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LUCAS HEIGHTS RESEARCH LABORATORIES

**RESULTS OF PIPE BEND ANALYSIS
PART II: STRESS DISTRIBUTIONS FROM BENDING
FLANGED PIPE ELBOWS**

by

J.F. WHATHAM

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ABSTRACT

Graphs of outside surface stress distributions are presented and numerical values of stresses on inside and outside surfaces tabulated for a wide range of flange-ended pipe elbows subjected to pure in-plane bending; calculations are based on linear thin shell theory.

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PIPES; STRESSES; STRESS ANALYSIS; FLANGES

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1. INTRODUCTION

An analysis of flange-ended pipe elbows subjected to pure in-plane bending, supported by experiment, has been published [Whatham 1979] and the detailed analysis given [Whatham 1982].

The objective of this report is to present the surface stress distributions for a range of flanged elbows to assist pipework design engineers and to provide analytic solutions for checking numerical solution methods. Wall thicknesses vary from 1 to 10 per cent of the pipe radius with bend radii two, three and five times the pipe radius.

Stresses were calculated by the thin shell theory of Novozhilov [1970] with the assumptions that:

- (i) the pipe wall is thin ($t/r < 0.3$),
- (ii) normal stresses through the wall are negligible,
- (iii) normals through the wall remain normal to it and unchanged in length, and
- (iv) the flanges are infinitely stiff.

2. STRESS DERIVATION

The flanged pipe elbow configuration is shown in Figure 1. An element of the elbow middle surface, an imaginary surface mid-way between the inner and outer surfaces, is shown in Figure 2 and is supposed to have forces T_θ , T_η , $T_{\theta\eta}$, $T_{\eta\theta}$, N_θ , N_η and moments M_θ , M_η , $M_{\eta\theta}$, $M_{\theta\eta}$ per unit length acting on its edges. The solution was obtained by thin shell theory in terms of these forces and moments; the stresses presented in this report were then derived as follows:

$$\text{Hoop stress: } \sigma_{\theta\theta} = T_\theta/t + 12zM_\theta/t^3$$

$$\text{Axial stress: } \sigma_{\eta\eta} = T_\eta/t + 12zM_\eta/t^3 \quad (1)$$

$$\text{Shear stress: } \sigma_{n\theta} = S/t + z(12H/t^3 - S/rt) \quad (1) \text{ cont'd}$$

where

$$S = T_{\theta n} - M_{n\theta}/r_n = T_{n\theta} - M_{\theta n}/r,$$

and

$$H = M_{\theta n} = M_{n\theta} \quad .$$

These stresses were close to those derived from beam theory when considering a straight pipe subjected to bending or torsion; if a moment M is applied to a straight pipe, Novozhilov's theory gives [see Whatham 1981]

$$\begin{aligned} T_n &= \frac{12M \cos \theta}{(12+\gamma)\pi r^2} \\ M_n &= \frac{\gamma M \cos \theta}{(12+\gamma)\pi r} \\ T_\theta &= M_\theta = S = H = 0 \end{aligned} \quad (2)$$

where $\gamma = (t/r)^2$.

Substituting in Equations (1), the axial stress distribution approximates that from beam theory, which is

$$\sigma_{nn} = \frac{M(r+z)\cos \theta}{\pi r^3 t(1+\gamma/4)} \quad . \quad (3)$$

If torque T is applied to a straight pipe, Novozhilov's theory gives

$$\begin{aligned} S &= \frac{3T}{2(3+\gamma)\pi r^2} \\ H &= \frac{\gamma T}{4(3+\gamma)\pi r} \end{aligned} \quad (4)$$

$$T_n = M_n = T_\theta = M_\theta = 0 \quad .$$

Substituting in Equations (1), the shear stress distribution approximates that from beam theory, given by

$$\sigma_{n\theta} = \frac{T(r+z)}{2\pi r^3 t(1+\gamma/4)} \quad . \quad (5)$$

Equations (1) assume that the strains are linearly distributed through the pipe wall; this is not true for curved shells and the stresses $\sigma'_{\theta\theta}$, $\sigma'_{\eta\eta}$, $\sigma'_{\eta\theta}$ derived by the following equations are theoretically more accurate, even though the results do not agree with beam theory in the case of straight pipes:

$$\begin{aligned}\sigma'_{\theta\theta} &= \sigma_{\theta\theta} - z(A+vB)/(1-\nu^2) \\ \sigma'_{\eta\eta} &= \sigma_{\eta\eta} - z(B+vA)/(1-\nu^2) \\ \sigma'_{\eta\theta} &= \sigma_{\eta\theta} - \frac{z}{2r} \left[(r/(r+z) + r/(r_\eta+z))\sigma_{\eta\theta} - (r_\eta-r)\bar{\sigma}_{\eta\theta} / (r_\eta+z) \right]\end{aligned}\quad (6)$$

where

$$\begin{aligned}A &= (\sigma_{\theta\theta} - \nu\sigma_{\eta\eta}) / (r+z), \\ B &= (\sigma_{\eta\eta} - \nu\sigma_{\theta\theta}) / (r_\eta+z), \quad \text{and} \\ \bar{\sigma}_{\eta\theta} &= \frac{1}{2}\sigma_{\eta\theta} \text{ (inside)} + \frac{1}{2}\sigma_{\eta\theta} \text{ (outside)}.\end{aligned}$$

3. ELBOW CONFIGURATION AND RESULTS

Because of symmetry, stresses had only to be calculated for one side of the bend in Figure 1 ($\theta = 0-180^\circ$) and from flange to mid-bend ($\phi = 0-45^\circ$). Stresses acting in the hoop and axial directions on the outside surface are plotted in Appendix A, together with the stresses on theoretically unterminated pipe bends, in which case they are independent of ϕ . The maxima and minima of the latter curves are given by the floating numbers.

The two graphs for each pipe bend are accompanied by tabulated stresses from which the graphs were constructed. In addition, since shear stresses and inside surface stresses are also given and a linear variation through the wall is assumed, the complete stress state in each pipe bend is provided.

A computer program package BENDPAC, written in FORTRAN IV and ASSEMBLER for an IBM3031 computer and designed to calculate the stresses in and the flexibility of flanged pipe elbows under in-plane or out-of-plane loading, is available from either the Australian Atomic Energy Commission or the National Energy Software Center, Argonne National Laboratory, USA.

4. REFERENCES

- Novozhilov, V.V. [1970] - Thin Shell Theory. 2nd Augmented and Revised Edition, Wolters-Noordhoff, Gröningen, The Netherlands.
- Whatham, J.F. [1979] - In-plane bending of flanged pipe elbows. Trans. Inst. Eng. Aust., CE 21(2)80.
- Whatham, J.F. [1981] - Thin shell equations for circular pipe bends. J. Nucl. Eng. Des., 65(1)77.
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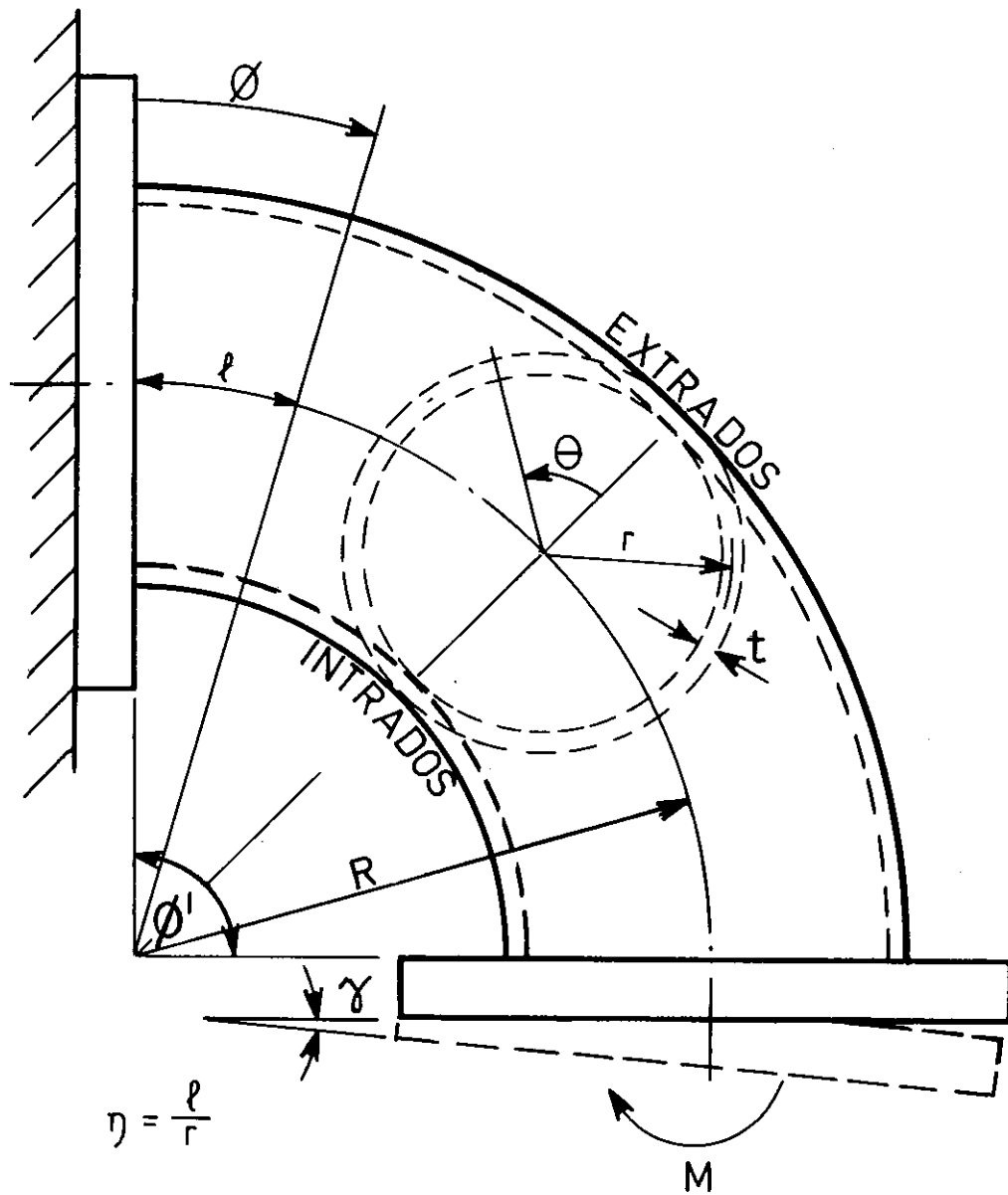


