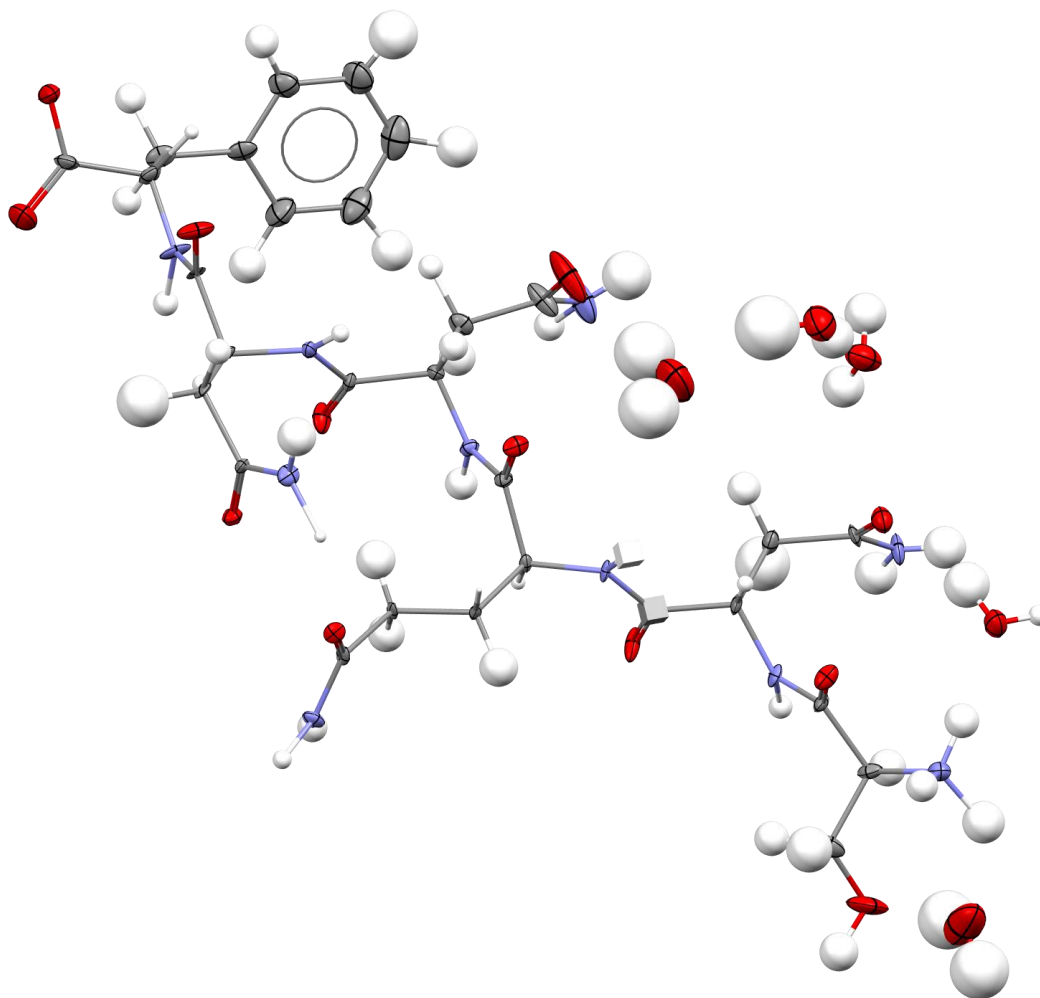
# Polypeptides and Protein Refinements

## Refinement details

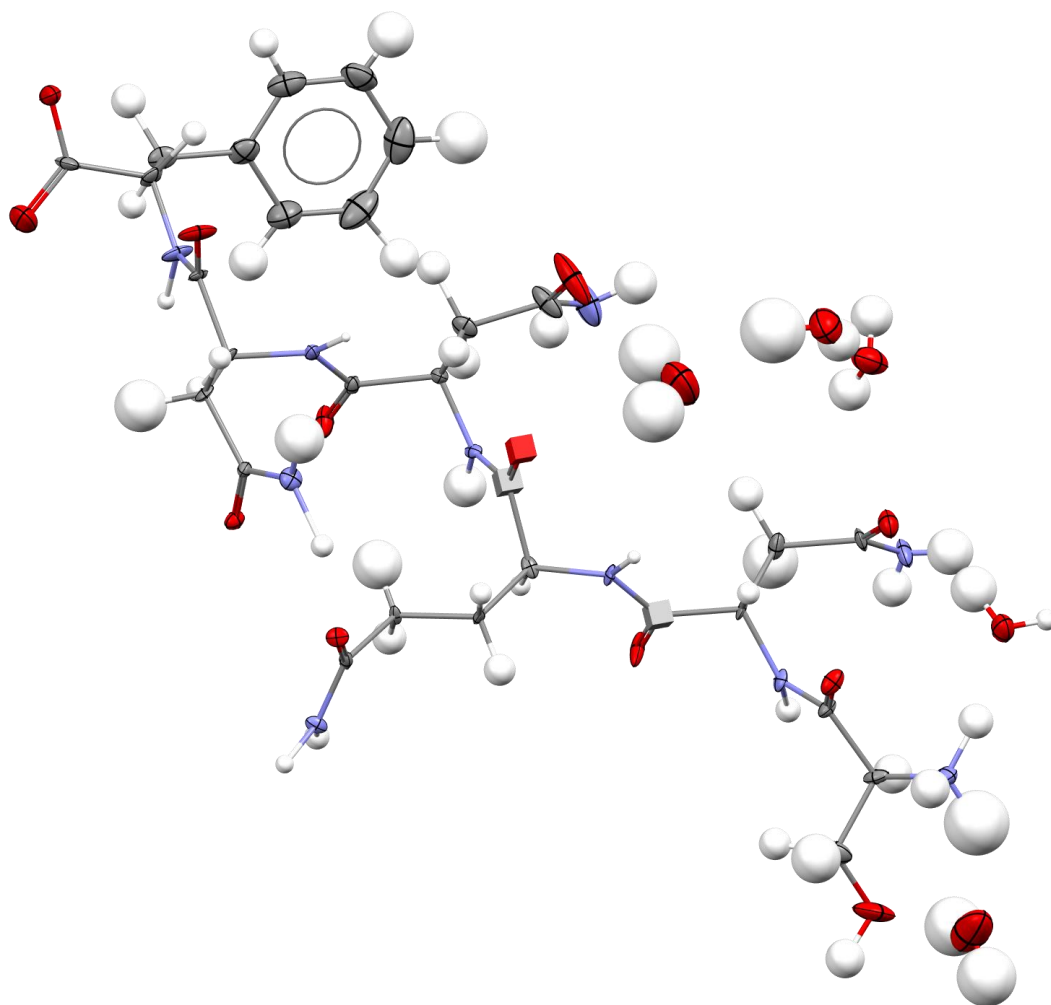
*Fibril-forming segment of the human prion protein (original PDB file: 2OL9)*<sup>S15</sup>

All the new refinements (IAM, HAR and HAR-ELMO) of the fibril-forming segment of the human prion protein were successfully completed including refinement of hydrogen atoms that were previously missing from the deposited structure. To accomplish this task, we treated all the hydrogen atoms isotropically except those belonging to the water molecules and hydrogen atom H1D, which were geometrically added through the *tleap* software associated with the AMBER Molecular Dynamics package<sup>S16</sup>. All the water molecules were kept fixed during the refinements.

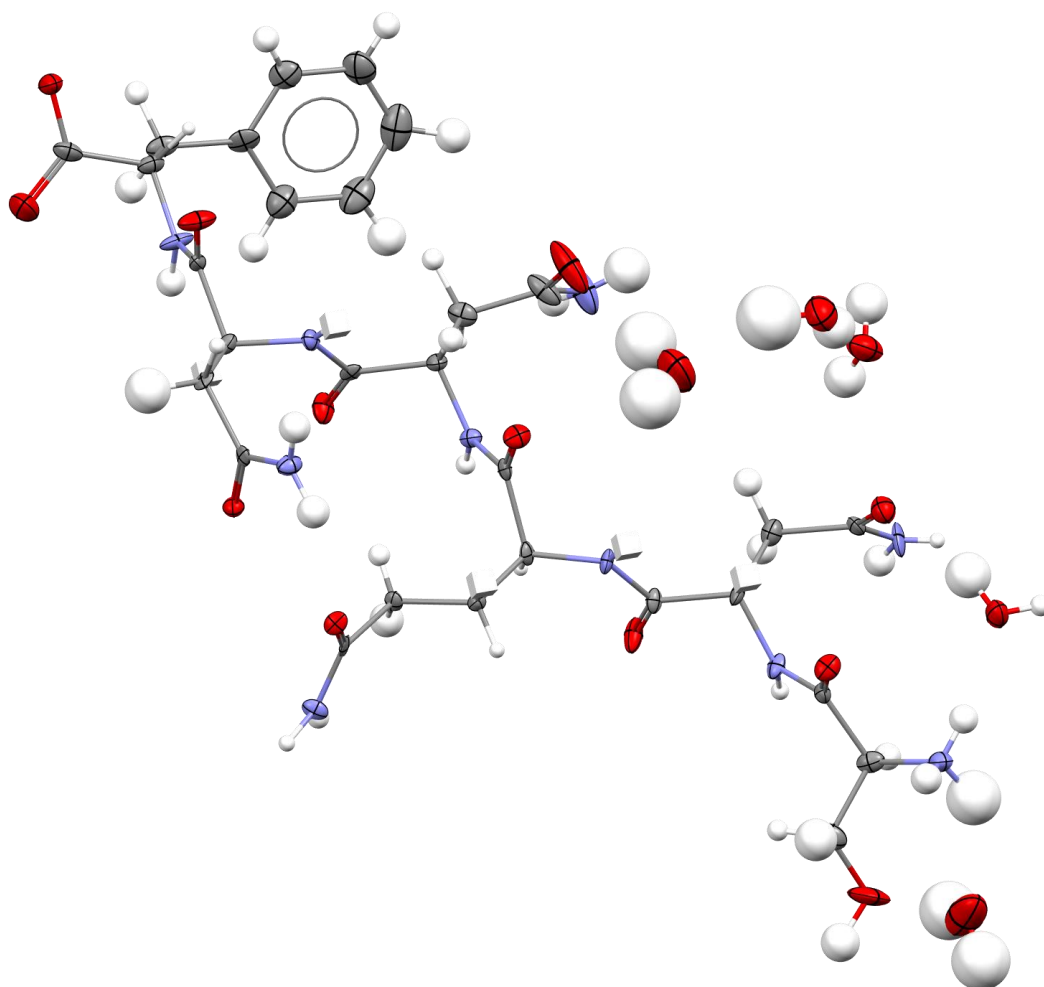
Some of the ADPs in all refinements (IAM, HAR and HAR-ELMO) are NPD, even for non-hydrogen atoms. Anyway, for HAR-ELMO, X-H bond distances are still reasonable (see main text). This shows that HAR-ELMO is feasible for low-quality data, and opens the method for evaluation of many already deposited polypeptide and protein structures in the future.



**Figure S78:** HAR molecular structure of the fibril-forming segment of the human prion protein with ADPs at 50% probability. NPD atoms depicted as boxes.



**Figure S79:** HAR-ELMO molecular structure of the fibril-forming segment of the human prion protein with ADPs at 50% probability. NPD atoms depicted as boxes.



**Figure S80:** IAM molecular structure of the fibril-forming segment of the human prion protein with ADPs at 50% probability. NPD atoms depicted as boxes.

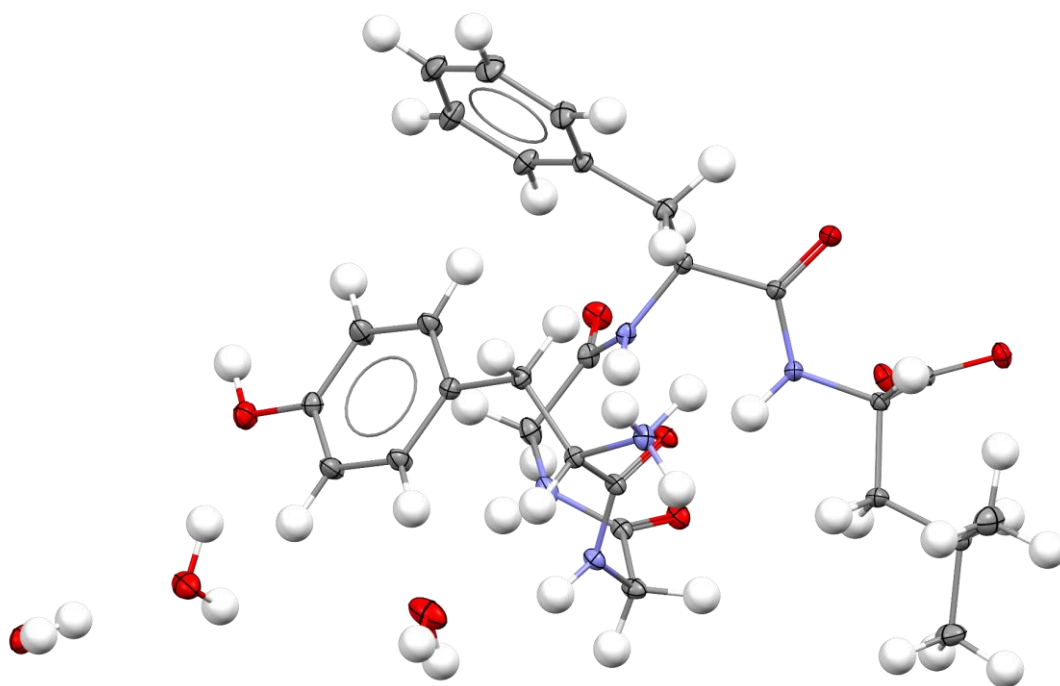
**Table S20:** Measurement details for the fibril-forming segment of the human prion protein (previously deposited in the protein data bank by Sawaya *et al.*<sup>S15</sup>). Information missing in this table was not given in the original paper and deposited structure.