FIGURE 1. PIPE BEND CONFIGURATION

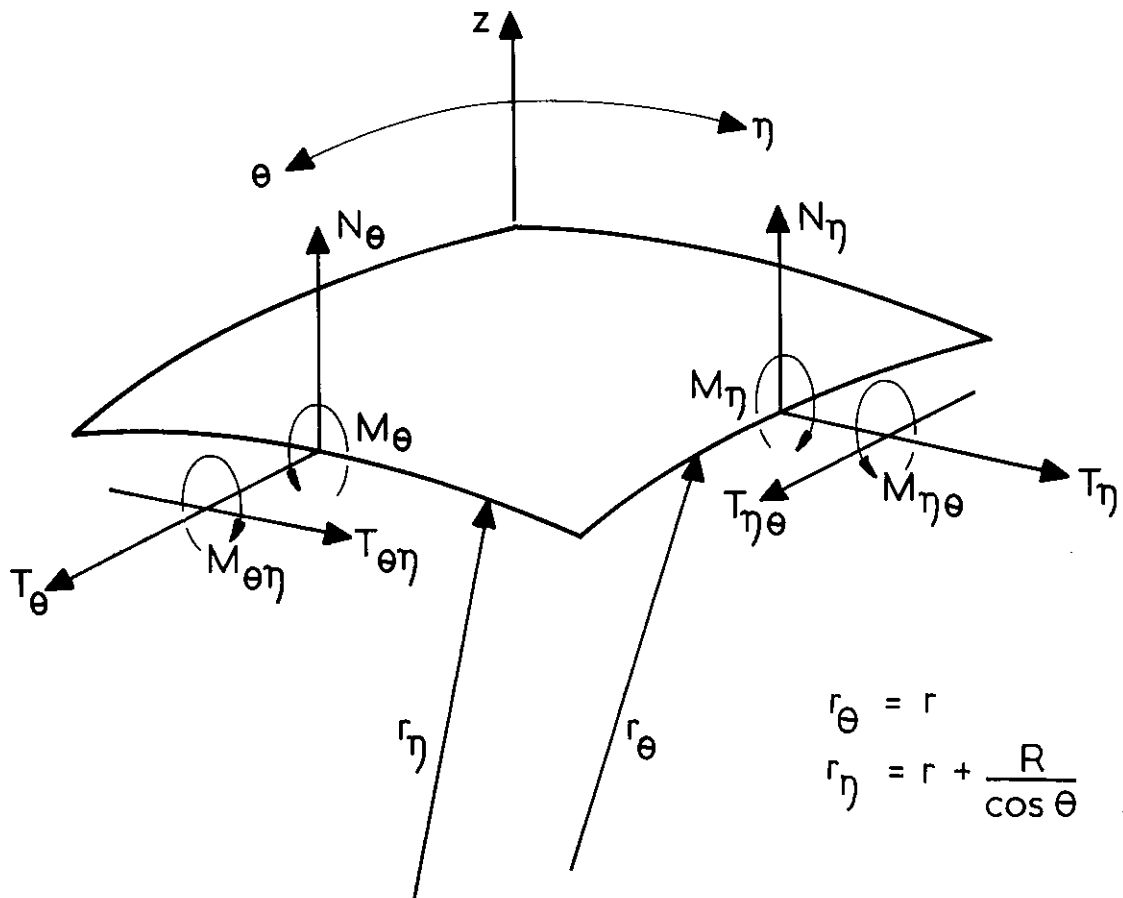


FIGURE 2. ELEMENT OF PIPE MIDDLE SURFACE

APPENDIX A
STRESSES IN FLANGED PIPE ELBOWS IN PURE BENDING

Parameters of pipe elbows considered:

$$R/r = 2, 3, 5$$

$$t/r = 0.01, 0.02, 0.05, 0.1$$

$$\nu = 0.3$$

$$\text{Stress factor} = \text{stress} \cdot \pi r^2 t / M$$

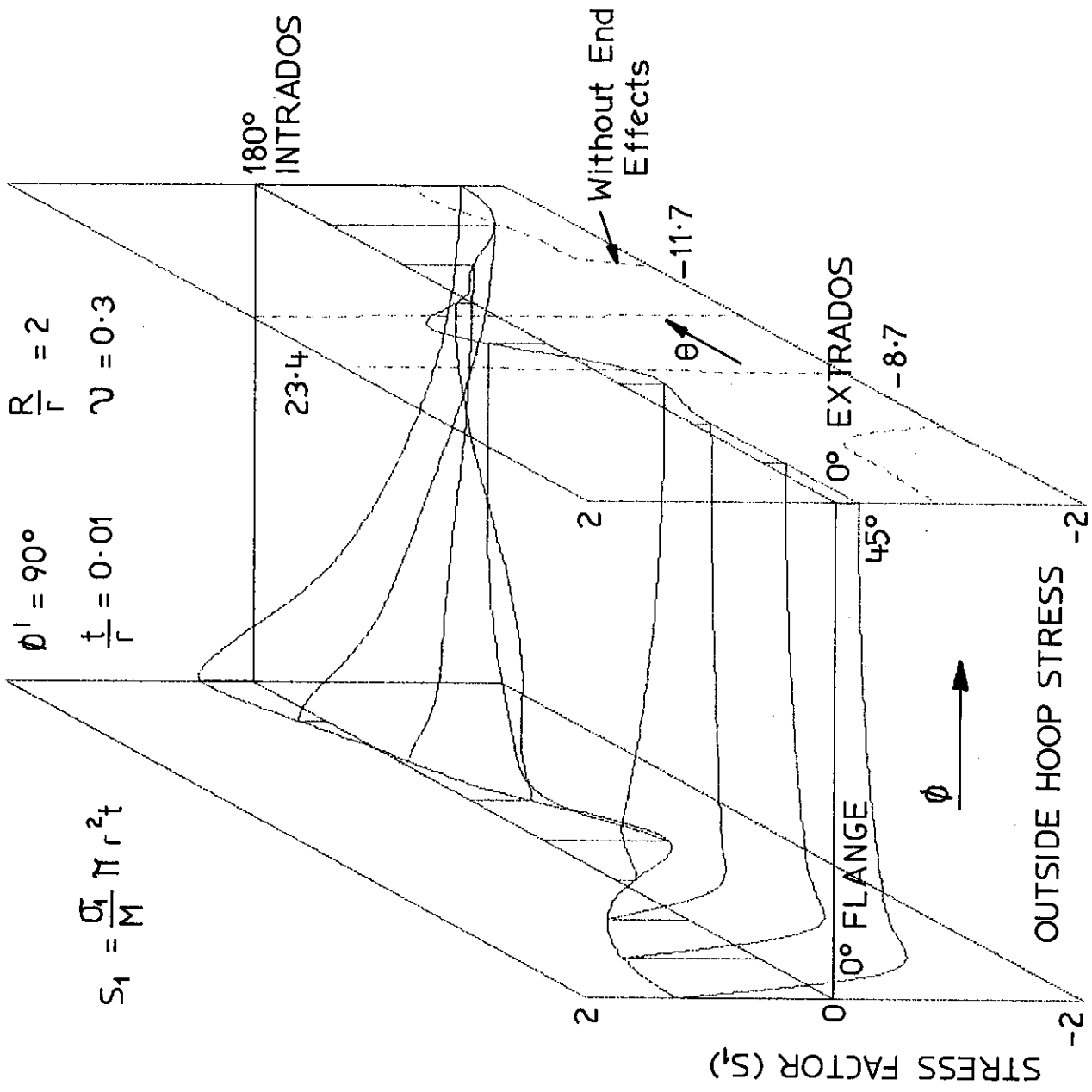


FIGURE A1

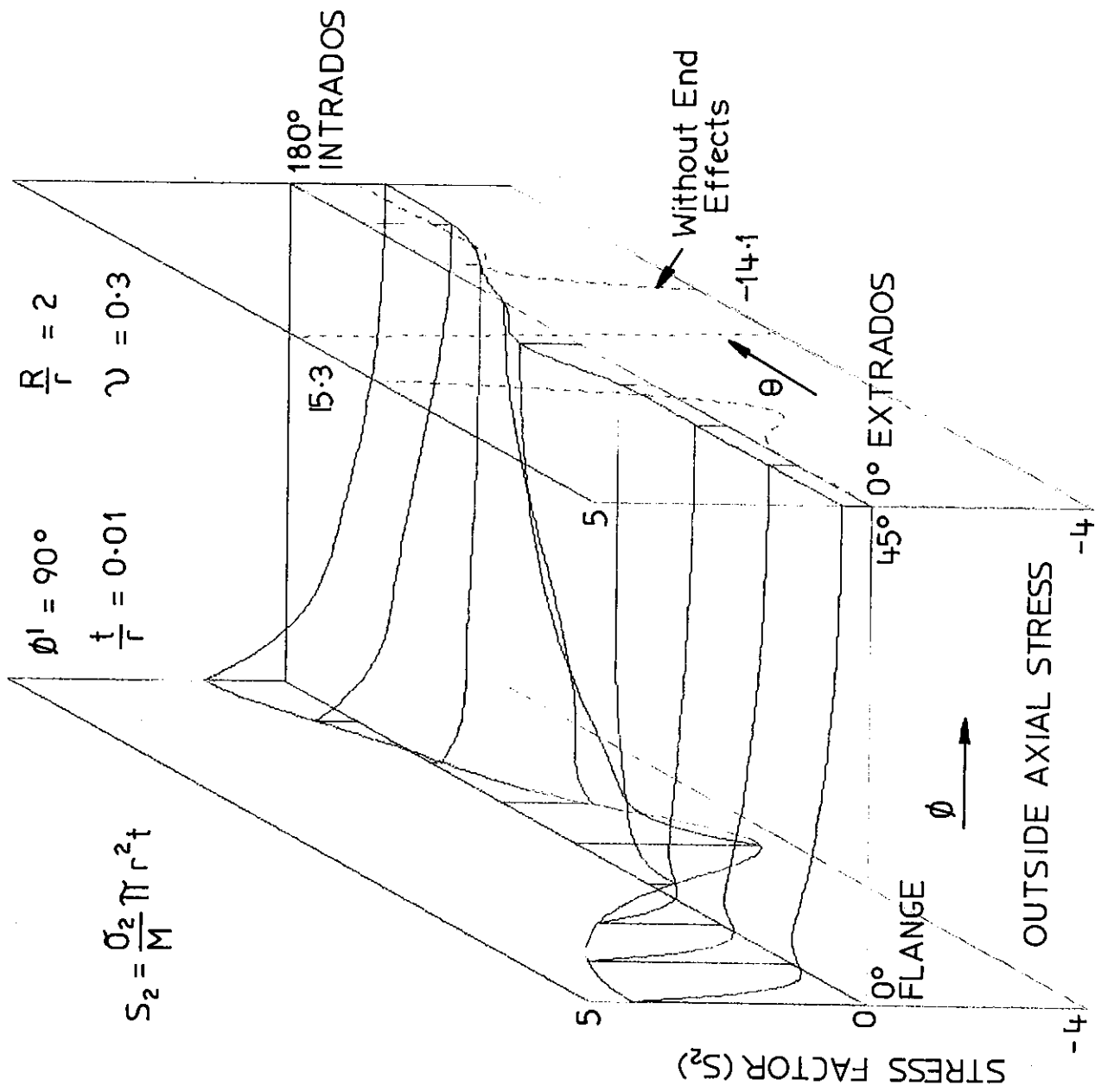


FIGURE A2

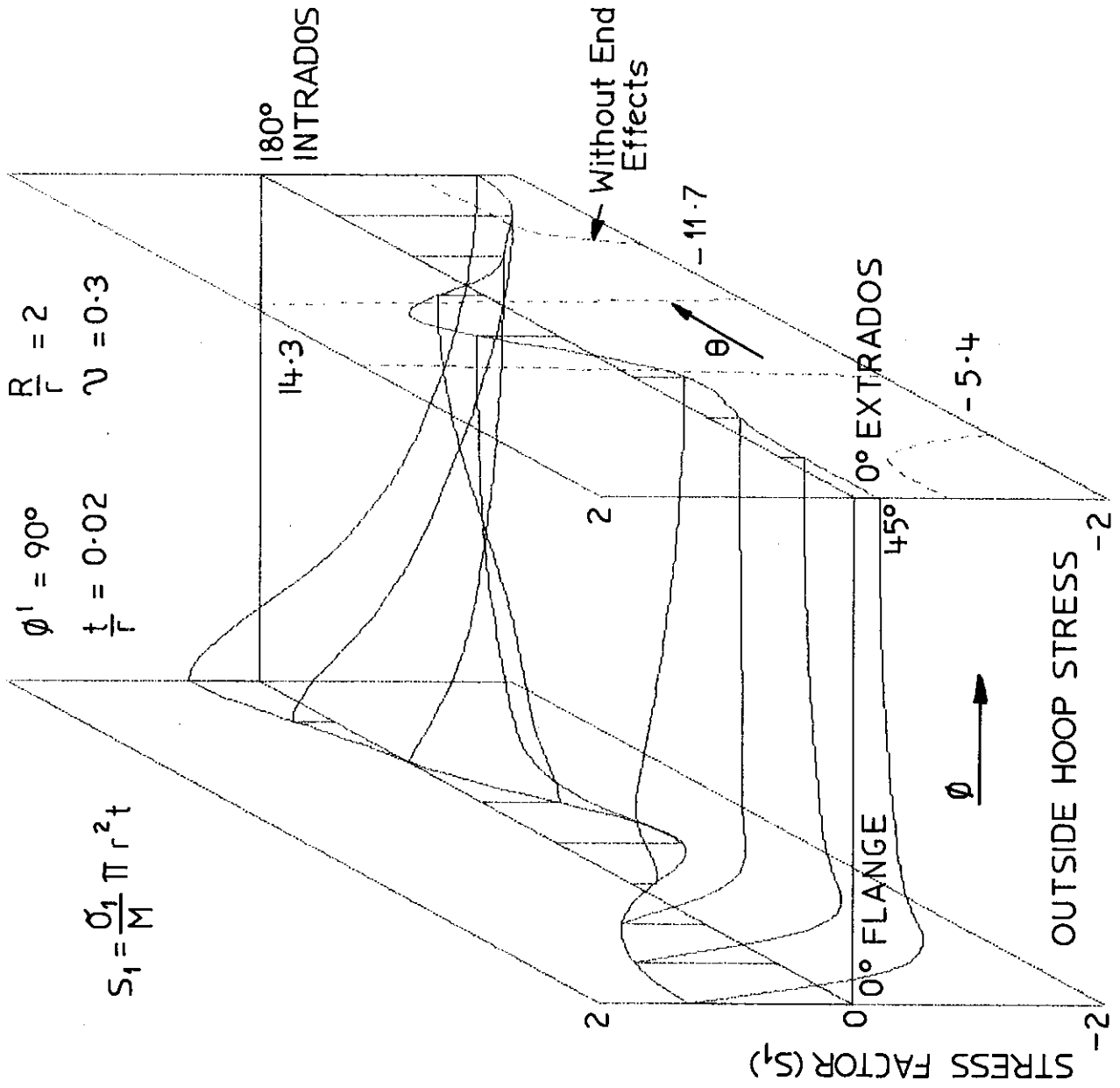


FIGURE A3

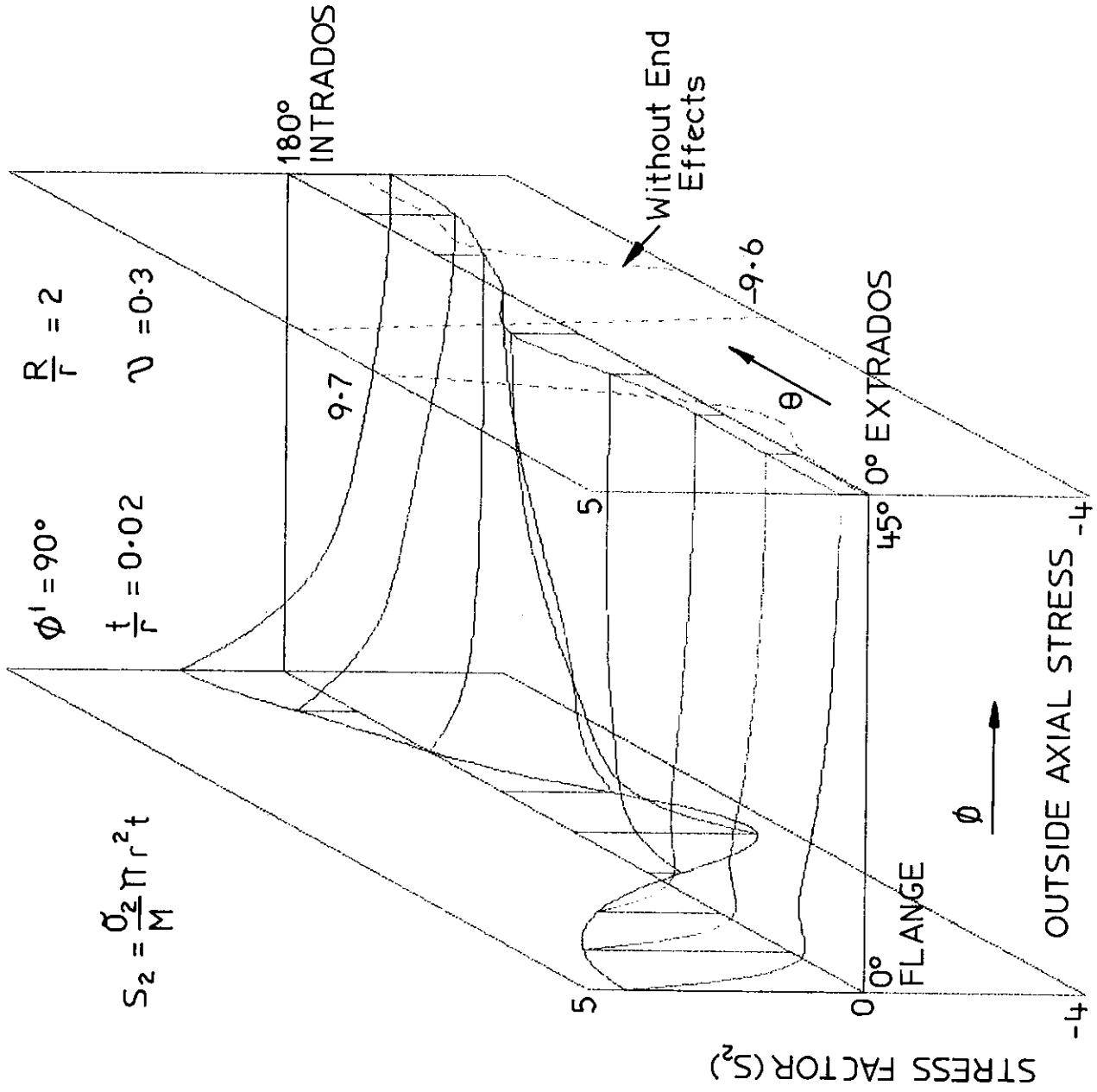


FIGURE A4

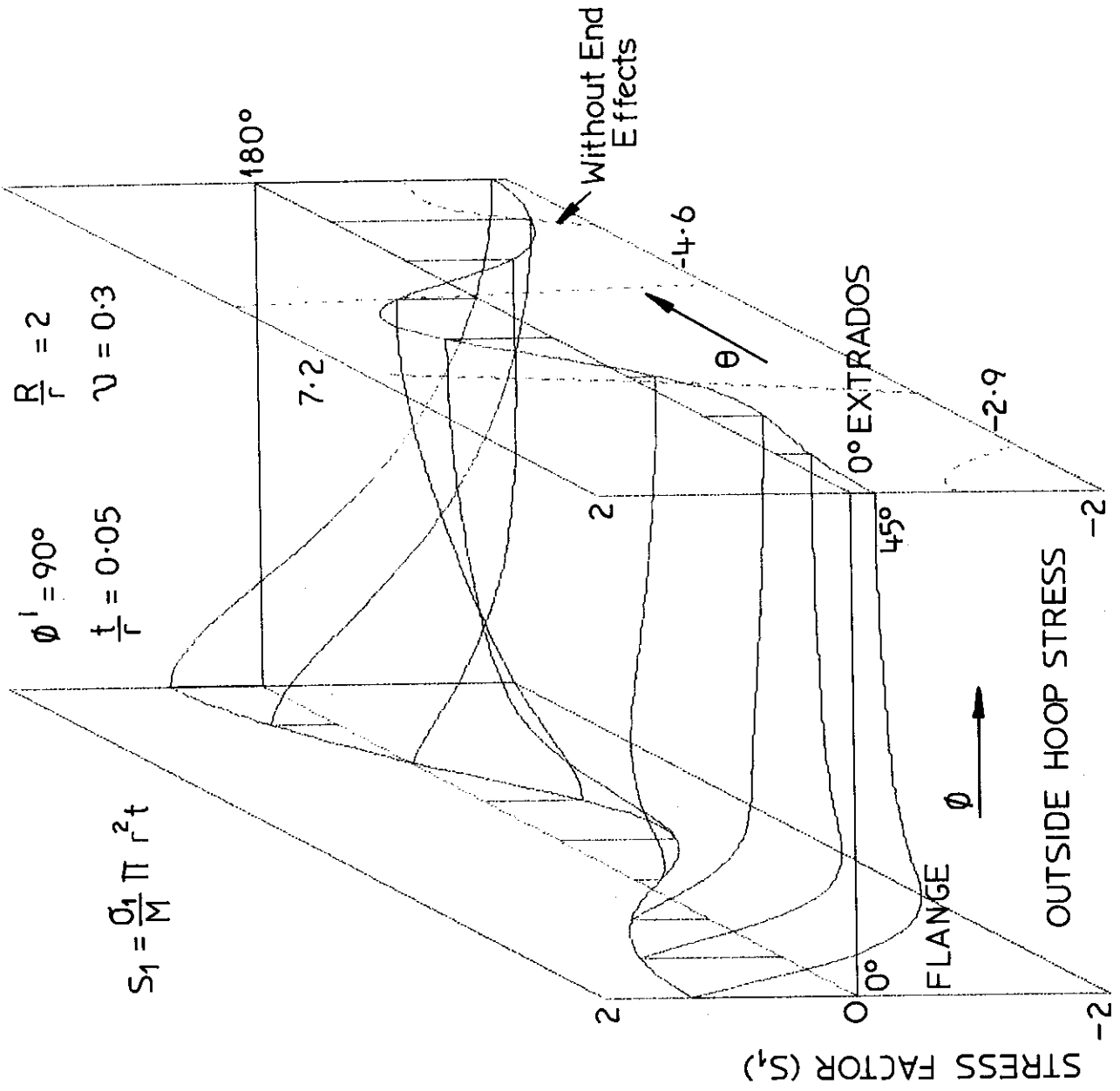


FIGURE A5

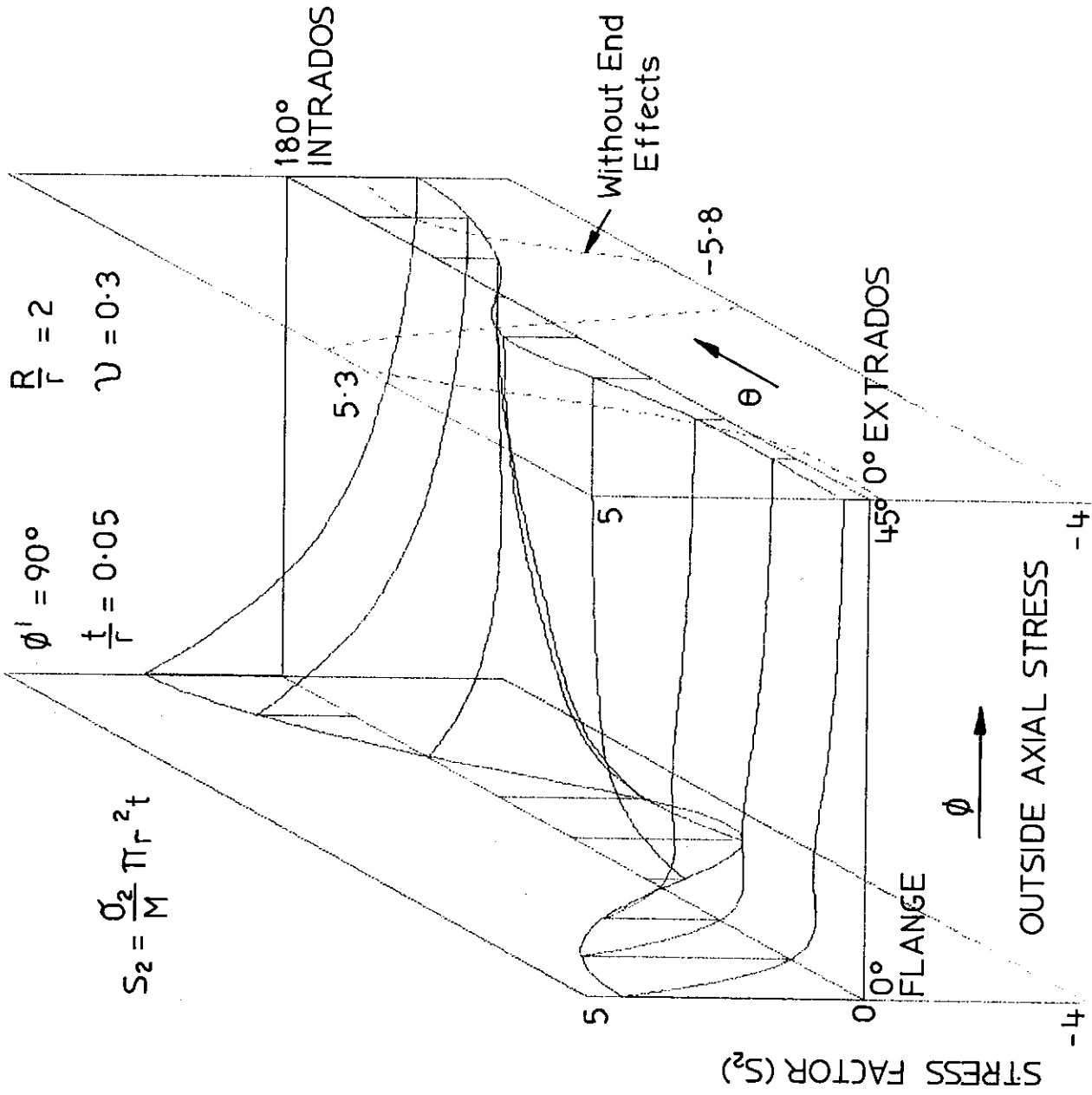


FIGURE A6

TABLE A6

R/r = 2.0 t/r = 0.05

THETA	PHI=0.0	INSIDE HOOP STRESS FACTORS					35.0	40.0	45.0	WITHOUT END EFFECTS
		15.0	20.0	25.0	30.0	35.0				
180.0	-0.6240	-0.3460	-0.5430	-0.7238	-0.8611	-0.9522	-1.0028	-1.0189	1.0297	
157.5	-0.6403	-0.2901	-0.3744	-0.4266	-0.4442	-0.4405	-0.4309	-0.4265	1.5491	
135.0	-0.3827	-0.0023	0.0416	0.0711	0.0927	0.1081	0.1173	0.1204	4.6040	
112.5	0.0161	-0.3336	-0.4583	-0.6085	-0.7473	-0.8554	-0.9233	-0.9464	-1.8869	
90.0	0.3317	-0.6541	-0.7733	-0.8828	-0.9642	-1.0171	-1.0464	-1.0558	-9.2749	
67.5	0.2129	-0.1976	-0.1345	-0.0798	-0.0289	0.0135	0.0414	0.0511	-1.9492	
45.0	-0.0678	-0.0254	0.0647	0.1302	0.1798	0.2157	0.2373	0.2445	2.8487	
22.5	-0.2586	-0.1725	-0.1098	-0.0743	-0.0520	-0.0373	-0.0290	-0.0263	1.7640	
-0.0	-0.3200	-0.2486	-0.1912	-0.1620	-0.1451	-0.1341	-0.1280	-0.1260	0.8654	

THETA	PHI=0.0	INSIDE AXIAL STRESS FACTORS					35.0	40.0	45.0	WITHOUT END EFFECTS
		15.0	20.0	25.0	30.0	35.0				