|   |  |
|---|--|
| <b>PDB code</b>                               | 2OL9   |
| <b>Chemical formula</b>                       | C <sub>29</sub> H <sub>42</sub> N <sub>10</sub> O <sub>12</sub> ·5(H <sub>2</sub> O) |
| <b><i>M<sub>r</sub></i> (u)</b>               | 812.80   |
| <b>Crystal system</b>                         | Triclinic  |
| <b>Space group</b>                            | <i>P</i> 1   |
| <b><i>a, b, c</i> (Å)</b>                     | 14.0020, 4.8790, 15.1000   |
| <b><math>\alpha, \beta, \gamma</math> (°)</b> | 75.2340, 75.880, 78.8940   |
| <b><i>V</i> (Å<sup>3</sup>)</b>               | 957.96   |
| <b><i>Z</i></b>                               | 1  |
| <b>Diffractometer</b>                         | ALS BEAMLINE 8.2.2 diffractometer  |
| <b>Radiation type</b>                         | Synchrotron  |
| <b>Wavelength (Å)</b>                         | 0.88560  |
| <b>Temperature (K)</b>                        | 100  |
| <b>Crystal size (mm)</b>                      |  |
| <b>Absorption cor.</b>                        | -  |
| <b><math>\mu</math> (mm<sup>-1</sup>)</b>     | 0.20   |
| <b><i>T<sub>min</sub></i></b>                 | -  |
| <b><i>T<sub>max</sub></i></b>                 | -  |
| <b>Extinction correction.</b>                 | none   |
| <b>Resolution (Å)</b>                         | 0.85   |
| <b>hkl ranges</b>                             | <i>h</i> = -14, 15<br><i>k</i> = -4, 4<br><i>l</i> = 0, 17                           |
| <b>Theta min</b>                              | 1.887  |
| <b>Theta max</b>                              | 31.359   |
| <b>Theta full</b>                             | 31.359   |
| <b>Comple. (max)</b>                          | 0.8211   |
| <b>Comple. (full)</b>                         | 0.8211   |
| <b>Refl. Measured</b>                         | 3264   |
| <b>Unique refl.</b>                           | 2680   |
| <b>Unique obs. refl.</b>                      | 2642   |
| <b>Obs. criteria</b>                          | $F > 0$ & $F/u(F) > 3.0$ & $ F\_calc  > 10^{-3}$                                     |
| <b>Rint</b>                                   | 0.036  |
| <b>Rsym</b>                                   | -  |

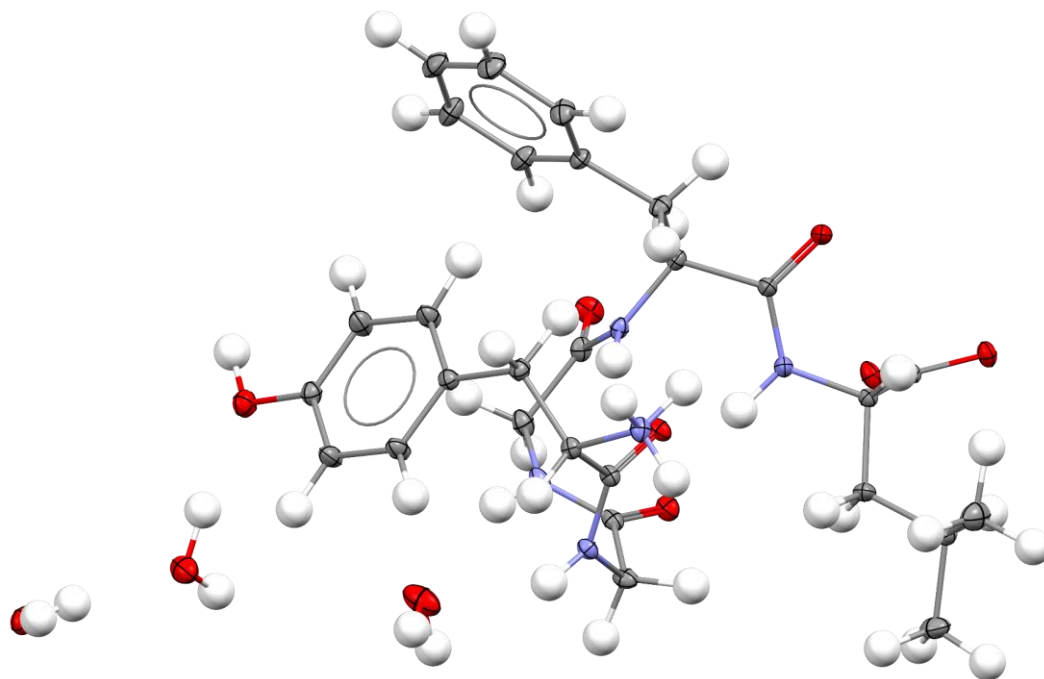
**Table S21:** Refinement of X-ray data for the fibril-forming segment of the human prion protein. CCDC deposition nos.: 1917596-1917598.

|  | <b>HAR</b>                     | <b>HAR-ELMO</b>                | <b>IAM</b>                     |
|--|--------------------------------|--------------------------------|--------------------------------|
| <b><math>R[F &gt; 3\sigma(F)]</math>, <math>wR(F)</math>, <math>S</math></b>                                 | 0.044, 0.052, 3.15             | 0.047, 0.057, 3.45             | 0.045, 0.053, 3.20             |
| <b>No. of reflections</b>  | 2642                           | 2642                           | 2642                           |
| <b>No. of parameters</b>   | 624                            | 624                            | 624                            |
| <b>No. of restraints</b>   | 0                              | 0                              | 0                              |
| <b>No. of constraints</b>  | 349                            | 349                            | 349                            |
| <b>H-atom treatment</b>  | H atoms treated isotropically. | H atoms treated isotropically. | H atoms treated isotropically. |
| <b><math>(\Delta/\sigma)_{\max}</math></b>   | 0.004                          | < 0.001                        | < 0.001                        |
| <b><math>\Delta\rho_{\max}</math>, <math>\Delta\rho_{\min}</math> (<math>\text{e}\text{\AA}^{-3}</math>)</b> | 0.51, -0.39                    | 0.51, -0.41                    | 0.50, -0.38                    |

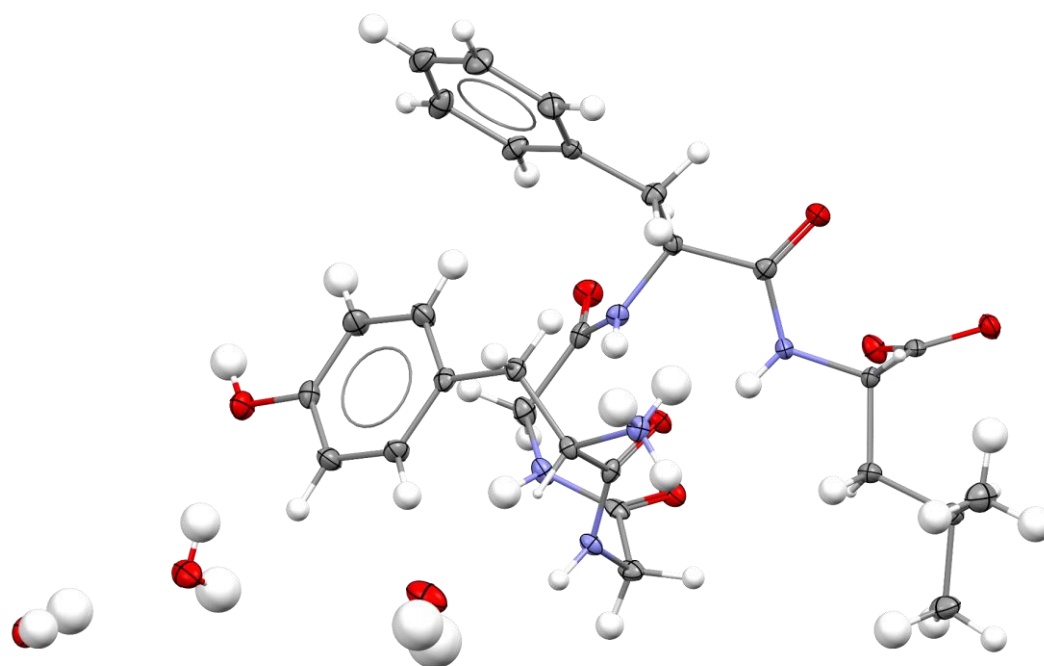
*Leu-Enkephalin (original CSD entry GEWWAG01)*<sup>S17</sup>



**Figure S81:** HAR molecular structure of Leu-enkephalin with ADPs depicted at a 50% probability level.



**Figure S82:** HAR-ELMO molecular structure of Leu-enkephalin with ADPs depicted at a 50% probability level.



**Figure S83:** IAM molecular structure of Leu-enkephalin with ADPs depicted at a 50% probability level.

**Table S22:** Measurement details for Leu-enkephalin (previously deposited in the Cambridge structural database by Pichon-Pesme *et al.*<sup>S17</sup>). Information missing in this table was not given in the original paper and deposited structure.

|   |  |
|---|--|
| <b>CSD entry</b>                          | GEWWAG01   |
| <b>Chemical formula</b>                   | C <sub>28</sub> H <sub>37</sub> N <sub>5</sub> O <sub>7</sub> ·3(H <sub>2</sub> O) |
| <b><i>M<sub>r</sub></i> (u)</b>           | 609.68   |
| <b>Crystal system</b>                     | Orthorhombic   |
| <b>Space group</b>                        | <i>P</i> 2 <sub>1</sub> 2 <sub>1</sub> 2 <sub>1</sub>                              |
| <b><i>a, b, c</i> (Å)</b>                 | 10.851 (4), 13.095 (3), 21.192 (4)   |
| <b><i>V</i> (Å<sup>3</sup>)</b>           | 3011.3 (14)  |
| <b><i>Z</i></b>                           | 4  |
| <b>Diffractometer</b>                     | CAD4F diffractometer   |
| <b>Radiation type</b>                     | MoK $\alpha$   |
| <b>Wavelength (Å)</b>                     | 0.71073  |
| <b>Temperature (K)</b>                    | 100  |
| <b>Crystal size (mm)</b>                  | -  |
| <b>Absorption cor.</b>                    | -  |
| <b><math>\mu</math> (mm<sup>-1</sup>)</b> | 0.10   |
| <b><i>T</i>min</b>                        | -  |
| <b><i>T</i>max</b>                        | -  |
| <b>Extinction correction.</b>             | none   |
| <b>Resolution (Å)</b>                     | 0.43   |
| <b>hkl ranges</b>                         | <i>h</i> = 0, 24<br><i>k</i> = 0, 29<br><i>l</i> = 0, 45                           |
| <b>Theta min</b>                          | 1.828  |
| <b>Theta max</b>                          | 54.797   |
| <b>Theta full</b>                         | 25.242   |
| <b>Comple. (max)</b>                      | 0.526  |
| <b>Comple. (full)</b>                     | 0.959  |
| <b>Refl. Measured</b>                     | 40844  |
| <b>Unique refl.</b>                       | 10777  |
| <b>Unique obs. refl.</b>                  | 5851   |
| <b>Obs. criteria</b>                      | $F > 0$ & $F/u(F) > 3.0$ & $ F\_calc  > 10^{-3}$                                   |
| <b><i>R</i>int</b>                        | -  |
| <b><i>R</i>merge</b>                      | -  |

**Table S23:** Refinement of X-ray data for Leu-enkephalin. CCDC deposition nos.: 1917730-1917732.

|  | <b>HAR</b>                     | <b>HAR-ELMO</b>                | <b>IAM</b>                     |
|--|--------------------------------|--------------------------------|--------------------------------|
| <b><math>R[F &gt; 3\sigma(F)]</math>, <math>wR(F)</math>, <math>S</math></b>                                 | 0.042, 0.023, 0.71             | 0.043, 0.024, 0.74             | 0.056, 0.034, 1.03             |
| <b>No. of reflections</b>  | 5851                           | 5851                           | 5851                           |
| <b>No. of parameters</b>   | 560                            | 560                            | 560                            |
| <b>No. of restraints</b>   | 0                              | 0                              | 0                              |
| <b>No. of constraints</b>  | 215                            | 215                            | 215                            |
| <b>H-atom treatment</b>  | H atoms treated isotropically. | H atoms treated isotropically. | H atoms treated isotropically. |
| <b><math>(\Delta/\sigma)_{\max}</math></b>   | 0.006                          | < 0.001                        | < 0.001                        |
| <b><math>\Delta\rho_{\max}</math>, <math>\Delta\rho_{\min}</math> (<math>\text{e}\text{\AA}^{-3}</math>)</b> | 0.20, -0.22                    | 0.21, -0.22                    | 0.29, -0.32                    |

***Crambin (original PDB file: 1EJG<sup>S18</sup>)***

The X-ray data set used in this study is the one associated with the PDB structure 1EJG previously deposited for the protein crambin. Notwithstanding the authors reported a refinement including solvent molecules, these were not present in the deposited PDB file. Fourier difference maps clearly showed regions of solvent residual densities that were not modelled. Consequently, the PLATON/SQUEEZE tool was applied to calculate the void space and extract its scattering contribution from the reflection list. Missing hydrogen atoms were placed according to calculated positions using the *tleap* utility of the AMBER Molecular Dynamics package.<sup>S16</sup> Furthermore, since at the moment HAR and HAR-ELMO techniques cannot properly treat disorder, only the atoms belonging to the major components in the disordered parts of the protein were modelled by assigning them full occupancies.

After this preliminary step, an unconstrained structure refinement of crambin was performed against the modified set of structure factors, using the IAM procedure inside the software TONTO, at maximum resolution ( $d=0.54 \text{ \AA}$ ) and one considering a subset of the data set ( $d=0.73 \text{ \AA}$ ). Subsequently, HAR-ELMO and another IAM were performed with parameters for all atoms belonging to the disordered regions kept fixed, based on the values obtained from the first IAM. Other than these, a few other atoms belonging to the outermost flexible loop of crambin were also kept fixed to guarantee convergence and a high precision of the final structure. In all cases, all the refined hydrogen atoms were treated isotropically, while all the refined non-hydrogen atoms were treated anisotropically.