180.0	-2.7467	-0.5335	-0.4387	-0.4611	-0.5186	-0.5707	-0.6033	-0.6141	1.1249	
157.5	-2.1343	-0.4606	-0.4046	-0.4249	-0.4627	-0.4932	-0.5106	-0.5160	1.6202	
135.0	-1.2757	-0.5103	-0.4978	-0.5076	-0.5213	-0.5315	-0.5369	-0.5385	1.5266	
112.5	0.0537	-0.8051	-0.7093	-0.6393	-0.5949	-0.5666	-0.5500	-0.5444	-3.1149	
90.0	1.1057	-0.3108	-0.0758	0.0882	0.2005	0.2769	0.3224	0.3376	-2.2038	
67.5	0.7096	0.5001	0.6479	0.7420	0.8015	0.8400	0.8620	0.8692	2.1155	
45.0	-0.2259	0.8068	0.7697	0.7363	0.7035	0.6783	0.6628	0.6576	1.6092	
22.5	-0.6619	0.8563	0.7291	0.6382	0.5665	0.5166	0.4875	0.4780	0.0641	
-0.0	-1.0668	0.8686	0.7240	0.6229	0.5450	0.4920	0.4616	0.4517	-0.3164	

THETA	PHI=0.0	INSIDE SHEAR STRESS FACTORS					35.0	40.0	45.0	WITHOUT END EFFECTS
		15.0	20.0	25.0	30.0	35.0				
180.0	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0	
157.5	-0.6652	-0.9270	-0.8880	-0.7885	-0.6383	-0.4486	-0.2313	-0.0000	0.0	
135.0	-0.8096	-1.1903	-1.0796	-0.9133	-0.7113	-0.4860	-0.2464	-0.0000	0.0	
112.5	-0.5370	-0.5414	-0.3860	-0.2625	-0.1688	-0.0986	-0.0450	0.0000	0.0	
90.0	0.0369	0.4356	0.4361	0.3936	0.3208	0.2260	0.1166	0.0000	0.0	
67.5	0.5518	0.7577	0.6252	0.4975	0.3719	0.2473	0.1235	-0.0000	0.0	
45.0	0.6635	0.5454	0.4179	0.3136	0.2237	0.1438	0.0704	-0.0000	0.0	
22.5	0.4150	0.2538	0.1879	0.1364	0.0947	0.0596	0.0288	-0.0000	0.0	
-0.0	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	0.0000	0.0	