For the sake of completeness, we report the list of atoms that we fixed during the refinements in Table S24.

**Table S24:** Crambin atoms (with corresponding residues and labels in the original PDB file) that were fixed during the HAR-ELMO refinements.

| Label in cif file | Residue | Label in pdb file | Label in cif file | Residue | Label in pdb file |
|-------------------|---------|-------------------|-------------------|---------|-------------------|
| N3                | THR 1   | N                 | C121              | GLU 23  | CG                |
| H1                | THR 1   | H1                | H158              | GLU 23  | HG2               |
| H2                | THR 1   | H2                | H159              | GLU 23  | HG3               |
| H3                | THR 1   | H3                | C122              | GLU 23  | CD                |
| C7                | THR 1   | CB                | O39               | GLU 23  | OE1               |
| H8                | THR 1   | HB                | O40               | GLU 23  | OE2               |
| H4                | THR 1   | HG1               | H164              | ALA 24  | HB1               |
| C8                | THR 1   | CG2               | H165              | ALA 24  | HB2               |
| H5                | THR 1   | HG21              | H166              | ALA 24  | HB3               |
| H6                | THR 1   | HG22              | C124              | LEU 25  | CB                |
| H7                | THR 1   | HG23              | H176              | LEU 25  | HB2               |
| C4                | THR 2   | CA                | H177              | LEU 25  | HB3               |
| C9                | THR 2   | CB                | C125              | LEU 25  | CG                |
| H15               | THR 2   | HB                | H175              | LEU 25  | HG                |
| O4                | THR 2   | OG1               | C126              | LEU 25  | CD1               |
| H11               | THR 2   | HG1               | H169              | LEU 25  | HD11              |
| C10               | THR 2   | CG2               | H170              | LEU 25  | HD12              |
| H12               | THR 2   | HG21              | H171              | LEU 25  | HD13              |
| H13               | THR 2   | HG22              | C127              | LEU 25  | CD2               |
| H14               | THR 2   | HG23              | H173              | LEU 25  | HD21              |
| H309              | CYS 4   | HB3               | H174              | LEU 25  | HD22              |
| H18               | PRO 5   | HB2               | H172              | LEU 25  | HD23              |
| H19               | PRO 5   | HB3               | H188              | THR 28  | HG21              |
| H26               | SER 6   | HG                | H189              | THR 28  | HG22              |
| C64               | ILE 7   | C                 | H190              | THR 28  | HG23              |
| O30               | ILE 7   | O                 | C21               | TYR 29  | CA                |
| C65               | ILE 7   | CA                | H201              | TYR 29  | HA                |
| H40               | ILE 7   | HA                | C132              | TYR 29  | CG                |
| C75               | ILE 7   | CB                | C133              | TYR 29  | CD1               |
| H39               | ILE 7   | HB                | H198              | TYR 29  | HD1               |
| C76               | ILE 7   | CG1               | C137              | TYR 29  | CD2               |
| H34               | ILE 7   | HG12              | H195              | TYR 29  | HD2               |
| H35               | ILE 7   | HG13              | C134              | TYR 29  | CE1               |
| C78               | ILE 7   | CG2               | H197              | TYR 29  | HE1               |
| H36               | ILE 7   | HG21              | C136              | TYR 29  | CE2               |
| H37               | ILE 7   | HG22              | H196              | TYR 29  | HE2               |
| H38               | ILE 7   | HG23              | C135              | TYR 29  | CZ                |
| C77               | ILE 7   | CD1               | O42               | TYR 29  | OH                |
| H31               | ILE 7   | HD11              | H194              | TYR 29  | HH                |
| H32               | ILE 7   | HD12              | H203              | THR 30  | HG1               |
| H33               | ILE 7   | HD13              | H204              | THR 30  | HG21              |
|                   |         |                   | H205              | THR 30  | HG22              |
|                   |         |                   | H206              | THR 30  | HG23              |

**Table S24:** continued.

| Label in cif file | Residue |    | Label in pdb file |
|-------------------|---------|----|-------------------|
| N29               | VAL     | 8  | N                 |
| H41               | VAL     | 8  | H                 |
| C63               | VAL     | 8  | CA                |
| H49               | VAL     | 8  | HA                |
| C79               | VAL     | 8  | CB                |
| H48               | VAL     | 8  | HB                |
| C80               | VAL     | 8  | CG1               |
| H42               | VAL     | 8  | HG11              |
| H43               | VAL     | 8  | HG12              |
| H44               | VAL     | 8  | HG13              |
| C81               | VAL     | 8  | CG2               |
| H45               | VAL     | 8  | HG21              |
| H46               | VAL     | 8  | HG22              |
| H47               | VAL     | 8  | HG23              |
| C85               | ARG     | 10 | CD                |
| H61               | ARG     | 10 | HD2               |
| H62               | ARG     | 10 | HD3               |
| H60               | ARG     | 10 | HE1               |
| N33               | ARG     | 10 | NE                |
| C86               | ARG     | 10 | CZ                |
| N34               | ARG     | 10 | NH1               |
| H56               | ARG     | 10 | HH11              |
| H57               | ARG     | 10 | HH12              |
| N35               | ARG     | 10 | NH2               |
| H58               | ARG     | 10 | HH21              |
| H59               | ARG     | 10 | HH22              |
| C88               | ASN     | 12 | CB                |
| H76               | ASN     | 12 | HB2               |
| H77               | ASN     | 12 | HB3               |
| C89               | ASN     | 12 | CG                |
| N36               | ASN     | 12 | ND2               |
| H74               | ASN     | 12 | HD21              |
| H75               | ASN     | 12 | HD22              |
| O36               | ASN     | 12 | OD1               |
| C92               | PHE     | 13 | CD1               |
| H84               | PHE     | 13 | HD1               |
| C93               | PHE     | 13 | CE1               |
| H83               | PHE     | 13 | HE1               |
| C94               | PHE     | 13 | CZ                |
| H82               | PHE     | 13 | HZ                |
| C96               | PHE     | 13 | CD2               |
| H80               | PHE     | 13 | HD2               |
| C95               | PHE     | 13 | CE2               |
| H81               | PHE     | 13 | HE2               |

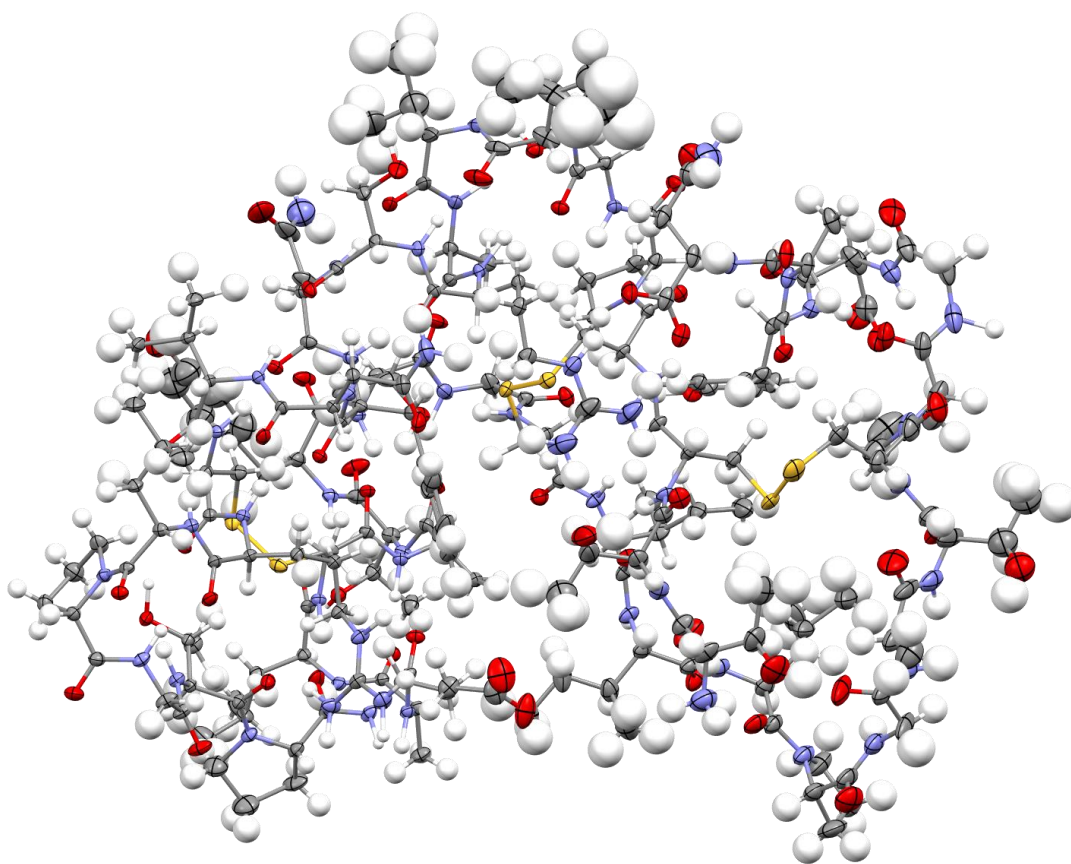
  

| Label in cif | Residue |    | Label in pdb file |
|--------------|---------|----|-------------------|
| H296         | ILE     | 33 | HD12              |
| C195         | ILE     | 34 | CB                |
| H292         | ILE     | 34 | HB                |
| C196         | ILE     | 34 | CG1               |
| H288         | ILE     | 34 | HG12              |
| H287         | ILE     | 34 | HG13              |
| C198         | ILE     | 34 | CG2               |
| H289         | ILE     | 34 | HG21              |
| H290         | ILE     | 34 | HG22              |
| H291         | ILE     | 34 | HG23              |
| C197         | ILE     | 34 | CD1               |
| H284         | ILE     | 34 | HD11              |
| H285         | ILE     | 34 | HD12              |
| H286         | ILE     | 34 | HD13              |
| H276         | ILE     | 35 | HG12              |
| H277         | ILE     | 35 | HG13              |
| H278         | ILE     | 35 | HG21              |
| H279         | ILE     | 35 | HG22              |
| H280         | ILE     | 35 | HG23              |
| H273         | ILE     | 35 | HD11              |
| H274         | ILE     | 35 | HD12              |
| H275         | ILE     | 35 | HD13              |
| C188         | PRO     | 36 | CB                |
| H270         | PRO     | 36 | HB2               |
| H271         | PRO     | 36 | HB3               |
| C189         | PRO     | 36 | CG                |
| H269         | PRO     | 36 | HG2               |
| H268         | PRO     | 36 | HG3               |
| H257         | GLY     | 37 | H                 |
| H261         | ALA     | 38 | HA                |
| H258         | ALA     | 38 | HB1               |
| H259         | ALA     | 38 | HB2               |
| H260         | ALA     | 38 | HB3               |
| H265         | THR     | 39 | H                 |
| C185         | THR     | 39 | CB                |
| H255         | THR     | 39 | HB                |
| O64          | THR     | 39 | OG1               |
| C186         | THR     | 39 | CG2               |
| H251         | THR     | 39 | HG1               |
| H252         | THR     | 39 | HG21              |
| H253         | THR     | 39 | HG22              |
| H254         | THR     | 39 | HG23              |

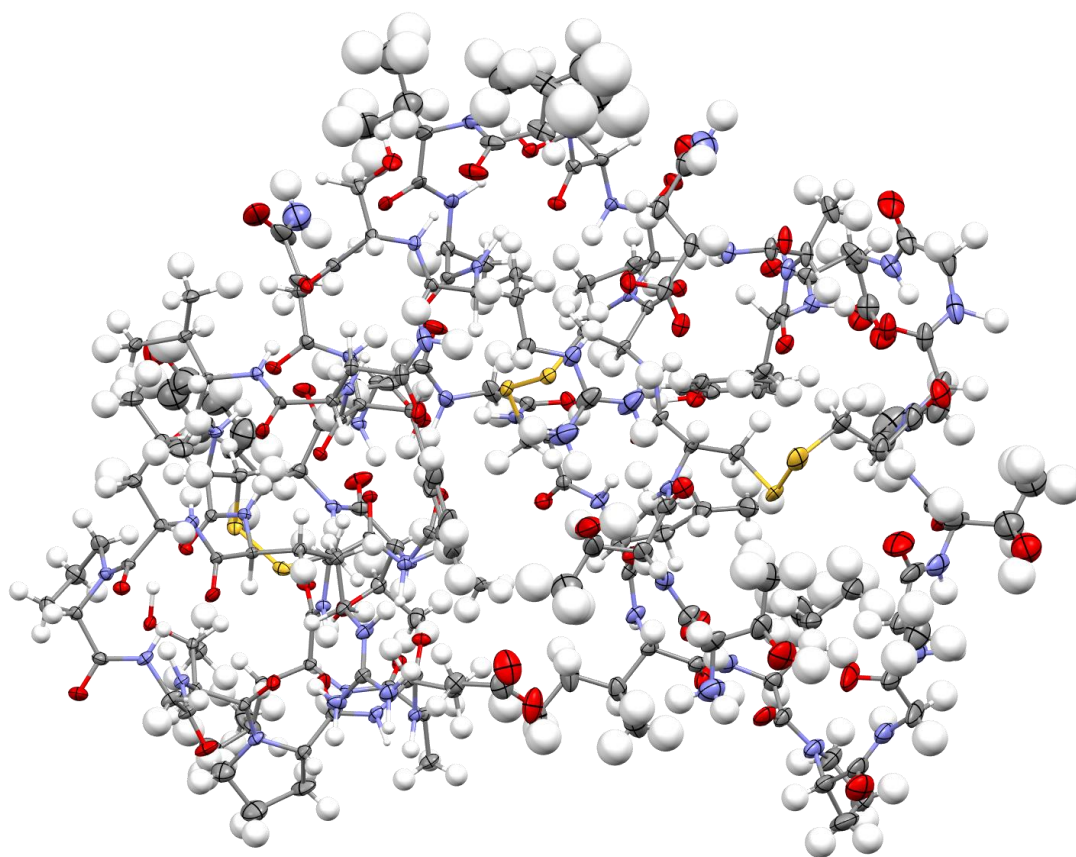
**Table S24:** continued.