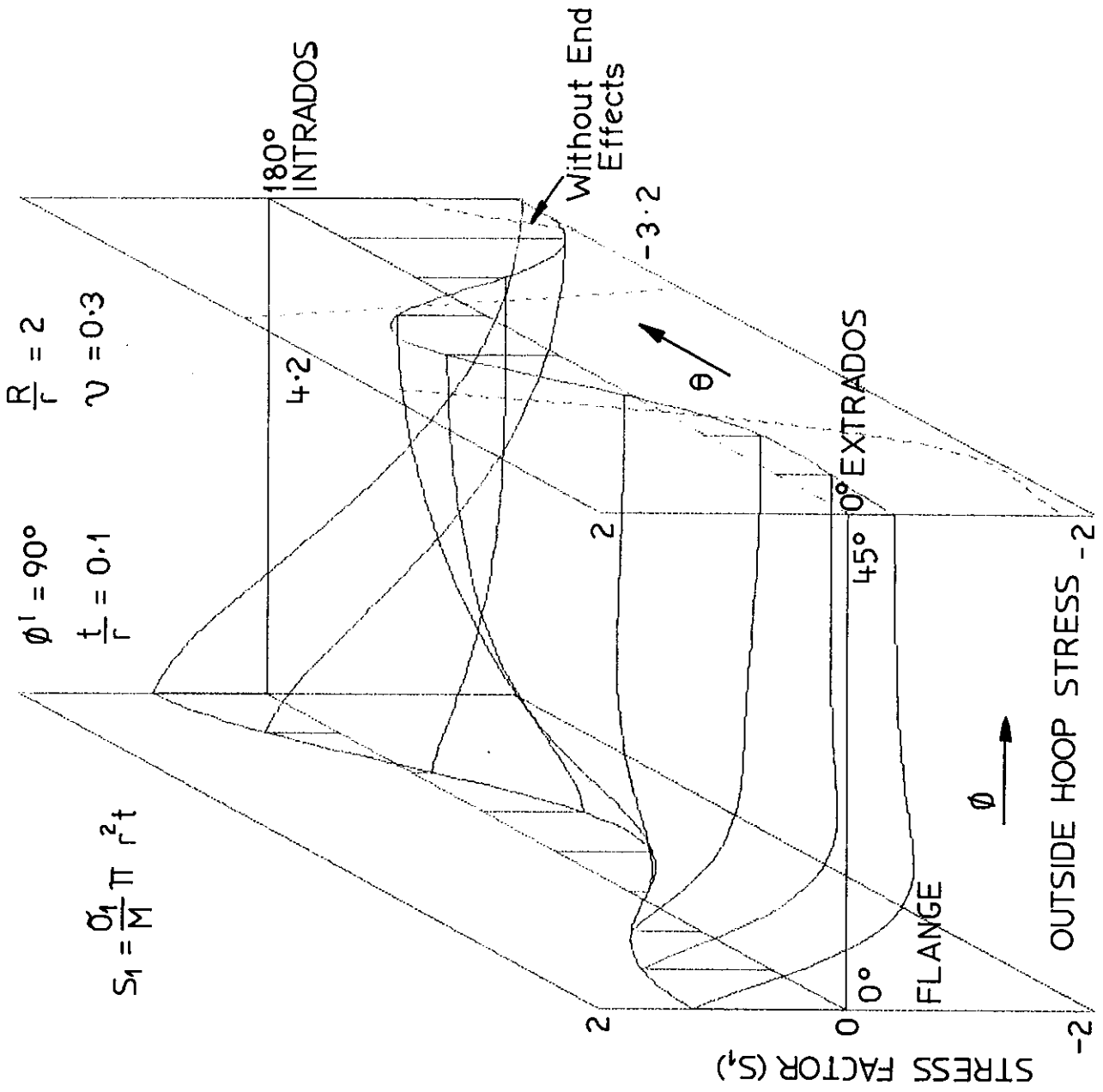


FIGURE A7

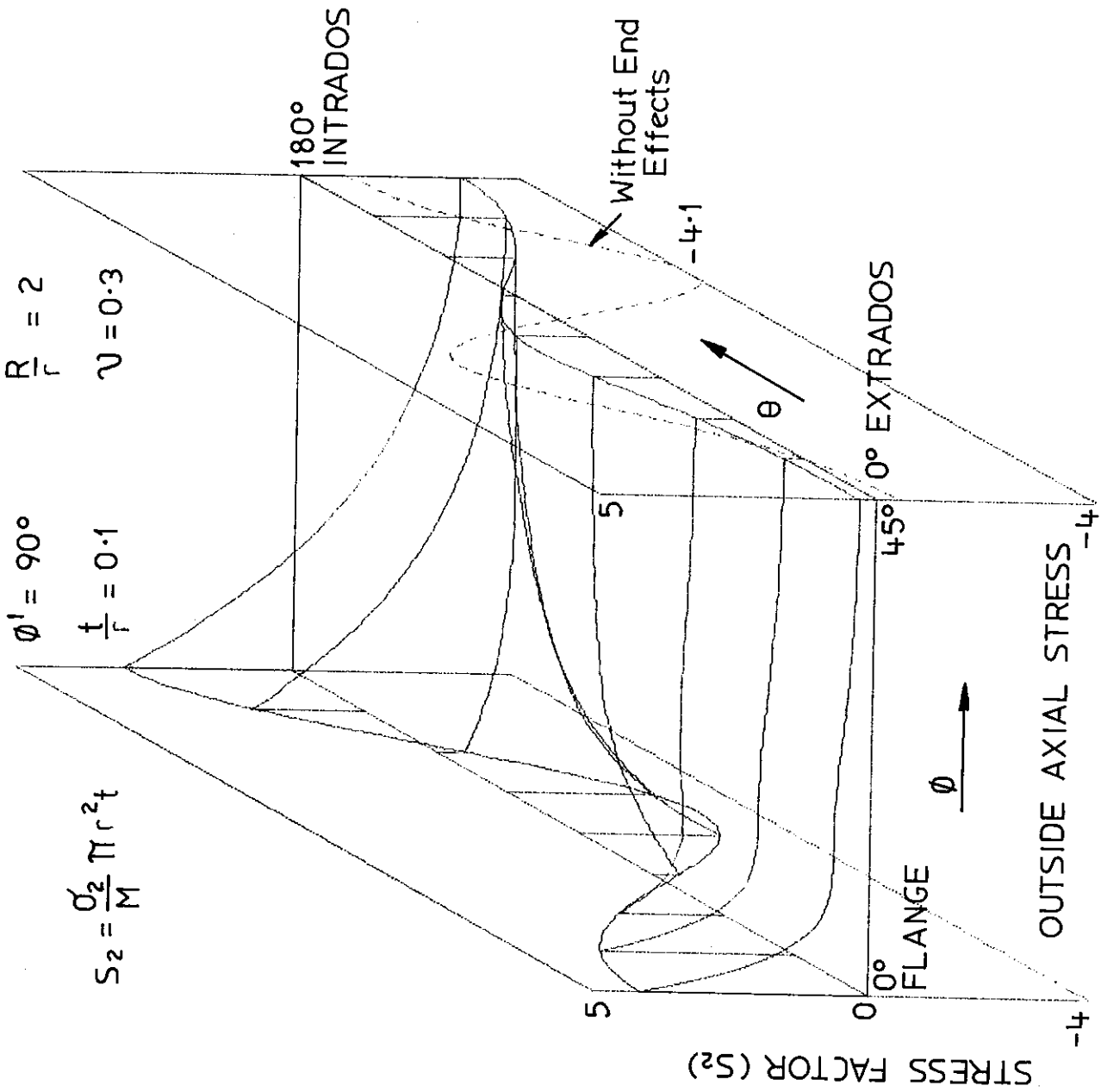


FIGURE A8

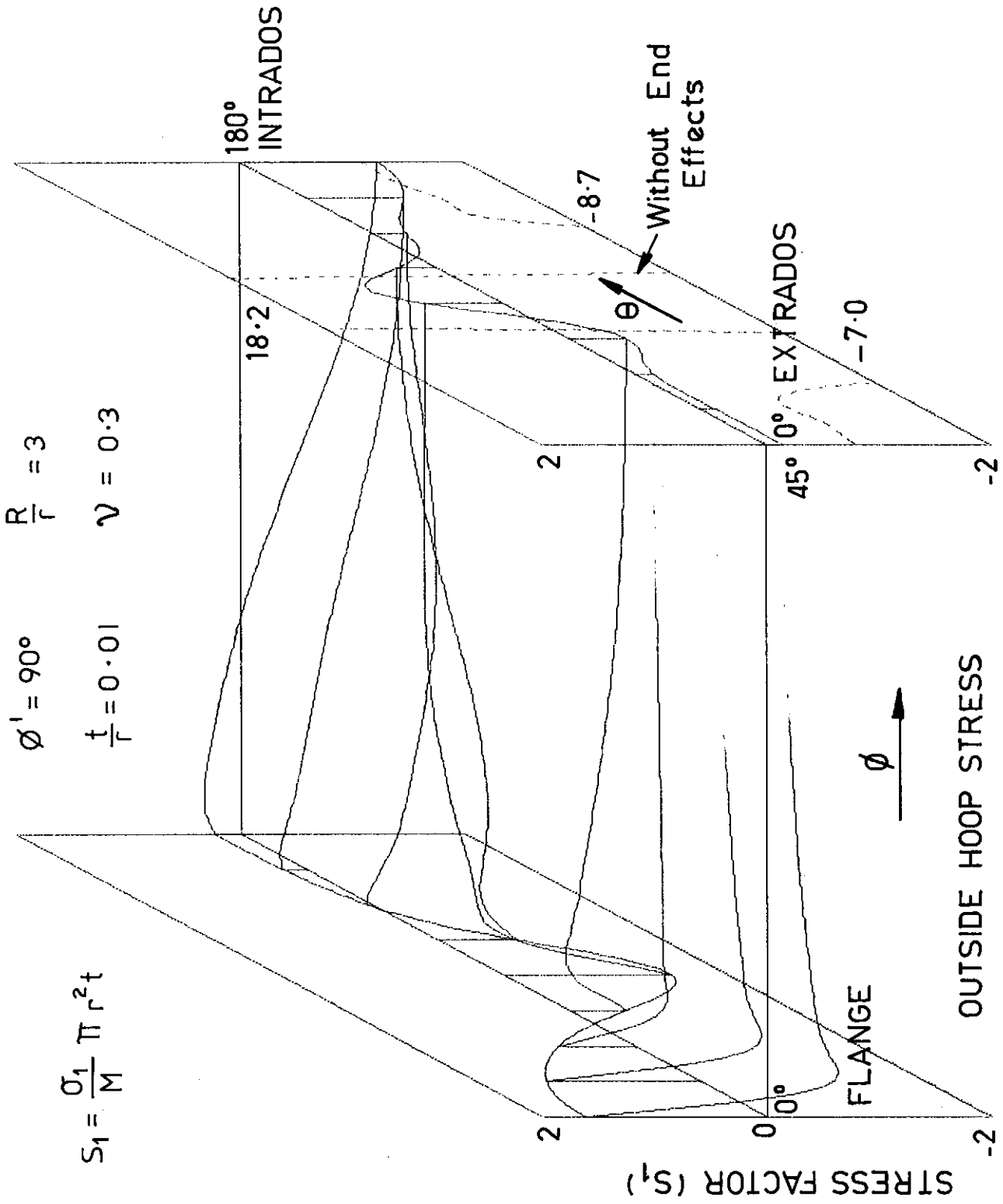


FIGURE A9

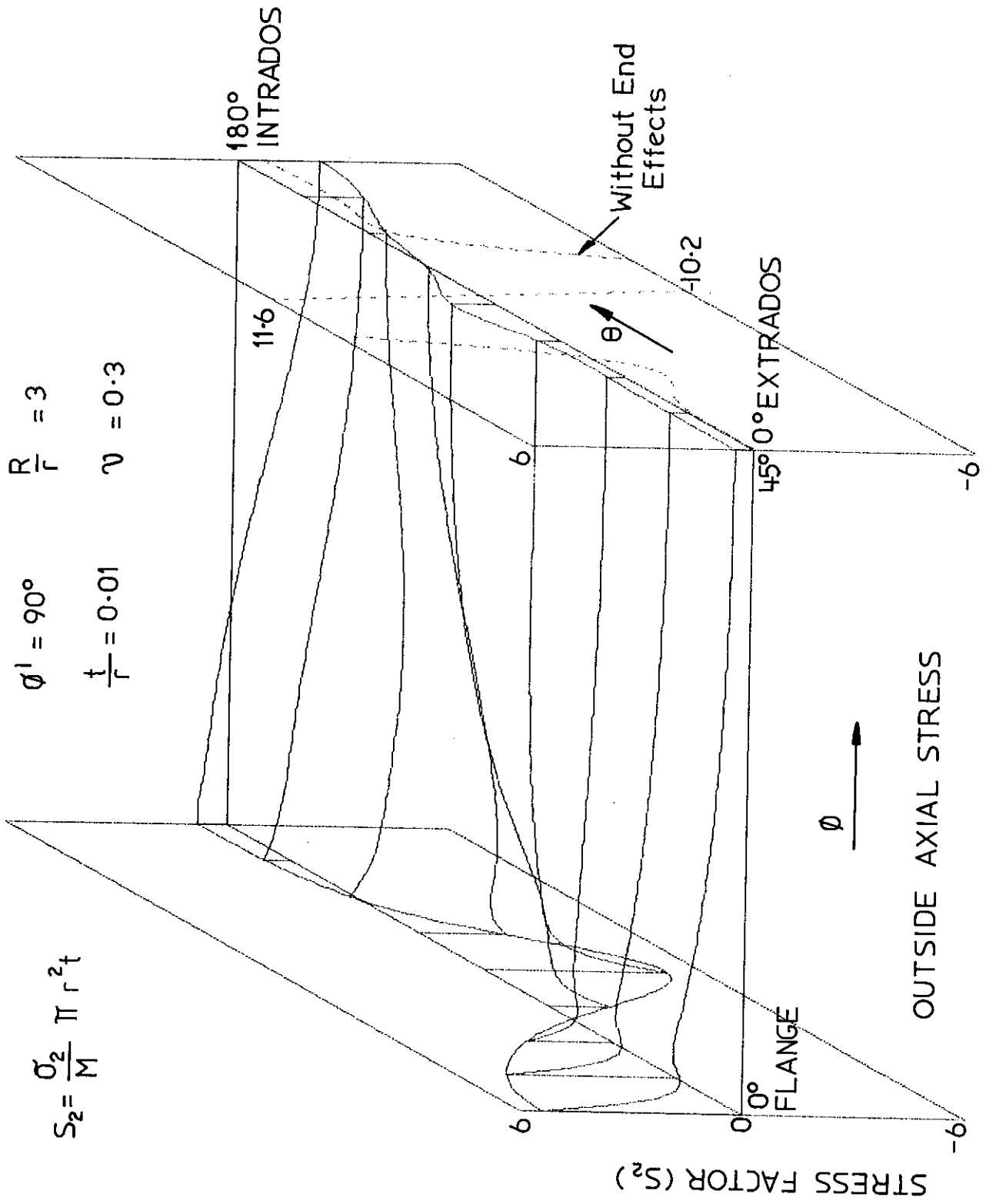


FIGURE A10

TABLE A9

R/r = 3.0 t/r = 0.01

THETA	PHI=0.0	OUTSIDE HOOP STRESS FACTORS							WITHOUT END EFFECTS		
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	
180.0	0.2402	0.2952	0.1593	-0.0156	-0.2383	-0.4933	-0.7569	-0.9931	-1.1592	-1.2192	-1.0451
157.5	0.2252	0.1081	-0.0194	-0.1531	-0.3130	-0.4845	-0.6450	-0.7722	-0.8521	-0.8791	-1.1496
135.0	0.0488	-0.2333	-0.3826	-0.5045	-0.5703	-0.5632	-0.4993	-0.4132	-0.3430	-0.3162	-2.8711
112.5	-0.6931	-0.3931	-0.4342	-0.3396	-0.1815	-0.0074	0.1472	0.2634	0.3338	0.3572	-6.2355
90.0	-1.4875	0.2584	0.4167	0.5737	0.6659	0.7063	0.7130	0.7038	0.6926	0.6879	18.1680
67.5	-0.5023	0.0076	-0.1316	-0.2439	-0.3378	-0.4091	-0.4591	-0.4909	-0.5083	-0.5138	-4.4420
45.0	0.6880	-0.2477	-0.2362	-0.2271	-0.2143	-0.2009	-0.1890	-0.1799	-0.1743	-0.1724	-3.3085
22.5	1.3869	-0.4258	-0.3328	-0.2736	-0.2285	-0.1949	-0.1706	-0.1541	-0.1446	-0.1415	-0.8132
-0.0	1.6240	-0.4953	-0.3781	-0.3043	-0.2504	-0.2114	-0.1837	-0.1653	-0.1548	-0.1513	-0.8527

THETA	PHI=0.0	OUTSIDE AXIAL STRESS FACTORS							WITHOUT END EFFECTS		
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	
180.0	0.8005	0.5732	0.3202	-0.0131	-0.4290	-0.9003	-1.3829	-1.8106	-2.1082	-2.2151	-0.7180
157.5	0.7508	0.2065	-0.0461	-0.3480	-0.6769	-0.9978	-1.2733	-1.4774	-1.5996	-1.6399	-0.7955
135.0	0.1628	-0.6833	-0.9499	-1.1296	-1.1629	-1.0658	-0.8907	-0.7037	-0.5644	-0.5132	-0.6012
112.5	-2.3102	-2.0297	-1.9201	-1.5836	-1.1663	-0.7510	-0.3930	-0.1237	0.0419	0.0975	-9.7407
90.0	-4.9585	-1.4781	-0.6786	-0.0098	0.4720	0.8002	1.0101	1.1342	1.1979	1.2174	6.0826
67.5	-1.6743	0.0858	0.4097	0.5828	0.6549	0.6718	0.6630	0.6466	0.6332	0.6282	5.8509
45.0	2.2935	1.1084	0.9817	0.8554	0.7406	0.6446	0.5699	0.5169	0.4853	0.4749	-1.1844
22.5	4.6230	1.6769	1.3161	1.0585	0.8671	0.7268	0.6268	0.5600	0.5216	0.5090	-0.0773
-0.0	5.4134	1.8486	1.4038	1.1010	0.8838	0.7288	0.6205	0.5492	0.5086	0.4954	-0.0455

THETA	PHI=0.0	OUTSIDE SHEAR STRESS FACTORS							WITHOUT END EFFECTS		
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	
180.0	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0
157.5	-0.3648	-0.4716	-0.5870	-0.6793	-0.7216	-0.6966	-0.5998	-0.4392	-0.2318	-0.0000	0.0
135.0	-0.7650	-0.8822	-0.9146	-0.8696	-0.7686	-0.6342	-0.4830	-0.3244	-0.1627	-0.0000	0.0
112.5	-0.9904	-0.8236	-0.5838	-0.3900	-0.2461	-0.1455	-0.0794	-0.0387	-0.0151	-0.0000	0.0
90.0	-0.3366	-0.0560	0.1088	0.1983	0.2356	0.2335	0.2013	0.1466	0.0770	0.0000	0.0
67.5	0.8056	0.8415	0.7224	0.6085	0.4970	0.3896	0.2869	0.1886	0.0934	-0.0000	0.0
45.0	1.0781	0.9279	0.7034	0.5336	0.4006	0.2940	0.2061	0.1309	0.0636	-0.0000	0.0
22.5	0.6782	0.5370	0.3868	0.2813	0.2044	0.1464	0.1008	0.0632	0.0305	-0.0000	0.0
-0.0	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	0.0000	0.0

TABLE A10

R/r = 3.0 t/r = 0.01

THETA	PHI=0.0	INSIDE HOOP STRESS FACTORS							WITHOUT END EFFECTS						