| Label in cif file | Residue |    | Label in pdb file |
|-------------------|---------|----|-------------------|
| H126              | LEU     | 18 | HD11              |
| H127              | LEU     | 18 | HD12              |
| H128              | LEU     | 18 | HD13              |
| H123              | LEU     | 18 | HD21              |
| H124              | LEU     | 18 | HD22              |
| H125              | LEU     | 18 | HD23              |
| C114              | PRO     | 19 | CB                |
| H133              | PRO     | 19 | HB2               |
| H134              | PRO     | 19 | HB3               |
| C113              | PRO     | 19 | CG                |
| H135              | PRO     | 19 | HG2               |
| H136              | PRO     | 19 | HG3               |
| C112              | PRO     | 19 | CD                |
| H137              | PRO     | 19 | HD2               |
| H138              | PRO     | 19 | HD3               |
| C34               | PRO     | 22 | C                 |
| O15               | PRO     | 22 | O                 |
| C35               | PRO     | 22 | CA                |
| H156              | PRO     | 22 | HA                |
| C119              | PRO     | 22 | CB                |
| H151              | PRO     | 22 | HB2               |
| H150              | PRO     | 22 | HB3               |
| C118              | PRO     | 22 | CG                |
| H152              | PRO     | 22 | HG2               |
| H153              | PRO     | 22 | HG3               |
| C117              | PRO     | 22 | CD                |
| H155              | PRO     | 22 | HD2               |
| H154              | PRO     | 22 | HD3               |

| Label in cif file | Residue |    | Label in pdb file |
|-------------------|---------|----|-------------------|
| H246              | PRO     | 41 | HB2               |
| H247              | PRO     | 41 | HB3               |
| H245              | PRO     | 41 | HG2               |
| H244              | PRO     | 41 | HG3               |
| C180              | ASP     | 43 | CB                |
| H235              | ASP     | 43 | HB2               |
| H236              | ASP     | 43 | HB3               |
| C181              | ASP     | 43 | CG                |
| O62               | ASP     | 43 | OD1               |
| O63               | ASP     | 43 | OD2               |
| C170              | ASN     | 46 | CB                |
| H217              | ASN     | 46 | HB2               |
| H218              | ASN     | 46 | HB3               |
| C171              | ASN     | 46 | CG                |
| N55               | ASN     | 46 | ND2               |
| H215              | ASN     | 46 | HD21              |
| H216              | ASN     | 46 | HD22              |
| O60               | ASN     | 46 | OD1               |



**Figure S84:** HAR-ELMO molecular structure of crambin (0.54 Å resolution data-set) with ADPs at a 50% probability level.



**Figure S85:** HAR-ELMO molecular structure of crambin (0.73 Å resolution data-set) with ADPs at a 50% probability level.

**Table S25:** Measurement details for crambin (previously deposited in the protein data bank by Jelsch *et al.*<sup>S18</sup>). Information missing in this table was not given in the original paper and deposited structure.

|                                 |  |  |
|---------------------------------|--|--|
| <b>PDB code</b>                 | 1EJG   |  |
| <b>Chemical formula</b>         | C <sub>202</sub> H <sub>315</sub> N <sub>55</sub> O <sub>64</sub> S <sub>6</sub>             |  |
| <b><i>M<sub>r</sub></i> (u)</b> | 4730.48  |  |
| <b>Crystal system</b>           | Monoclinic   |  |
| <b>Space group</b>              | <i>P</i> 2 <sub>1</sub>  |  |
| <b><i>a, b, c</i> (Å)</b>       | 40.824, 18.498, 22.371   |  |
| <b>β (°)</b>                    | 90.47  |  |
| <b><i>V</i> (Å<sup>3</sup>)</b> | 16893.17   |  |
| <b><i>Z</i></b>                 | 2  |  |
| <b>Diffractometer</b>           | 300-mm MarResearch imaging plate diffractometer  |  |
| <b>Radiation type</b>           | Synchrotron  |  |
| <b>Wavelength (Å)</b>           | 0.54000  |  |
| <b>Temperature (K)</b>          | 100  |  |
| <b>Crystal size (mm)</b>        | -  |  |
| <b>Absorption cor.</b>          | none   |  |
| <b>μ (mm<sup>-1</sup>)</b>      | 0.06   |  |
| <b><i>T</i><sub>min</sub></b>   | -  |  |
| <b><i>T</i><sub>max</sub></b>   | -  |  |
| <b>Extinction correction.</b>   | none   |  |
| <b>Resolution (Å)</b>           | 0.54   | 0.73   |
| <b>hkl ranges</b>               | <i>h</i> = -75, 75<br><i>k</i> = 0, 34<br><i>l</i> = 0, 41                                   | <i>h</i> = -55, 55<br><i>k</i> = 0, 25<br><i>l</i> = 0, 30                                   |
| <b>Theta min</b>                | 0.692  | 0.692  |
| <b>Theta max</b>                | 30.021   | 21.707   |
| <b>Theta full</b>               | 18.905   | 18.905   |
| <b>Comple. (max)</b>            | 0.976  | 0.992  |
| <b>Comple. (full)</b>           | 0.994  | 0.994  |
| <b>Refl. Measured</b>           | 489969   | 489969   |
| <b>Unique refl.</b>             | 112233   | 46479  |
| <b>Unique obs. refl.</b>        | 96139  | 45265  |
| <b>Obs. criteria</b>            | <i>F</i> > 0 & <i>F</i> / <i>u</i> ( <i>F</i> ) > 3.0 &   <i>F</i> _calc  > 10 <sup>-3</sup> | <i>F</i> > 0 & <i>F</i> / <i>u</i> ( <i>F</i> ) > 3.0 &   <i>F</i> _calc  > 10 <sup>-3</sup> |
| <b><i>R</i><sub>int</sub></b>   | 0.070  | 0.055  |

**Table S26:** Refinement of X-ray data for crambin.

|  | <b>HAR-ELMO<br/>(0.54 Å)</b>   | <b>IAM<br/>(0.54 Å)</b>  | <b>HAR-ELMO<br/>(0.73 Å)</b>   | <b>IAM<br/>(0.73 Å)</b>  |
|--|--|--|--|--|
| <b><math>R[F &gt; 3\sigma(F)],</math><br/><math>wR(F), S</math></b>            | 0.072,<br>0.084, 2.24  | 0.070,<br>0.083, 2.21  | 0.062,<br>0.079, 2.77  | 0.062,<br>0.078, 2.74  |
| <b>No. of reflections</b>  | 96139  | 96139  | 45265  | 45265  |
| <b>No. of<br/>parameters</b>   | 2965   | 2965   | 2965   | 2965   |
| <b>No. of restraints</b>   | 0  | 0  | 0  | 0  |
| <b>No. of<br/>constraints</b>  | 2814   | 2814   | 2814   | 2814   |
| <b>H-atom<br/>treatment</b>  | H atoms<br>treated by a<br>mixture of<br>independent<br>and<br>constrained<br>refinement | H atoms<br>treated by a<br>mixture of<br>independent<br>and<br>constrained<br>refinement | H atoms<br>treated by a<br>mixture of<br>independent<br>and<br>constrained<br>refinement | H atoms<br>treated by a<br>mixture of<br>independent<br>and<br>constrained<br>refinement |
| <b><math>(\Delta/\sigma)_{\max}</math></b>                                     | < 0.001  | < 0.001  | < 0.001  | 0.0516   |
| <b><math>\Delta\rho_{\max}, \Delta\rho_{\min}</math><br/>(eÅ<sup>-3</sup>)</b> | 1.47, -0.77  | 1.51, -0.75  | 0.94, -0.68  | 0.96, -0.68  |

## Comparison of hydrogen bond distances

**Table S27:** Averaged X-H bond distances (in Å) according to the Allen-Bruno classes<sup>S19</sup> for the fibril-forming segment of the human prion protein. The last column refers to the number of bond lengths in the class.

| Allen-Bruno class                                | Neutron Reference <sup>S19</sup> | HAR                   | HAR-ELMO              | IAM                   | #               |
|--|----------------------------------|-----------------------|-----------------------|-----------------------|-----------------|
| X-H (all)  |                                  | 1.09(11) <sup>a</sup> | 1.07(14) <sup>a</sup> | 0.95(11) <sup>a</sup> | 42 <sup>a</sup> |
|  |                                  | 1.09(11) <sup>b</sup> | 1.07(13) <sup>b</sup> | 0.95(11) <sup>b</sup> | 41 <sup>b</sup> |
| Z <sub>3</sub> -Csp <sup>3</sup> -H              | 1.098(11)                        | 1.17(8)               | 1.13(10)              | 1.01(10)              | 6               |
| Z <sub>2</sub> -Csp <sup>3</sup> -H <sub>2</sub> | 1.091(17)                        | 1.12(9)               | 1.11(11)              | 1.01(10)              | 14              |
| C <sub>2</sub> -Csp <sup>3</sup> -H <sub>2</sub> | 1.092(17)                        | 1.11(9)               | 1.11(11)              | 1.01(11)              | 12              |
| C(ar)-H  | 1.083(17)                        | 1.08(7)               | 1.07(14)              | 0.96(8)               | 5               |
| Z-O-H  | 0.983(25)                        | 0.966(4)              | 0.967(4)              | 0.966(4)              | 1 <sup>c</sup>  |
| C(any)-O-H                                       | 0.980(21)                        | 0.966(4)              | 0.967(4)              | 0.966(4)              | 1 <sup>c</sup>  |
| Csp <sup>3</sup> -O-H                            | 0.970(12)                        | 0.966(4)              | 0.967(4)              | 0.966(4)              | 1 <sup>c</sup>  |
| N <sup>+</sup> -H                                | 1.036(16)                        | 1.12(15)              | 1.04(5)               | 0.94(9)               | 3               |
| Csp <sup>2</sup> -N-H <sub>2</sub><br>(all)      | 1.013(9)                         | 1.04(14) <sup>a</sup> | 1.02(23) <sup>a</sup> | 0.86(10) <sup>a</sup> | 8 <sup>a</sup>  |
|  |                                  | 1.02(13) <sup>b</sup> | 0.97(19) <sup>b</sup> | 0.84(10) <sup>b</sup> | 7 <sup>b</sup>  |
| Csp <sup>2</sup> -N-H <sub>2</sub><br>(N amido)  | 1.010(8)                         | 1.04(14) <sup>a</sup> | 1.02(23) <sup>a</sup> | 0.86(10) <sup>a</sup> | 8 <sup>a</sup>  |
|  |                                  | 1.02(13) <sup>b</sup> | 0.97(19) <sup>b</sup> | 0.84(10) <sup>b</sup> | 7 <sup>b</sup>  |
| Csp <sup>2</sup> -N-H <sub>2</sub><br>(N pl)     | 1.012(8)                         | 1.04(14) <sup>a</sup> | 1.02(23) <sup>a</sup> | 0.86(10) <sup>a</sup> | 8 <sup>a</sup>  |
|  |                                  | 1.02(13) <sup>b</sup> | 0.97(19) <sup>b</sup> | 0.84(10) <sup>b</sup> | 7 <sup>b</sup>  |
| Z <sub>2</sub> -N-H                              | 1.027(16)                        | 1.04(10)              | 1.04(11)              | 0.85(8)               | 5               |

<sup>a</sup> Including outliers.

<sup>b</sup> Excluding outliers. Outliers are defined as being outside the geometric criterion

$$d(i-j) < R(i) + R(j) + 0.4 \text{ \AA}$$

<sup>c</sup> The values are the averages with the standard uncertainty of the bond lengths. If there is only one value in the Allen Bruno class, the bond length is taken from the CIF file and the error is the experimental error.