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	50.0	55.0	60.0		
180.0	0.1603	0.2154	0.0827	-0.0573	-0.2121	-0.3722	-0.5185	-0.6320	-0.7019	-0.7251	-0.7251	1.0445	1.0445		
157.5	0.0195	0.0872	-0.0570	-0.1843	-0.2893	-0.3561	-0.3881	-0.3988	-0.4007	-0.4006	-0.4006	1.1489	1.1489		
135.0	-0.2575	-0.1530	-0.1764	-0.1128	-0.0359	0.0192	0.0409	0.0381	0.0272	0.0219	0.0219	2.9345	2.9345		
112.5	-0.4118	-0.0939	-0.0215	-0.0273	-0.0903	-0.1722	-0.2464	-0.3004	-0.3317	-0.3418	-0.3418	5.8506	5.8506		
90.0	0.0226	-0.2320	-0.4742	-0.6432	-0.7401	-0.7798	-0.7835	-0.7711	-0.7576	-0.7521	-0.7521	-20.2240	-20.2240		
67.5	0.1490	0.0195	0.0649	0.1443	0.2236	0.2907	0.3413	0.3754	0.3948	0.4010	0.4010	4.0990	4.0990		
45.0	0.0035	-0.1926	-0.1418	-0.1086	-0.0819	-0.0615	-0.0467	-0.0367	-0.0308	-0.0289	-0.0289	3.3623	3.3623		
22.5	-0.1194	-0.3957	-0.2865	-0.2249	-0.1801	-0.1477	-0.1249	-0.1099	-0.1012	-0.0984	-0.0984	0.8137	0.8137		
-0.0	-0.1687	-0.4626	-0.3251	-0.2479	-0.1933	-0.1550	-0.1285	-0.1112	-0.1014	-0.0983	-0.0983	0.8530	0.8530		

THETA	PHI=0.0	INSIDE AXIAL STRESS FACTORS							WITHOUT END EFFECTS						
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	50.0	55.0	60.0		
180.0	0.5345	0.4124	0.1782	-0.1243	-0.4669	-0.8269	-1.1666	-1.4448	-1.6265	-1.6896	-1.6896	0.7349	0.7349		
157.5	0.0651	0.1583	-0.1158	-0.3939	-0.6545	-0.8760	-1.0466	-1.1650	-1.2342	-1.2569	-1.2569	0.7554	0.7554		
135.0	-0.8584	-0.6042	-0.8039	-0.8598	-0.8219	-0.7276	-0.6139	-0.5112	-0.4409	-0.4161	-0.4161	2.1455	2.1455		
112.5	-1.3725	-1.7695	-1.5578	-1.2927	-1.0007	-0.7225	-0.4837	-0.3016	-0.1879	-0.1493	-0.1493	-3.6899	-3.6899		
90.0	0.0754	-1.6872	-0.9712	-0.4599	-0.0670	0.2217	0.4235	0.5545	0.6275	0.6509	0.6509	-5.4593	-5.4593		
67.5	0.4966	-0.0271	0.3845	0.6171	0.7442	0.8058	0.8297	0.8350	0.8337	0.8326	0.8326	6.5881	6.5881		
45.0	0.0116	1.0769	0.9801	0.8677	0.7616	0.6705	0.5984	0.5467	0.5158	0.5055	0.5055	0.1606	0.1606		
22.5	-0.3980	1.6428	1.3154	1.0598	0.8697	0.7300	0.6302	0.5633	0.5249	0.5123	0.5123	-0.0414	-0.0414		
-0.0	-0.5624	1.8132	1.4095	1.1078	0.8913	0.7365	0.6282	0.5567	0.5160	0.5028	0.5028	0.0532	0.0532		

THETA	PHI=0.0	INSIDE SHEAR STRESS FACTORS							WITHOUT END EFFECTS						
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	50.0	55.0	60.0		
180.0	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0	0.0		
157.5	-0.3611	-0.4584	-0.6050	-0.7323	-0.8202	-0.8377	-0.7602	-0.5806	-0.3149	-0.0000	-0.0000	0.0	0.0		
135.0	-0.7574	-0.8870	-0.9818	-1.0162	-0.9699	-0.8480	-0.6702	-0.4590	-0.2322	-0.0000	-0.0000	0.0	0.0		
112.5	-0.9805	-1.0875	-0.8434	-0.5840	-0.3489	-0.1681	-0.0521	0.0036	0.0139	0.0000	0.0000	0.0	0.0		
90.0	-0.3332	-0.0087	0.2454	0.3807	0.4232	0.3994	0.3307	0.2337	0.1205	0.0000	0.0000	0.0	0.0		
67.5	0.7976	0.9927	0.8554	0.7122	0.5715	0.4396	0.3182	0.2062	0.1013	-0.0000	-0.0000	0.0	0.0		
45.0	1.0673	0.9551	0.7192	0.5398	0.4019	0.2931	0.2045	0.1295	0.0628	0.0000	0.0000	0.0	0.0		
22.5	0.6715	0.5484	0.3937	0.2843	0.2053	0.1463	0.1003	0.0628	0.0302	0.0000	0.0000	0.0	0.0		
-0.0	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	0.0	0.0		

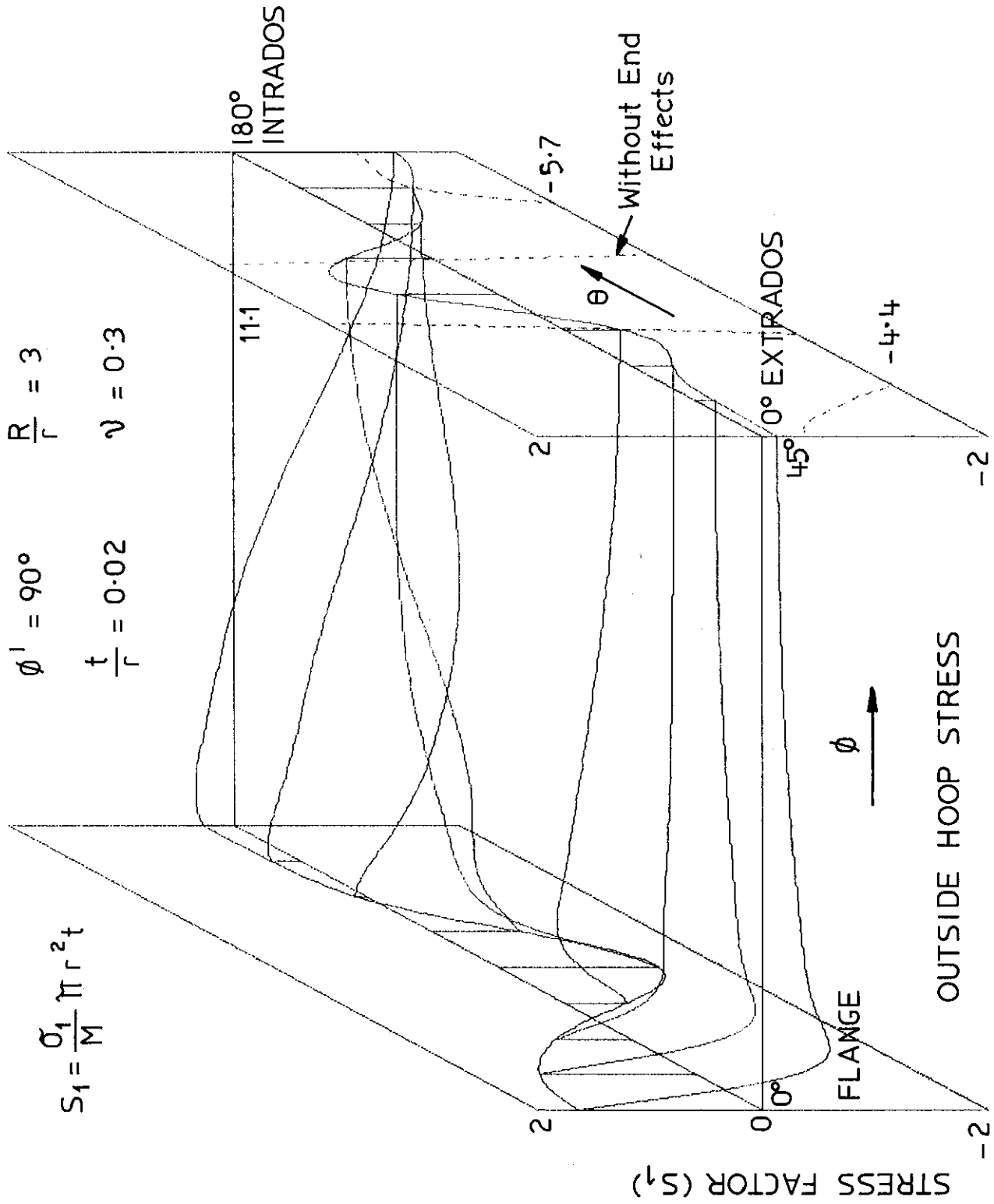


FIGURE A11

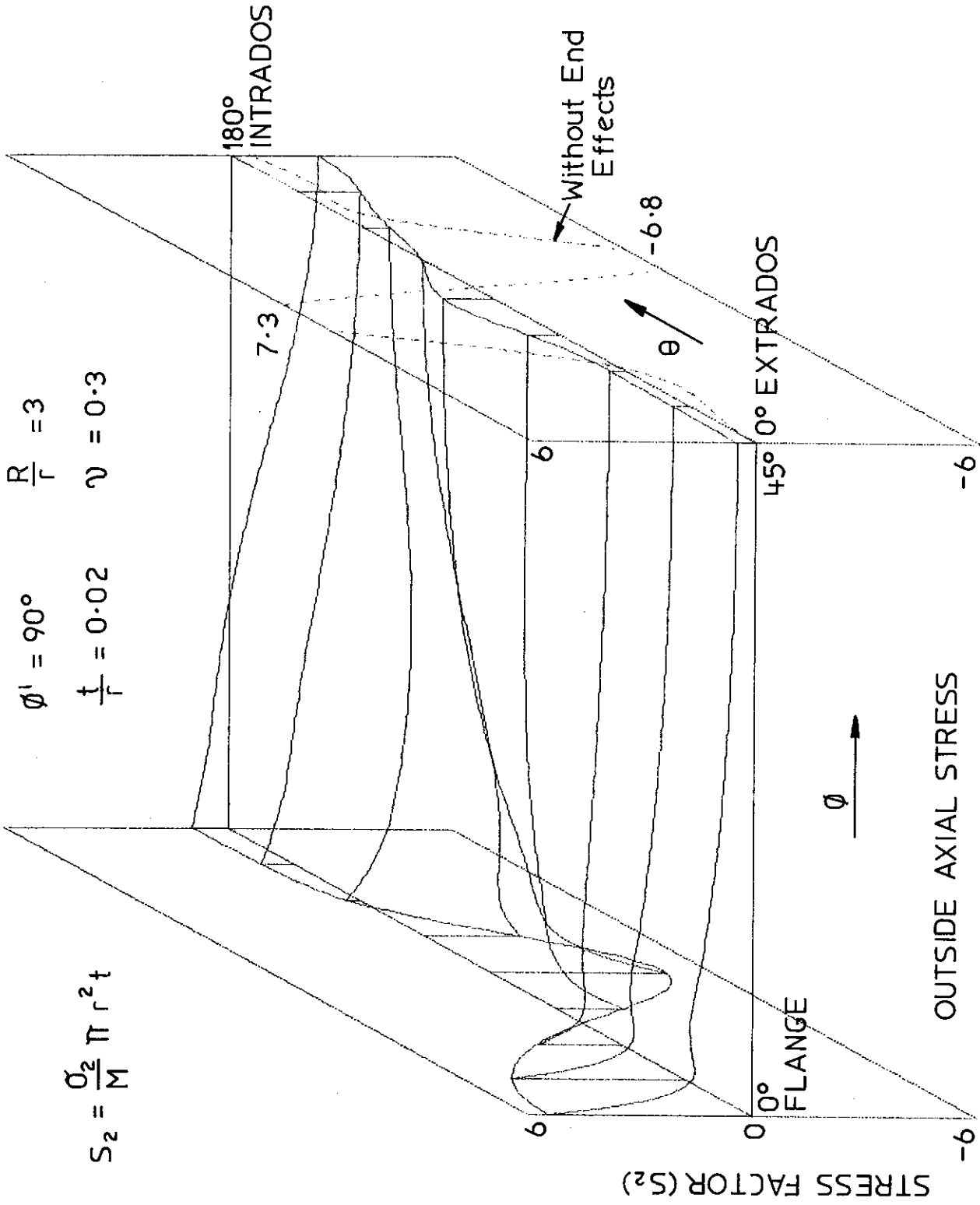


FIGURE A12

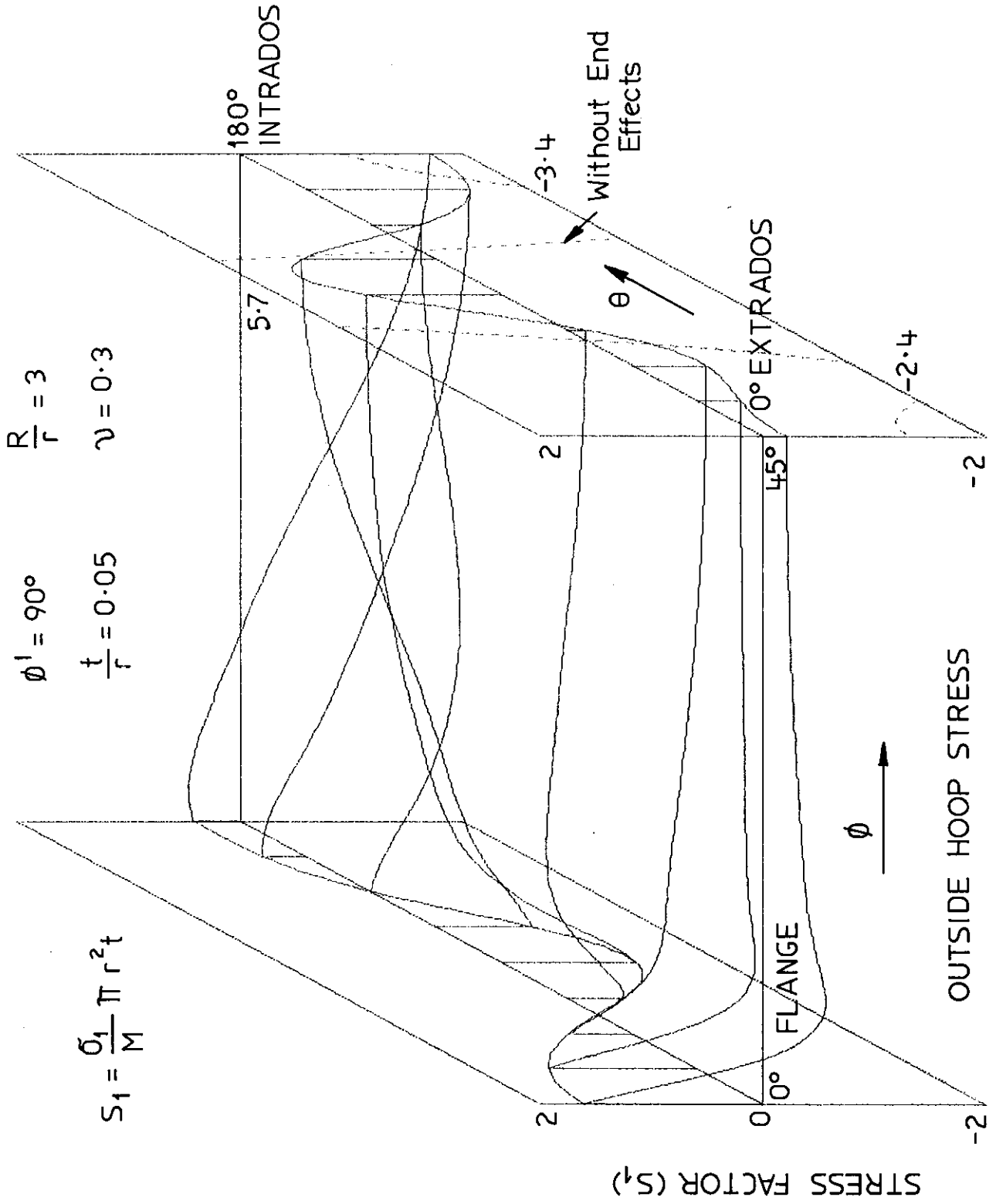


FIGURE A13

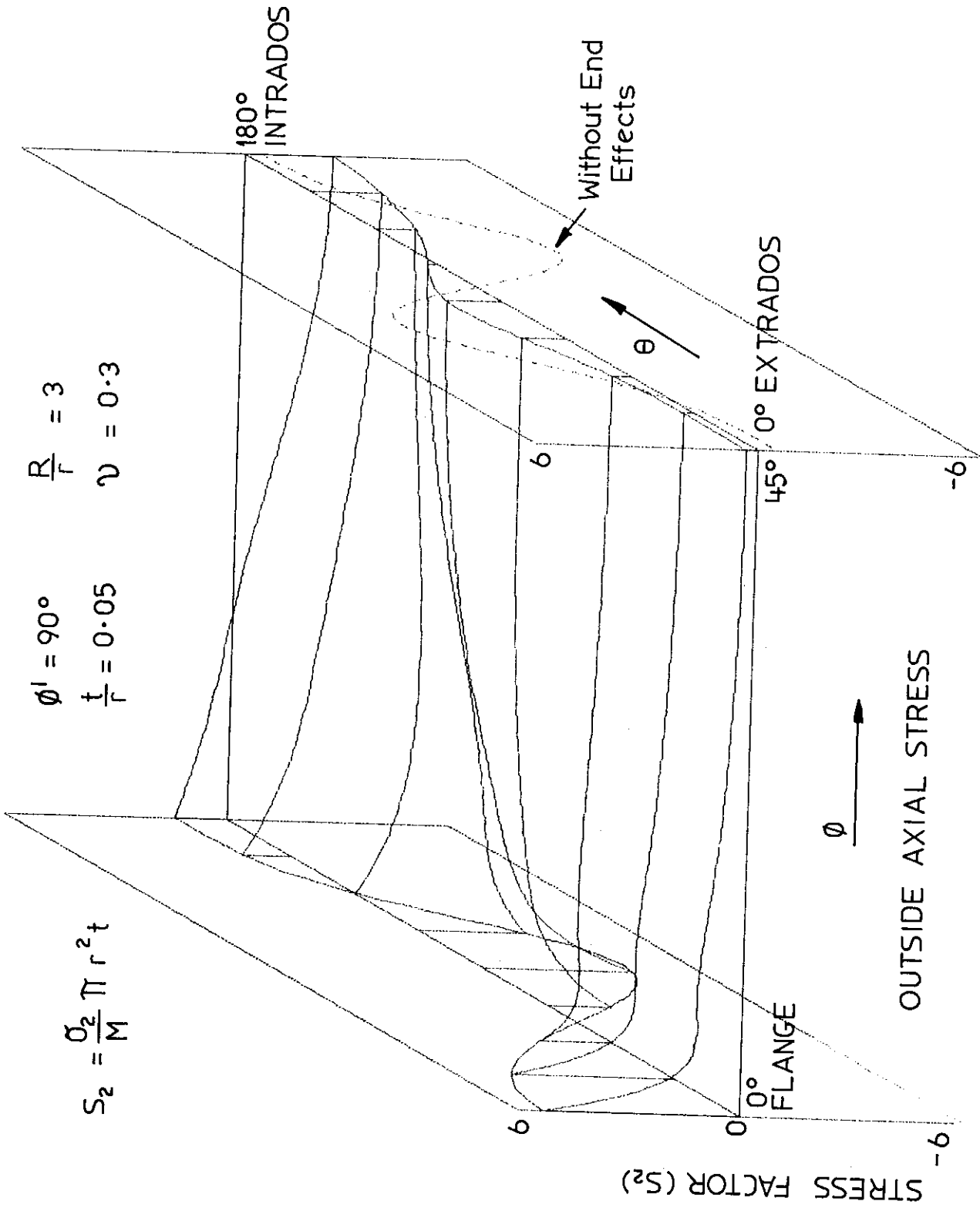


FIGURE A14

TABLE A14

R/r = 3.0 t/r = 0.05

THETA	PHI=0.0	INSIDE HOOP STRESS FACTORS						WITHOUT END EFFECTS											
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	40.0	35.0	30.0	25.0	20.0	15.0	10.0	5.0	
180.0	-0.1197	0.0371	-0.1308	-0.2551	-0.2414	-0.1184	0.0590	0.2357	0.3637	0.4103	0.9202	0.2357	0.3637	0.4103	0.9202	0.2357	0.3637	0.4103	0.9202
157.5	-0.2648	0.0298	0.0177	0.0326	0.1150	0.2259	0.3326	0.4175	0.4717	0.4902	2.1187	0.4175	0.4717	0.4902	2.1187	0.4175	0.4717	0.4902	2.1187
135.0	-0.4228	0.0239	0.2372	0.3315	0.3433	0.2854	0.1823	0.0709	-0.0126	-0.0434	3.2124	0.0709	-0.0126	-0.0434	3.2124	0.0709	-0.0126	-0.0434	3.2124
112.5	-0.1405	-0.2420	-0.2122	-0.4024	-0.6649	-0.9285	-1.1641	-1.3495	-1.4676	-1.5081	-2.4216	-1.3495	-1.4676	-1.5081	-2.4216	-1.3495	-1.4676	-1.5081	-2.4216
90.0	0.2748	-0.5319	-0.6593	-0.9049	-1.1175	-1.2593	-1.3455	-1.3929	-1.4152	-1.4215	-6.9128	-1.3929	-1.4152	-1.4215	-6.9128	-1.3929	-1.4152	-1.4215	-6.9128
67.5	0.2849	-0.3501	-0.3164	-0.2886	-0.2380	-0.1610	-0.0796	-0.0105	0.0353	0.0514	-2.2472	-0.0105	0.0353	0.0514	-2.2472	-0.0105	0.0353	0.0514	-2.2472
45.0	0.0092	-0.0721	-0.0213	0.1291	0.2505	0.3525	0.4323	0.4887	0.5223	0.5334	2.0624	0.4887	0.5223	0.5334	2.0624	0.4887	0.5223	0.5334	2.0624
22.5	-0.2325	-0.0106	-0.1063	0.0131	0.0849	0.1323	0.1638	0.1831	0.1935	0.1967	1.9794	0.1831	0.1935	0.1967	1.9794	0.1831	0.1935	0.1967	1.9794
-0.0	-0.3173	-0.0270	-0.1961	-0.0990	-0.0517	-0.0255	-0.0100	-0.0015	0.0026	0.0038	1.3121	-0.0015	0.0026	0.0038	1.3121	-0.0015	0.0026	0.0038	1.3121

THETA	PHI=0.0	INSIDE AXIAL STRESS FACTORS						WITHOUT END EFFECTS											
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	40.0	35.0	30.0	25.0	20.0	15.0	10.0	5.0	
180.0	-0.3989	-0.1397	-0.1523	-0.3179	-0.4546	-0.5196	-0.5324	-0.5201	-0.5038	-0.4968	0.9518	-0.5201	-0.5038	-0.4968	0.9518	-0.5201	-0.5038	-0.4968	0.9518
157.5	-0.8828	-0.3024	-0.2180	-0.3231	-0.4221	-0.4800	-0.5104	-0.5265	-0.5344	-0.5368	1.2644	-0.5265	-0.5344	-0.5368	1.2644	-0.5265	-0.5344	-0.5368	1.2644