**Table S28:** Averaged X-H bond distances (in Å) according to the Allen-Bruno classes<sup>S19</sup> for Leu-enkephalin. The last column refers to the number of bond lengths in the class.

| Allen-Bruno class                                | Neutron Reference <sup>S19</sup> | HAR     | HAR-ELMO | IAM      | #  |
|--|----------------------------------|---------|----------|----------|----|
| X-H (all)  |                                  | 1.04(6) | 1.04(7)  | 0.80(33) | 43 |
| Z <sub>3</sub> -Csp <sup>3</sup> -H              | 1.098(11)                        | 1.08(3) | 1.09(4)  | 0.59(49) | 10 |
| C <sub>3</sub> -Csp <sup>3</sup> -H              | 1.091(17)                        | 1.09(3) | 1.10(4)  | 0.44(51) | 7  |
| Z <sub>2</sub> -Csp <sup>3</sup> -H <sub>2</sub> | 1.092(17)                        | 1.08(3) | 1.09(3)  | 0.88(31) | 10 |
| C <sub>2</sub> -Csp <sup>3</sup> -H <sub>2</sub> | 1.083(17)                        | 1.09(3) | 1.10(3)  | 0.97(3)  | 6  |
| C(ar)-H  | 0.983(25)                        | 1.05(3) | 1.05(3)  | 0.84(32) | 9  |
| Z-O-H  | 0.980(21)                        | 0.97(5) | 0.97(6)  | 0.85(6)  | 7  |
| C(any)-O-H                                       | 1.098(11)                        | 0.98(2) | 0.99(2)  | 0.82(2)  | 1  |
| C(ar)-O-H  | 0.992(17)                        | 0.98(2) | 0.99(2)  | 0.82(2)  | 1  |
| N <sup>+</sup> -H                                | 1.036(16)                        | 1.03(3) | 1.00(5)  | 0.92(4)  | 3  |
| Z <sub>2</sub> -N-H                              | 1.027(16)                        | 0.96(2) | 0.97(3)  | 0.84(5)  | 4  |

**Table S29:** Averaged X-H bond distances (in Å) according to the Allen-Bruno classes<sup>S19</sup> for crambin for both resolutions. The last column refers to the number of bond lengths in the class.

| Allen-Bruno class                                | Neutron Reference <sup>S19</sup> | Resolution = 0.54 Å   |                       |                  | Resolution = 0.73 Å   |                      |                  |
|--|----------------------------------|-----------------------|-----------------------|------------------|-----------------------|----------------------|------------------|
|  |                                  | HAR-ELMO              | IAM                   | #                | HAR-ELMO              | IAM                  | #                |
| X-H (all)  |                                  | 1.11(12) <sup>a</sup> | 0.97(9) <sup>a</sup>  | 173 <sup>a</sup> | 1.10(10) <sup>a</sup> | 0.96(9) <sup>a</sup> | 173 <sup>a</sup> |
|  |                                  | 1.10(10) <sup>b</sup> | 0.96(9) <sup>b</sup>  | 167 <sup>b</sup> | 1.10(10) <sup>b</sup> | 0.95(9) <sup>b</sup> | 172 <sup>b</sup> |
| Z <sub>3</sub> -Csp <sup>3</sup> -H              | 1.098(11)                        | 1.12(10) <sup>a</sup> | 0.98(9) <sup>a</sup>  | 43 <sup>a</sup>  | 1.10(9) <sup>a</sup>  | 0.96(9) <sup>a</sup> | 43 <sup>a</sup>  |
|  |                                  | 1.11(8) <sup>b</sup>  | 0.97(7) <sup>b</sup>  | 41 <sup>b</sup>  | 1.10(8) <sup>b</sup>  | 0.95(7) <sup>b</sup> | 42 <sup>b</sup>  |
| C <sub>3</sub> -Csp <sup>3</sup> -H              | 1.091(17)                        | 1.09(10)              | 0.96(7)               | 4                | 1.08(6)               | 0.95(4)              | 4                |
| Z <sub>2</sub> -Csp <sup>3</sup> -H <sub>2</sub> | 1.092(17)                        | 1.11(11) <sup>a</sup> | 0.98(9) <sup>a</sup>  | 55 <sup>a</sup>  | 1.10(10)              | 0.97(9)              | 55               |
|  |                                  | 1.10(10) <sup>b</sup> | 0.97(9) <sup>b</sup>  | 53 <sup>b</sup>  |                       |                      |                  |
| C <sub>2</sub> -Csp <sup>3</sup> -H <sub>2</sub> | 1.083(17)                        | 1.10(10) <sup>a</sup> | 0.97(8) <sup>a</sup>  | 24 <sup>a</sup>  | 1.09(9)               | 0.96(8)              | 24               |
|  |                                  | 1.09(9) <sup>b</sup>  | 0.97(8) <sup>b</sup>  | 23 <sup>b</sup>  |                       |                      |                  |
| Z-Csp <sup>3</sup> -H <sub>3</sub>               | 1.077(26)                        | 1.13(18) <sup>a</sup> | 0.98(11) <sup>a</sup> | 23 <sup>a</sup>  | 1.09(13)              | 0.97(11)             | 23               |
|  |                                  | 1.10(13) <sup>b</sup> | 0.97(11) <sup>b</sup> | 21 <sup>b</sup>  |                       |                      |                  |
| C-Csp <sup>3</sup> -H <sub>3</sub>               | 1.077(29)                        | 1.13(18) <sup>a</sup> | 0.98(11) <sup>a</sup> | 23 <sup>a</sup>  | 1.09(13)              | 0.97(11)             | 23               |
|  |                                  | 1.10(13) <sup>b</sup> | 0.97(11) <sup>b</sup> | 21 <sup>b</sup>  |                       |                      |                  |
| C(ar)-H  | 0.983(25)                        | 1.10(11)              | 0.96(9)               | 4                | 1.07(9)               | 0.95(6)              | 4                |
| Z-O-H  | 0.983(25)                        | 1.04(7)               | 0.91(6)               | 4                | 1.03(8)               | 0.91(8)              | 4                |
| C(any)-O-H                                       | 0.980(21)                        | 1.04(7)               | 0.91(6)               | 4                | 1.03(8)               | 0.91(8)              | 4                |
| Csp <sup>3</sup> -O-H                            | 0.970(12)                        | 1.02(7)               | 0.90(8)               | 3                | 1.01(8)               | 0.89(9)              | 3                |
| C(ar)-O-H  | 0.992(17)                        | 1.09(4)               | 0.93(4)               | 1 <sup>c</sup>   | 1.10(5)               | 0.94(4)              | 1 <sup>c</sup>   |

**Table S29:** continued.

| Allen-Bruno class                                      | Neutron Reference <sup>S19</sup> | Resolution = 0.54 Å |          |    | Resolution = 0.73 Å |         |    |
|--|----------------------------------|---------------------|----------|----|---------------------|---------|----|
|  |                                  | HAR-ELMO            | IAM      | #  | HAR-ELMO            | IAM     | #  |
| <i>Csp</i> <sup>2</sup> -N-H <sub>2</sub><br>(all)     | 1.013(9)                         | 1.05(6)             | 0.90(11) | 6  | 1.04(7)             | 0.90(7) | 6  |
| <i>Csp</i> <sup>2</sup> -N-H <sub>2</sub><br>(N amido) | 1.010(8)                         | 1.00(1)             | 0.82(12) | 2  | 0.98(8)             | 0.83(6) | 2  |
| <i>Csp</i> <sup>2</sup> -N-H <sub>2</sub><br>(N pl)    | 1.012(8)                         | 1.08(4)             | 0.95(5)  | 4  | 1.07(3)             | 0.94(5) | 4  |
| Z <sub>2</sub> -N-H                                    | 1.027(16)                        | 1.10(1)             | 0.95(8)  | 38 | 1.10(10)            | 0.94(9) | 38 |

<sup>a</sup> Including outliers.

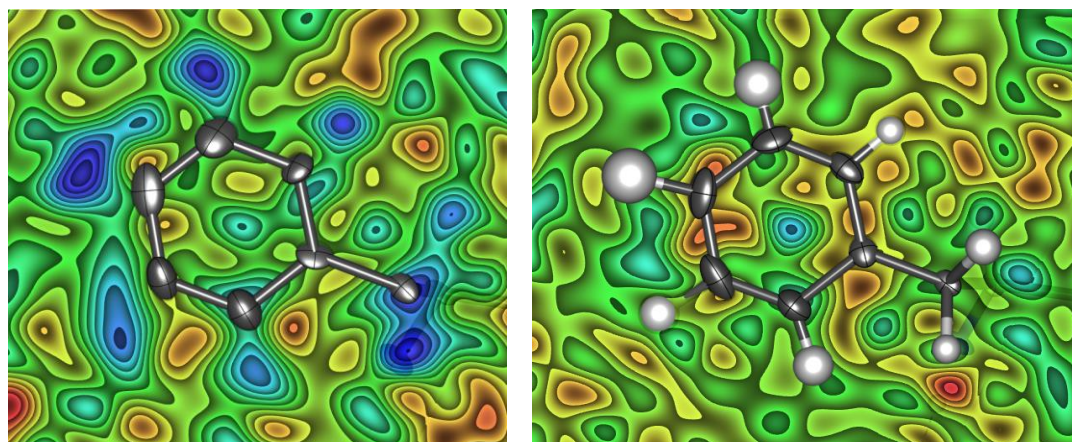
<sup>b</sup> Excluding outliers. Outliers are defined as being outside the geometric criterion

$$d(i-j) < R(i) + R(j) + 0.4 \text{ \AA}$$

<sup>c</sup> The values are the averages with the standard uncertainty of the bond lengths. If there is only one value in the Allen Bruno class, the bond length is taken from the CIF file and the error is the experimental error.

## Comparison of residual and deformation densities

### Fibril segment – Residual Densities

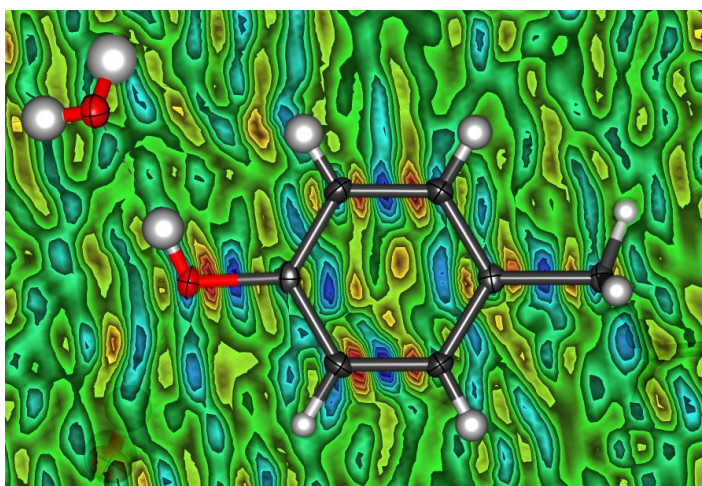


(a)

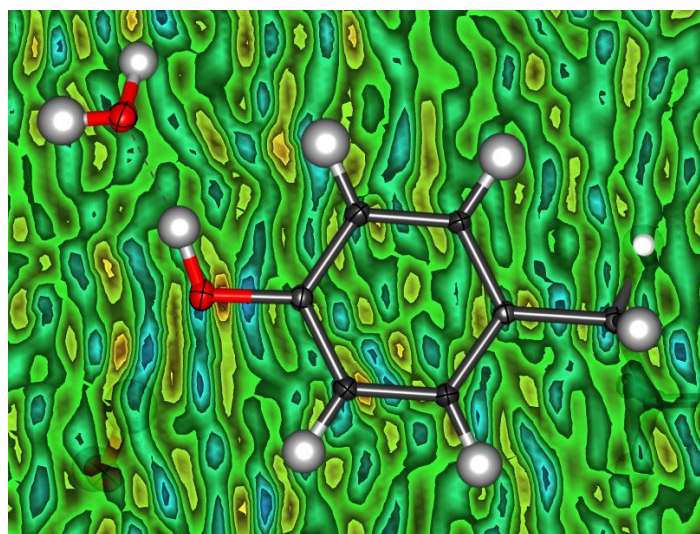
(b)

**Figure S86:** Phenyl group in the fibril-forming segment of the human prion protein: a) without hydrogen atoms as deposited, b) with hydrogen atoms refined in the HAR-ELMO procedure. For (a) and (b) min and max values are  $-0.2$  and  $0.3 \text{ e}\text{\AA}^{-3}$  and contour lines at  $0.05 \text{ e}\text{\AA}^{-3}$  interval. Colour code: from blue (positive), through green (zero) to red (negative). ADPs at 50% probability.

## Leu-enkephalin – Residual Densities

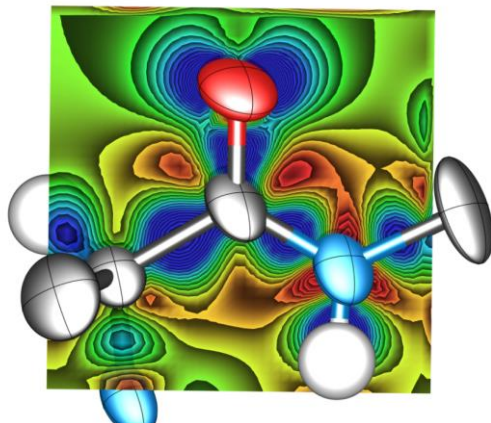


**Figure S87:** Residual density map for Leu-enkephalin in the plane of the TYR group for the IAM refinement. Min and max values are  $-0.2$  and  $0.3 \text{ e}\text{\AA}^{-3}$ , contour lines at  $0.05 \text{ e}\text{\AA}^{-3}$  interval. Colour code: from blue (positive), through green (zero) to red (negative). ADPs at 50% probability.

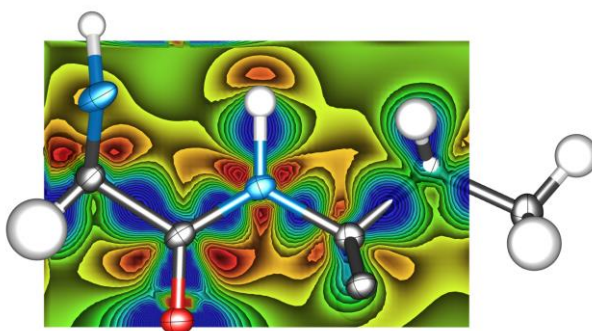


**Figure S88:** Residual density map for Leu-enkephalin in the plane of the TYR group for the HAR-ELMO refinement. Min and max values are  $-0.2$  and  $0.3 \text{ e}\text{\AA}^{-3}$ , contour lines at  $0.05 \text{ e}\text{\AA}^{-3}$  interval. Colour code: from blue (positive), through green (zero) to red (negative). ADPs at 50% probability.

## Crambin – Deformation Densities

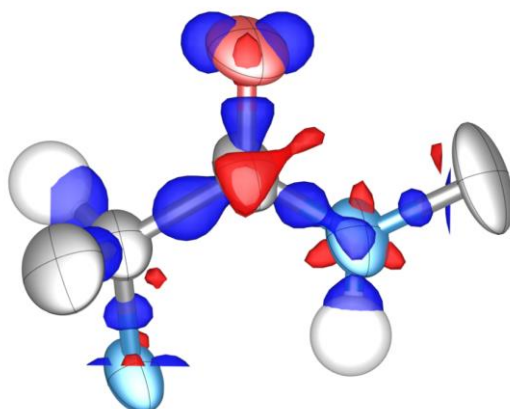


**Figure S89:** Deformation density map for crambin in the plane of a PRO group (residue 36) for the HAR-ELMO refinement with reflections up to 0.54 Å resolution. Colour code: from blue (positive), through green (zero) to red (negative). ADPs at 50% probability.

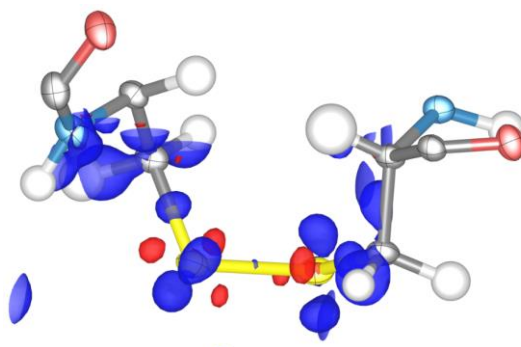


**Figure S90:** Deformation density map for crambin in the plane of an ALA group (residue 9) for the HAR-ELMO refinement with reflections up to 0.54 Å resolution. Colour code: from blue (positive), through green (zero) to red (negative). ADPs at 50% probability.

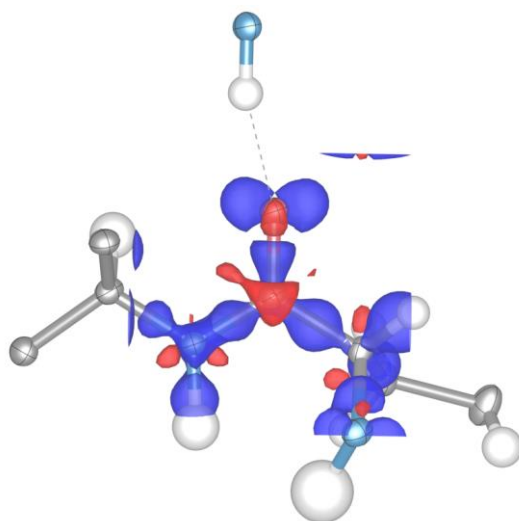
## Crambin – 3D Deformation Densities



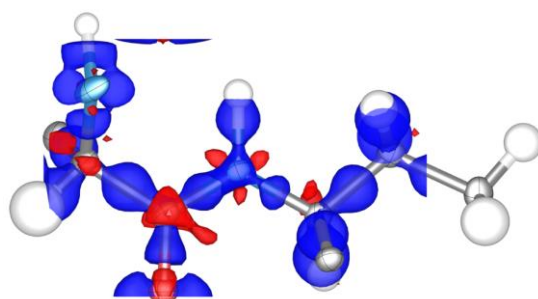
**Figure S91:** Deformation density of crambin residue 36 (PRO) corresponding to the HAR-ELMO refinement with reflections up to a resolution of 0.54 Å (isosurface level: 0.05 eÅ<sup>-3</sup>). Colour scheme: blue (positive) and red (negative). ADPs at 50% probability.



**Figure S92:** Deformation density of crambin around the disulphide bond between residues 32 (CYX) and 4 (CYX) corresponding to the HAR-ELMO refinement with reflections up to a resolution of 0.54 Å (isosurface level: 0.05 eÅ<sup>-3</sup>). Colour scheme: blue (positive) and red (negative). ADPs at 50% probability. The sulphur lone pairs are clearly visible.



**Figure S93:** Deformation density of crambin (hydrogen bond between residues 25 (LEU) and 29 (THR)) corresponding to the HAR-ELMO refinement with reflections up to a resolution of 0.54 Å (isosurface level: 0.05 eÅ<sup>-3</sup>). Colour scheme: blue (positive) and red (negative).



**Figure S94:** Deformation density of crambin residue 9 (ALA) corresponding to the HAR-ELMO refinement with reflections up to a resolution of 0.54 Å (isosurface level: 0.05 eÅ<sup>-3</sup>). Colour scheme: blue (positive) and red (negative).

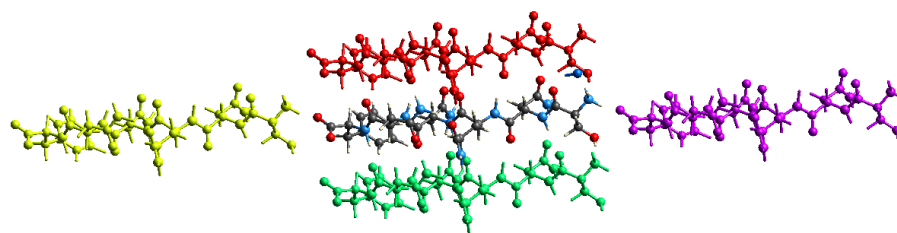
## Interaction Energies and Hirshfeld Surface Analysis for the fibril-forming segment of the human prion protein.

Dimer model interaction energies were calculated using the procedure outlined in references S20 and S21 and implemented in the software CrystalExplorer. The colour code in Table S30 shows which molecule is the partner forming the dimer with respect to the central molecule shown in Figure S95. Red and green refer to parallel strands, which are symmetry-related, yellow and purple to head-to-tail contacts, also symmetry-related, and blue to co-crystallized water.

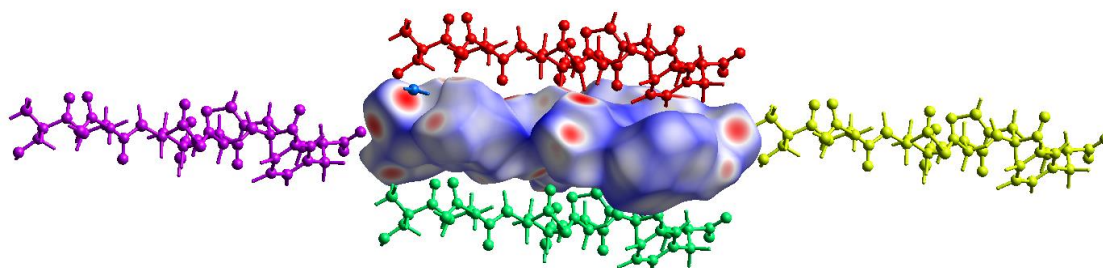
**Table S30:** Interaction Energies (kJ/mol) calculated at B3LYP/6-31G(d,p) level between dimers found in the crystal structure of the fibril-forming segment of the human prion protein. As discussed in the text, the parallel strands are not the main interactions in terms of energy. R is the distance between molecular centroids (mean atomic positions). The total energies are the sum of the four energy components, properly scaled according to the scale factors k shown below.

|        | R (Å) | E_ele  | E_pol  | E_dis  | E_rep | E_tot  |
|--------|-------|--------|--------|--------|-------|--------|
| Red    | 4.88  | -221.5 | -129.6 | -169.7 | 499.5 | -169.3 |
| Green  | 4.88  | -221.5 | -129.6 | -169.7 | 499.5 | -169.3 |
| Yellow | 22.07 | -182.7 | -42.5  | -11.2  | 52.1  | -202.2 |
| Purple | 22.07 | -182.7 | -42.5  | -11.2  | 52.1  | -202.2 |
| Blue   | 10.01 | -113.2 | -36.8  | -14.0  | 101.3 | -96.5  |

| Energy Model                                     | k_ele | k_pol | k_disp | k_rep |
|--|-------|-------|--------|-------|
| CE-B3LYP ... B3LYP/6-31G(d,p) electron densities | 1.057 | 0.740 | 0.871  | 0.618 |



(a)

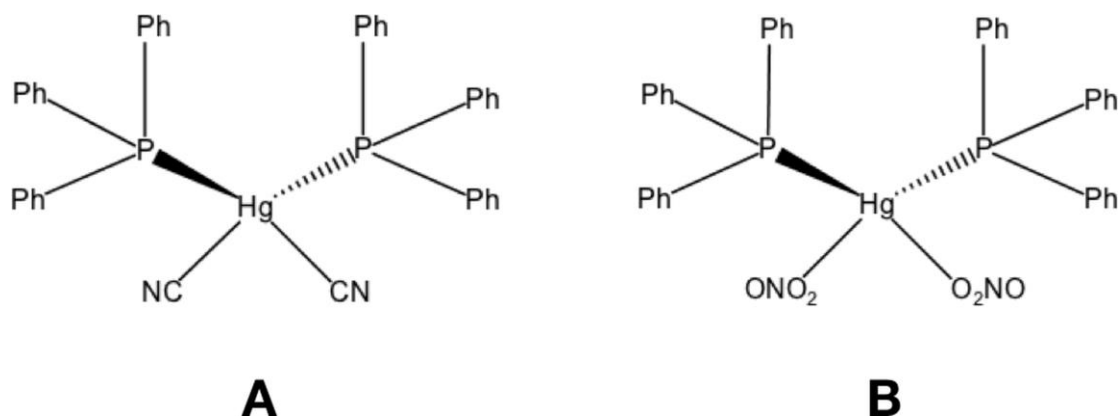


(b)

**Figure S95:** Symmetry-generated cluster around a central molecule of the fibril-forming segment of the human prion protein, colour coded according to Table S30. In b) a Hirshfeld surface is plotted around the central molecule with the property  $d_{\text{norm}}$  mapped onto it. Red areas show close contacts such as hydrogen bonds. Details about Hirshfeld Surface Analysis can be found in ref. S22.

## Refinement of coordination compounds

*Specific model molecule for ELMOs of coordination compounds.* For the sake of completeness, in Figure S96 we report the Lewis structure of the coordination compounds investigated in this paper:  $(\text{Ph}_3\text{P})_2\text{Hg}(\text{CN})_2$  (see Figure S96-A) and  $(\text{Ph}_3\text{P})_2\text{Hg}(\text{NO}_3)_2$  (see Figure S96-B).



**Figure S96:** Coordination compounds investigated in the paper: (A)  $(\text{Ph}_3\text{P})_2\text{Hg}(\text{CN})_2$  and (B)  $(\text{Ph}_3\text{P})_2\text{Hg}(\text{NO}_3)_2$

As mentioned earlier, the ELMOs used in the HAR-ELMO refinements of these two coordination compounds were obtained by performing ELMO calculations on tailor-made model molecules. In fact, the current ELMO libraries cover only the subunits for the twenty natural amino acids and water. The model systems adopted for the ELMO computations are depicted in Figure S97.

For model molecule  $(\text{H}_3\text{P})_2\text{Hg}(\text{CN})_2$  (see Figure S97-A), we computed the following ELMOs to describe:

- all the Hg core electrons;
- all the electrons of the  $\text{CN}^-$  ligands, including the electron pairs delocalized between the carbon atoms and Hg. This means that, for each ligand, we considered an ELMO delocalized between C and Hg to describe the bonds between the two atoms;
- the lone-pair electrons of the phosphorous atoms delocalized between P and Hg. In other words, we computed ELMOs delocalized between each of the P atoms and Hg to describe the different P-Hg bonds.

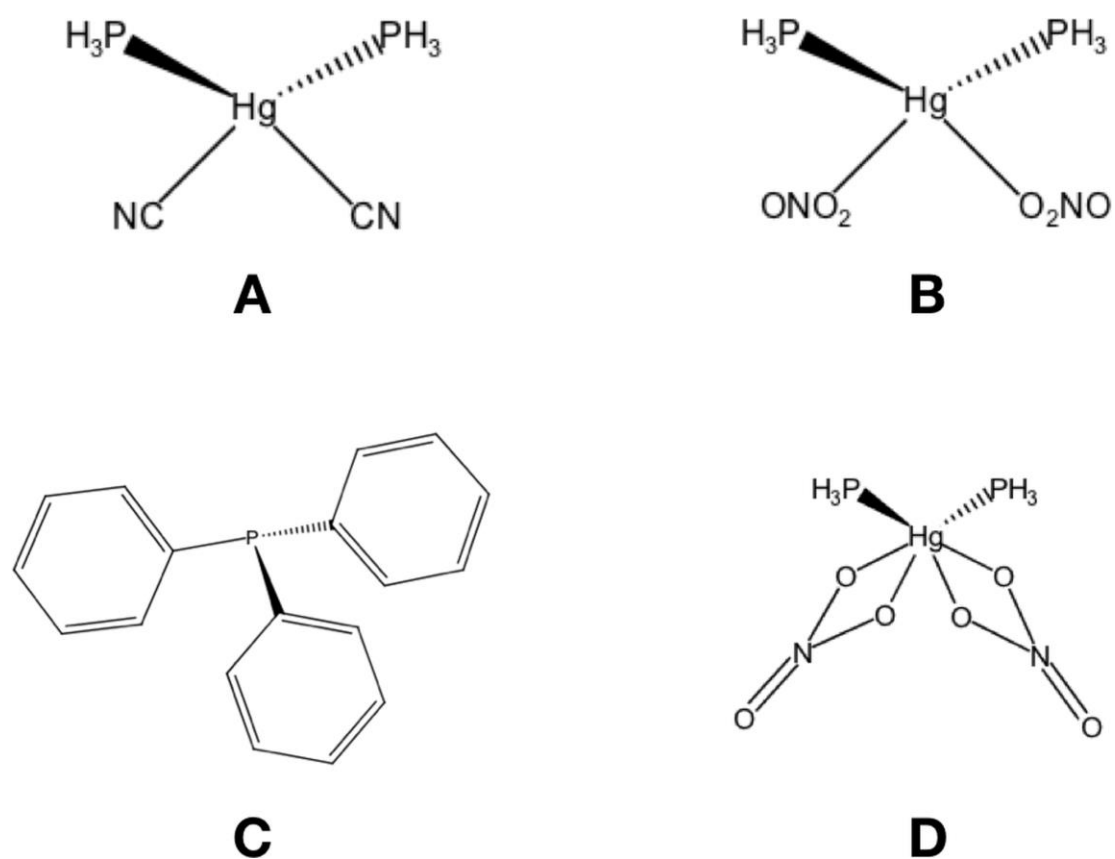
For model molecule  $(\text{H}_3\text{P})_2\text{Hg}(\text{NO}_3)_2$  (see Figure S97-B), we computed the following ELMOs to describe:

- all the Hg core electrons;
- all the electrons of the  $\text{NO}_3^-$  ligands, including the electron pairs delocalized between the oxygen atoms and Hg. This means that, for each ligand, we also considered ELMOs delocalized between the O atoms and Hg to describe the four Hg-O bonds of the system (see Figure S97-D for details);
- the lone-pair electrons of the phosphorous atoms delocalized between P and Hg. In other words, we computed ELMOs delocalized between each of the P atoms and Hg to describe the different P-Hg bonds.

To fully take into account the non-equivalence of the two Hg-O dative bonds provided by each nitrate ligand, we considered a geometry for model molecule  $(\text{H}_3\text{P})_2\text{Hg}(\text{NO}_3)_2$  characterized by different Hg-O bond lengths within the same nitrate ligand (2.845 Å and 2.467 Å).

For triphenylphosphine (see Figure S97-C) we computed all the ELMOs needed to describe all the electrons of the  $\text{PPh}_3$  ligands, except for those associated with the lone pair of the phosphorus atom.

All the ELMO calculations on the model molecules were performed using the DZP-DKH basis set and adopting localization schemes corresponding to the Lewis structures of the molecules under exam.



**Figure S97:** Model molecules used for the computations of the ELMOs used in the HAR-ELMO refinements of the two coordination compounds investigated in this study: A)  $(\text{H}_3\text{P})_2\text{Hg}(\text{CN})_2$ , B)  $(\text{H}_3\text{P})_2\text{Hg}(\text{NO}_3)_2$  and, C) triphenylphosphine ( $\text{PPh}_3$ ). Figure D is another representation of model molecule  $(\text{H}_3\text{P})_2\text{Hg}(\text{NO}_3)_2$  with the details of the two non-equivalent bonds between the oxygen atoms and Hg.

**Table S31:** Measurement details for the X-ray diffraction experiments of  $(\text{Ph}_3\text{P})_2\text{Hg}(\text{NO}_3)_2$  and  $(\text{Ph}_3\text{P})_2\text{Hg}(\text{CN})_2$ .

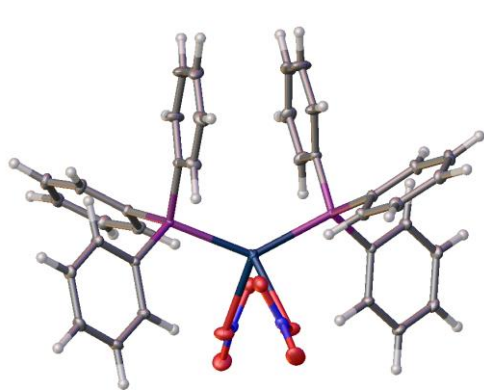
|   |  |  |
|---|--|--|
| <b>Chemical formula</b>                   | $(\text{Ph}_3\text{P})_2\text{Hg}(\text{NO}_3)_2$          | $(\text{Ph}_3\text{P})_2\text{Hg}(\text{CN})_2$            |
| <b>Mr (u)</b>                             | 849.15   | 777.17   |
| <b>Crystal system</b>                     | monoclinic   | orthorhombic   |
| <b>Space group</b>                        | C 2/c  | P na2 <sub>1</sub>   |
| <b>a, b, c, <math>\beta</math> (Å)</b>    | 13.2836(4)<br>13.8899(4)<br>17.7854(5)<br>91.070 (1)       | 17.9310(5)<br>9.8963(3)<br>18.1031(5)                      |
| <b>V (Å<sup>3</sup>)</b>                  | 3280.97(16)  | 3212.41(16)  |
| <b>Z</b>                                  | 4  | 4  |
| <b>Radiation type</b>                     | X-ray (MoK $\alpha$ )                                      | X-ray (MoK $\alpha$ )                                      |
| <b>Wavelength (Å)</b>                     | 0.71073  | 0.71073  |
| <b>Temperature (K)</b>                    | 100(1)   | 100(1)   |
| <b>Crystal size (mm)</b>                  | 0.26x0.22x<br>0.19   | 0.17x0.11x<br>0.09   |
| <b>Absorption cor.</b>                    | multi-scan   | multi-scan   |
| <b><math>\mu</math> (mm<sup>-1</sup>)</b> | 4.813  | 4.895  |
| <b>Tmin</b>                               | 0.30   | 0.53   |
| <b>Tmax</b>                               | 0.40   | 0.64   |
| <b>Extinction cor.<sup>S10</sup></b>      | none   | none   |
| <b>Resolution (Å)</b>                     | 0.50   | 0.55   |
| <b>hkl ranges</b>                         | $h=-26, 26$<br>$k=-27, 27$<br>$l=-35, 35$                  | $h=-32, 32$<br>$k=-17, 17$<br>$l=-32, 32$                  |
| <b>Theta min</b>                          | 2.12   | 2.35   |
| <b>Theta max</b>                          | 45.29  | 40.25  |
| <b>Theta full</b>                         | 39.39  | 40.25  |
| <b>Comple. (max)</b>                      | 0.995  | 1.000  |
| <b>Comple. (full)</b>                     | 1.000  | 1.000  |
| <b>Refl. Measured</b>                     | 124199   | 269147   |
| <b>Unique refl.</b>                       | 13738  | 10335  |
| <b>Unique obs. refl.</b>                  | 13031  | 9846   |
| <b>Obs. criteria</b>                      | F>0<br>F/u(F)>3.0<br> F <sub>calc</sub>  >10 <sup>-3</sup> | F>0<br>F/u(F)>3.0<br> F <sub>calc</sub>  >10 <sup>-3</sup> |
| <b>Rint</b>                               | 0.0263   | 0.0359   |
| <b>Rsigma</b>                             | 0.0134   | 0.0262   |
| <b>CCDC number</b>                        | 1917593  | 1917594  |

**Table S32:** Refinement of X-ray data for (Ph<sub>3</sub>P)<sub>2</sub>Hg(NO<sub>3</sub>)<sub>2</sub> and (Ph<sub>3</sub>P)<sub>2</sub>Hg(CN)<sub>2</sub>.

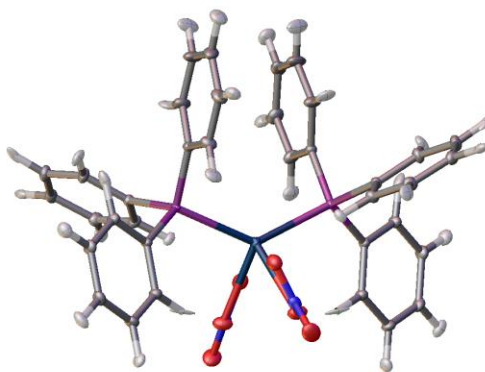
| (Ph <sub>3</sub> P) <sub>2</sub> Hg(NO <sub>3</sub> ) <sub>2</sub>      | IAM   | HAR-ELMO,<br>isotropic           | HAR-ELMO,<br>anisotropic                              |
|---|---|----------------------------------|---|
| <i>R</i> [ <i>F</i> >3σ( <i>F</i> )], <i>wR</i> ( <i>F</i> ), <i>S</i>  | 0.0204, 0.0221,<br>3.070                              | 0.0163, 0.0153,<br>2.114         | 0.0162, 0.0151,<br>2.098                              |
| <b>No. of reflections</b>   | 13031   | 13031                            | 13031   |
| <b>No. of parameters</b>  | 277   | 277                              | 352   |
| <b>H-atom treatment</b>   | H atoms refined<br>isotropically                      | H atoms refined<br>isotropically | All H-atom<br>parameters refined<br>(anisotropically) |
| <i>Δρ</i> <sub>max</sub> , <i>Δρ</i> <sub>min</sub> (eÅ <sup>-3</sup> ) | 2.072, -0.843   | 1.632, -0.669                    | 1.632, -0.680   |
| (Ph <sub>3</sub> P) <sub>2</sub> Hg(NO <sub>3</sub> ) <sub>2</sub>      | HAR, relativistic                                     | HAR, isotropic                   | HAR, anisotropic                                      |
| <i>R</i> [ <i>F</i> >3σ( <i>F</i> )], <i>wR</i> ( <i>F</i> ), <i>S</i>  | 0.0150, 0.0135,<br>1.875                              | 0.0163, 0.0149,<br>2.072         | 0.0162, 0.0148,<br>2.057                              |
| <b>No. of reflections</b>   | 13031   | 13031                            | 13031   |
| <b>No. of parameters</b>  | 352   | 277                              | 352   |
| <b>H-atom treatment</b>   | All H-atom<br>parameters refined<br>(anisotropically) | H atoms refined<br>isotropically | All H-atom<br>parameters refined<br>(anisotropically) |
| <i>Δρ</i> <sub>max</sub> , <i>Δρ</i> <sub>min</sub> (eÅ <sup>-3</sup> ) | 1.149, -0.805   | 1.664, -0.675                    | 1.672, -0.675   |
| (Ph <sub>3</sub> P) <sub>2</sub> Hg(CN) <sub>2</sub>                    | IAM   | HAR-ELMO,<br>isotropic           | HAR-ELMO,<br>anisotropic                              |
| <i>R</i> [ <i>F</i> >3σ( <i>F</i> )], <i>wR</i> ( <i>F</i> ), <i>S</i>  | 0.0215, 0.0211,<br>2.080                              | 0.0188, 0.0165,<br>1.632         | 0.0187, 0.0163,<br>1.619                              |
| <b>No. of reflections</b>   | 9846  | 9846                             | 9846  |
| <b>No. of parameters</b>  | 504   | 504                              | 657   |
| <b>H-atom treatment</b>   | H atoms refined<br>isotropically                      | H atoms refined<br>isotropically | All H-atom<br>parameters refined<br>(anisotropically) |
| <i>Δρ</i> <sub>max</sub> , <i>Δρ</i> <sub>min</sub> (eÅ <sup>-3</sup> ) | 1.299, -1.021   | 1.130, -1.015                    | 1.118, -0.994   |

Table S32: continued.

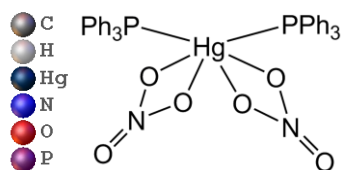
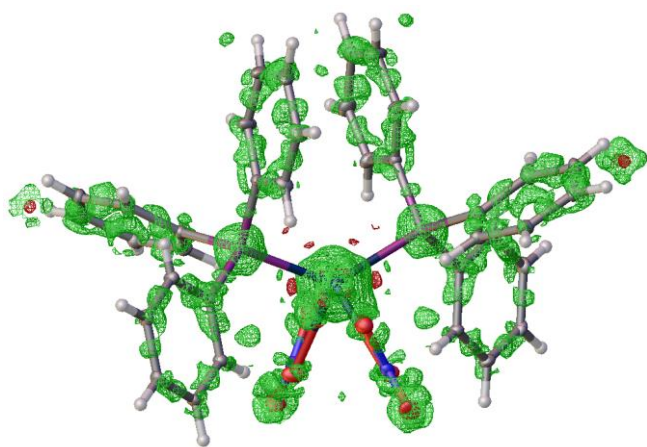
| <b>(Ph<sub>3</sub>P)<sub>2</sub>Hg(CN)<sub>2</sub></b>                    | - | <b>HAR, isotropic</b>            | <b>HAR, anisotropic</b>                               |
|---|---|----------------------------------|---|
| <b><i>R</i>[<i>F</i>&gt;3σ(<i>F</i>)], <i>wR</i>(<i>F</i>), <i>S</i></b>  |   | 0.0188, 0.0165,<br>1.626         | 0.0187, 0.0162,<br>1.613                              |
| <b>No. of reflections</b>   |   | 9846                             | 9846  |
| <b>No. of parameters</b>  |   | 504                              | 657   |
| <b>H-atom treatment</b>   |   | H atoms refined<br>isotropically | All H-atom<br>parameters refined<br>(anisotropically) |
| <b><i>Δρ</i><sub>max</sub>, <i>Δρ</i><sub>min</sub> (eÅ<sup>-3</sup>)</b> |   | 1.143, -1.016                    | 1.132, -0.995   |



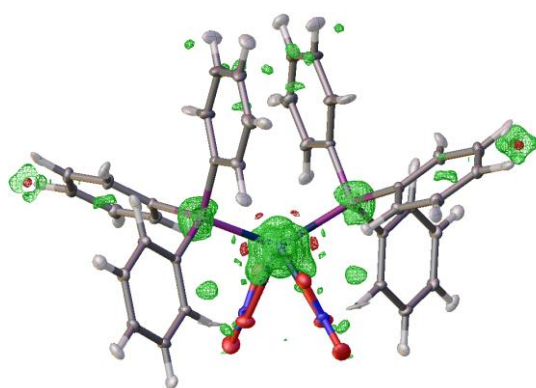
(a) HAR-ELMO, isotropic



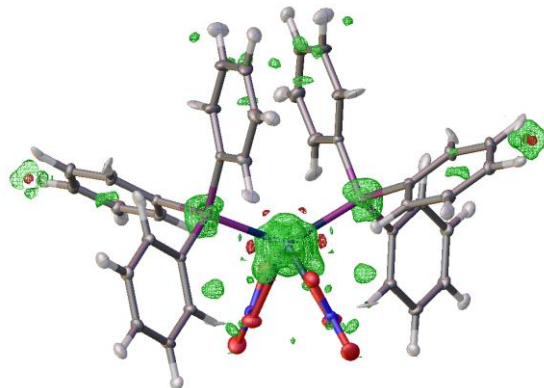
(b) HAR-ELMO, anisotropic



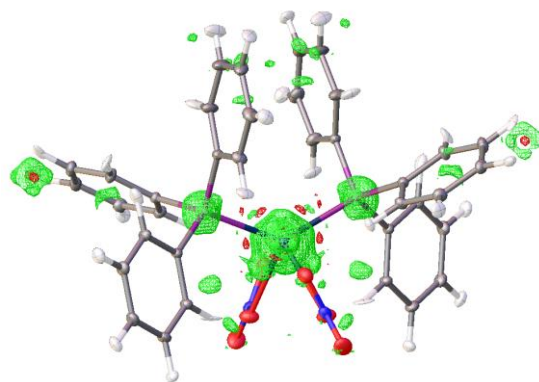
(c) IAM,  $-0.843/+2.072 \text{ e}\text{\AA}^{-3}$



(d) HAR-ELMO,  $-0.680/+1.632 \text{ e}\text{\AA}^{-3}$

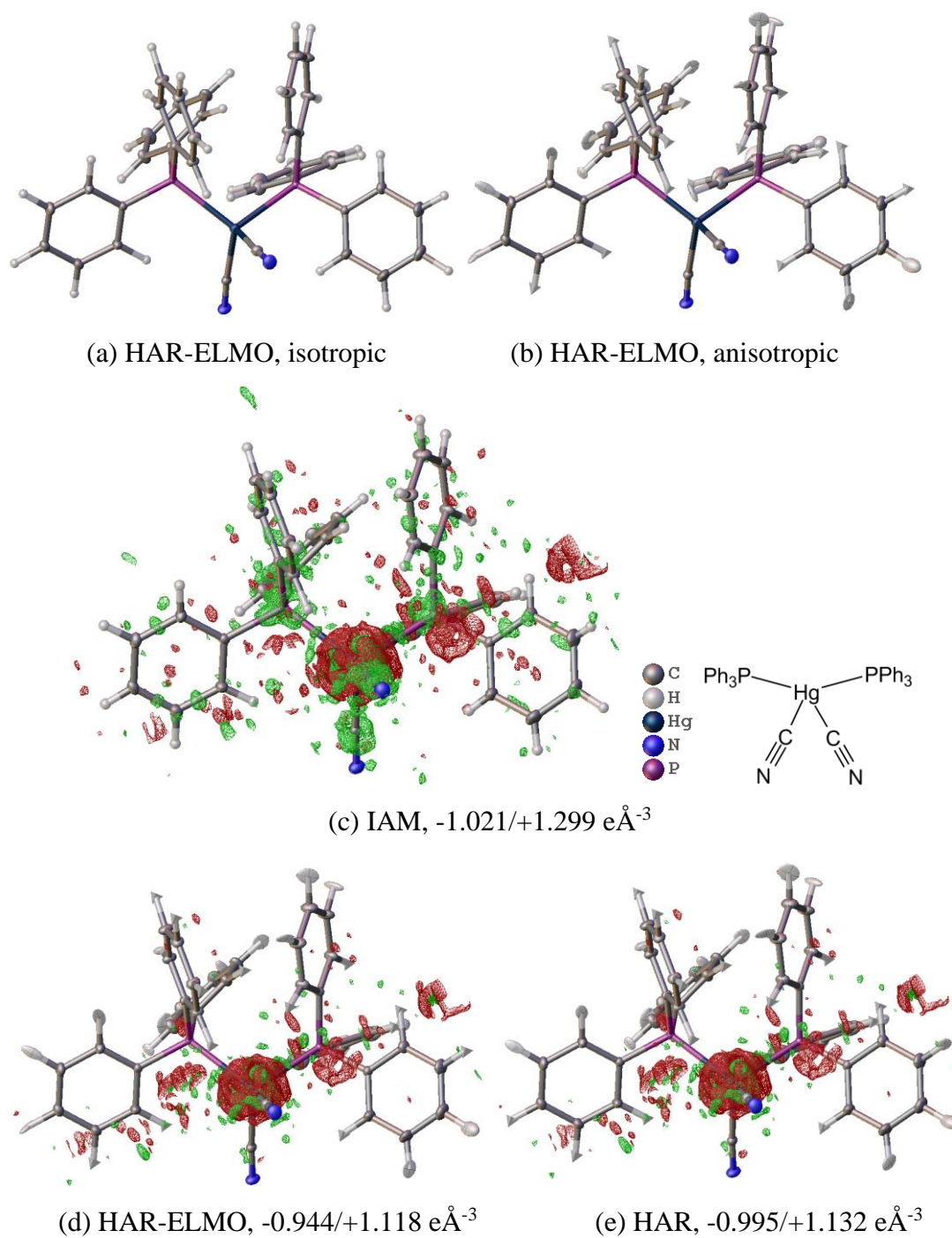


(e) HAR,  $-0.675/+1.672 \text{ e}\text{\AA}^{-3}$



(f) HAR at B3LYP-IOTC,  $-0.805/+1.149 \text{ e}\text{\AA}^{-3}$

**Figure S98:**  $(\text{Ph}_3\text{P})_2\text{Hg}(\text{NO}_3)_2$ . HAR-ELMO molecular structures using (a) isotropic displacement parameters and (b) anisotropic displacement parameters for the hydrogen atoms. (c) Residual density distribution after IAM refinement with minimum and maximum values, (d) after anisotropic HAR-ELMO, (e) after anisotropic HAR at the same level of theory (HF/DZP-DKH), (f) after HAR at B3LYP-IOTC level. Isovalue =  $\pm 0.2 \text{ e}\text{\AA}^{-3}$ , green=positive, red=negative. ADPs at 50% probability level.



**Figure S99:**  $(\text{Ph}_3\text{P})_2\text{Hg}(\text{CN})_2$ . HAR-ELMO molecular structures using (a) isotropic displacement parameters and (b) anisotropic displacement parameters for the hydrogen atoms. (c) Residual density distribution after IAM refinement with minimum and maximum values, (d) after anisotropic HAR-ELMO, (e) after anisotropic HAR at the same level of theory (HF/DZP-DKH). Isovalue =  $\pm 0.2 \text{ e}\text{\AA}^{-3}$ , green=positive, red=negative. ADPs at 50% probability level.

## Graphical visualization software used

Globally, throughout manuscript and supporting information, deformation densities, residual densities, ELI-D and ESPs were visualized using GaussView,<sup>S23</sup> VESTA,<sup>S24</sup> VMD<sup>S25</sup> and Olex2<sup>S26</sup>. For the crambin model (Fig 2a) UCSF Chimera was used.<sup>S27</sup>

## References

- S1. Stoll, H.; Wagenblast, G; Preuss, H. On the Use of Local Basis Sets for Localized Molecular Orbitals. *Theor. Chim. Acta* **1980**, *57*,169–178.
- S2. Philipp, D. M.; Friesner, R. A. Mixed Ab Initio QM/MM Modeling Using Frozen Orbitals and Tests with Alanine Dipeptide and Tetrapeptide. *J. Comput. Chem.* **1999**, *20*, 1468-1494.
- S3. Meyer, B.; Guillot, B.; Ruiz-Lopez, M. F.; Genoni, A. Libraries of Extremely Localized Molecular Orbitals. 1. Model Molecules Approximation and Molecular Orbitals Transferability. *J. Chem. Theory. Comput.* **2016**, *12*, 1052-1067.
- S4. Meyer, B.; Guillot, B.; Ruiz-Lopez, M. F.; Jelsch, C.; Genoni, A. Libraries of Extremely Localized Molecular Orbitals. 2. Comparison with the Pseudoatoms Transferability. *J. Chem. Theory. Comput.* **2016**, *12*, 1068-1081.
- S5. Meyer, B.; Genoni, A. Libraries of Extremely Localized Molecular Orbitals. 3. Construction and Preliminary Assessment of the New Databanks. *J. Phys. Chem. A* **2018**, *122*, 8965-8981.
- S6. Ferré, N.; Assfeld, X.; Rivail, J.-L. Specific Force Field Parameters Determination for the Hybrid Ab Initio QM/MM LSCF Method. *J. Comput. Chem.* **2002**, *23*, 610-624.
- S7. Capelli, S.; Bürgi, H.-B.; Dittrich, B.; Grabowsky, S.; Jayatilaka, D. Hirshfeld atom refinement. *IUCrJ* **2014**, *1*, 361-379.
- S8. Destro, R.; Marsh, R. E.; Bianchi, R. A low-temperature (23 K) study of *L*-alanine. *J. Phys. Chem.* **1998**, *92*, 966–973.
- S9. Capelli, S. C.; Bürgi, H.-B.; Mason, S. A.; Jayatilaka, D. Glycyl-*L*-alanine: a multi-temperature neutron study. *Acta Cryst. C* **2014**, *70*, 949–952.
- S10. Larson, A. C. In *Crystallographic Computing*; Ahmed, F. R., Ed.; Munksgaard: Copenhagen, Denmark, 1970; pp 291-294.
- S11. Fugel, M.; Jayatilaka, D.; Hupf, E.; Overgaard, J.; Hathwar, V. R.; Macchi, P.; Turner, M. J.; Howard, J. A. K.; Dolomanov, O. V.; Puschmann, H.; Iversen, B. B.; Bürgi, H.-B.; Grabowsky, S. Probing the accuracy and precision of Hirshfeld atom refinement with HART interfaced with Olex2. *IUCrJ* **2018**, *5*, 32-44.
- S12. Morgenroth, W.; Overgaard, J.; Clausen, H. F.; Svendsen, H.; Jørgensen, M. R. V.; Larsen, F. K; Iversen, B. B. Helium cryostat synchrotron charge densities determined using a large CCD detector – the upgraded beamline D3 at DESY. *J. Appl. Cryst.* **2008**, *41*, 846–853.

- S13. Jørgensen, M. R. V.; Hathwar, V. R.; Sist, M.; Wang, X.; Hoffmann, C. M.; Briseno, A. L.; Overgaard, J.; Iversen, B. B. Accurate atomic displacement parameters from time-of-flight neutron-diffraction data at TOPAZ. *Acta Cryst. A* **2014**, *70*, 679–681.
- S14. Meindl, K.; Henn, J. Foundations of residual-density analysis. *Acta Cryst. A* **2008**, *64*, 404–418.
- S15. Sawaya, M. R.; Sambashivan, S.; Nelson, R.; Ivanova, M. I.; Sievers, S. A.; Apostol, M. I.; Thompson, M. J.; Balbirnie, M.; Wiltzius, J. J. W.; McFarlane, H. T.; Madsen, A. Ø.; Riek, C.; Eisenberg, D. Atomic structures of amyloid cross- $\beta$  spines reveal varied steric zippers. *Nature* **2007**, *447*, 453–457.
- S16. Case, D. A.; Ben-Shalom, I. Y.; Brozell, S. R.; Cerutti, D. S.; Cheatham, T. E., III; Cruzeiro, V. W.; Darden, T. A.; Duke, R. E.; Ghoreishi, D.; Gilson, M. K.; Gohlke, H.; Goetz, A. W.; Greene, D.; Harris, R.; Homeyer, N.; Izadi, S.; Kovalenko, A.; Kurtzman, T.; Lee, T. S.; LeGrand, S.; Li, P.; Lin, C.; Liu, J.; Luchko, T.; Luo, R.; Mermelstein, D. J.; Merz, K. M.; Miao, Y.; Monard, G.; Nguyen, C.; Nguyen, H.; Omelyan, I.; Onufriev, A.; Pan, F.; Qi, R.; Roe, D. R.; Roitberg, A.; Sagui, C.; Schott-Verdugo, S.; Shen, J.; Simmerling, C. L.; Smith, J.; Salomon-Ferrer, R.; Swails, J.; Walker, R. C.; Wang, J.; Wei, H.; Wolf, R. M.; Wu, X.; Xiao, L.; York, D. M.; Kollman, P. A. *AMBER 2018*, University of California, San Francisco: San Francisco, CA, USA, 2018.
- S17. Pichon-Pesme, V.; Lecomte, C.; Wiest, R.; Bernard, M. Modeling fragments for the *ab initio* determination of electron density in polypeptides. An experimental and theoretical approach to the electron distribution in Leu-enkephalin trihydrate. *J. Am. Chem. Soc.* **1992**, *114*, 2713–2715.
- S18. Jelsch, C.; Teeter, M. M.; Lamzin, V.; Pichon-Pesme, V.; Blessing, R. H.; Lecomte, C. Accurate protein crystallography at ultra-high resolution: valence electron distribution in crambin. *Proc. Natl. Acad. USA* **2000**, *97*, 3171–3176.
- S19. Allen, F. H.; Bruno, I. J. Bond lengths in organic and metal-organic compounds revisited: X-H bond lengths from neutron diffraction data. *Acta Cryst. B* **2010**, *66*, 380–386.
- S20. Turner, M. J.; Grabowsky, S.; Jayatilaka, D.; Spackman, M. Accurate and Efficient Model Energies for Exploring intermolecular Interactions in Molecular Crystals. *J. Phys. Chem. Lett.* **2014**, *5*, 4249–4255.
- S21. Mackenzie, C. F.; Spackman, P. R.; Jayatilaka, D.; Spackman, M. CrystalExplorer model energies and energy frameworks: extension to metal coordination compounds, organic salts, solvates and open-shell systems. *IUCrJ* **2017**, *4*, 575–587.
- S22. Spackman, M. A.; Jayatilaka, D. Hirshfeld surface analysis. *CrystEngComm* **2009**, *11*, 19–32.

- S23. Dennington, R.; Keith, T. A.; Millam, J. M. *GaussView, Version 6*; Semichem Inc.: Shawnee Mission, KS, USA, 2016.
- S24. Momma, K.; Izumi, F. VESTA 3 for three-dimensional visualization of crystal, volumetric and morphology data. *J. Appl. Cryst.* **2011**, *44*, 1272-1276.
- S25. Humphrey, W.; Dalke, A.; Schulten, K. VMD - Visual Molecular Dynamics. *J. Molec. Graphics* **1996**, *14*, 33-38.
- S26. Dolomanov, O. V.; Bourhis, L. J.; Gildea, R. J.; Howard, J. A. K.; Puschmann, H. OLEX2: a complete structure solution, refinement and analysis program *J. Appl. Cryst.* **2009**, *42*, 339-341.
- S27. Pettersen, E. F.; Goddard, T. D.; Huang, C. C.; Couch, G. S.; Greenblatt, D. M.; Meng, E. C.; Ferrin, T. E. UCSF Chimera - a visualization system for exploratory research and analysis. *J Comput Chem.* **2004**, *25*, 1605-1612.