135.0	-1.4092	-0.7964	-0.6613	-0.6638	-0.6911	-0.7191	-0.7490	-0.7784	-0.8005	-0.8087	0.0782	-0.7784	-0.8005	-0.8087	0.0782	-0.7784	-0.8005	-0.8087	0.0782
112.5	-0.4683	-1.3454	-1.2243	-1.0516	-0.9476	-0.8693	-0.8076	-0.7643	-0.7389	-0.7306	-2.9195	-0.7643	-0.7389	-0.7306	-2.9195	-0.7643	-0.7389	-0.7306	-2.9195
90.0	0.9167	-1.1438	-0.8196	-0.4445	-0.2028	-0.0170	0.1287	0.2333	0.2964	0.3175	-1.7255	0.2333	0.2964	0.3175	-1.7255	0.2333	0.2964	0.3175	-1.7255
67.5	0.9498	-0.0766	0.2355	0.5206	0.6909	0.8081	0.8900	0.9435	0.9737	0.9835	1.5963	0.9435	0.9737	0.9835	1.5963	0.9435	0.9737	0.9835	1.5963
45.0	0.0305	1.0726	0.9316	0.9077	0.8745	0.8339	0.7971	0.7679	0.7492	0.7427	1.7294	0.7679	0.7492	0.7427	1.7294	0.7679	0.7492	0.7427	1.7294
22.5	-0.7750	1.7979	1.1890	0.9425	0.7757	0.6437	0.5470	0.4808	0.4422	0.4295	0.3870	0.4808	0.4422	0.4295	0.3870	0.4808	0.4422	0.4295	0.3870
-0.0	-1.0577	2.0336	1.2509	0.9397	0.7374	0.5839	0.4754	0.4033	0.3620	0.3486	-0.1552	0.4033	0.3620	0.3486	-0.1552	0.4033	0.3620	0.3486	-0.1552

THETA	PHI=0.0	INSIDE SHEAR STRESS FACTORS						WITHOUT END EFFECTS											
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	40.0	35.0	30.0	25.0	20.0	15.0	10.0	5.0	
180.0	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0	0.0000	0.0000	0.0000	0.0	0.0000	0.0000	0.0000	0.0
157.5	-0.3540	-0.4562	-0.6315	-0.7680	-0.8302	-0.8048	-0.6928	-0.5067	-0.2672	-0.0000	0.0	-0.5067	-0.2672	-0.0000	0.0	-0.5067	-0.2672	-0.0000	0.0
135.0	-0.6299	-1.0005	-1.0918	-1.0654	-0.9782	-0.8424	-0.6669	-0.4615	-0.2358	-0.0000	0.0	-0.4615	-0.2358	-0.0000	0.0	-0.4615	-0.2358	-0.0000	0.0
112.5	-0.6312	-0.9712	-0.7687	-0.5407	-0.3590	-0.2221	-0.1260	-0.0639	-0.0258	-0.0000	0.0	-0.0639	-0.0258	-0.0000	0.0	-0.0639	-0.0258	-0.0000	0.0
90.0	-0.1741	0.0159	0.2170	0.3268	0.3691	0.3585	0.3056	0.2212	0.1159	0.0000	0.0	0.2212	0.1159	0.0000	0.0	0.2212	0.1159	0.0000	0.0
67.5	0.4292	0.9338	0.8332	0.7163	0.6018	0.4833	0.3627	0.2417	0.1208	0.0000	0.0	0.2417	0.1208	0.0000	0.0	0.2417	0.1208	0.0000	0.0
45.0	0.6812	1.0423	0.7664	0.5821	0.4422	0.3268	0.2298	0.1462	0.0710	0.0000	0.0	0.1462	0.0710	0.0000	0.0	0.1462	0.0710	0.0000	0.0
22.5	0.4715	0.6023	0.4017	0.2874	0.2066	0.1456	0.0986	0.0610	0.0291	0.0000	0.0	0.0610	0.0291	0.0000	0.0	0.0610	0.0291	0.0000	0.0
-0.0	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	0.0	-0.0000	-0.0000	-0.0000	0.0	-0.0000	-0.0000	-0.0000	0.0

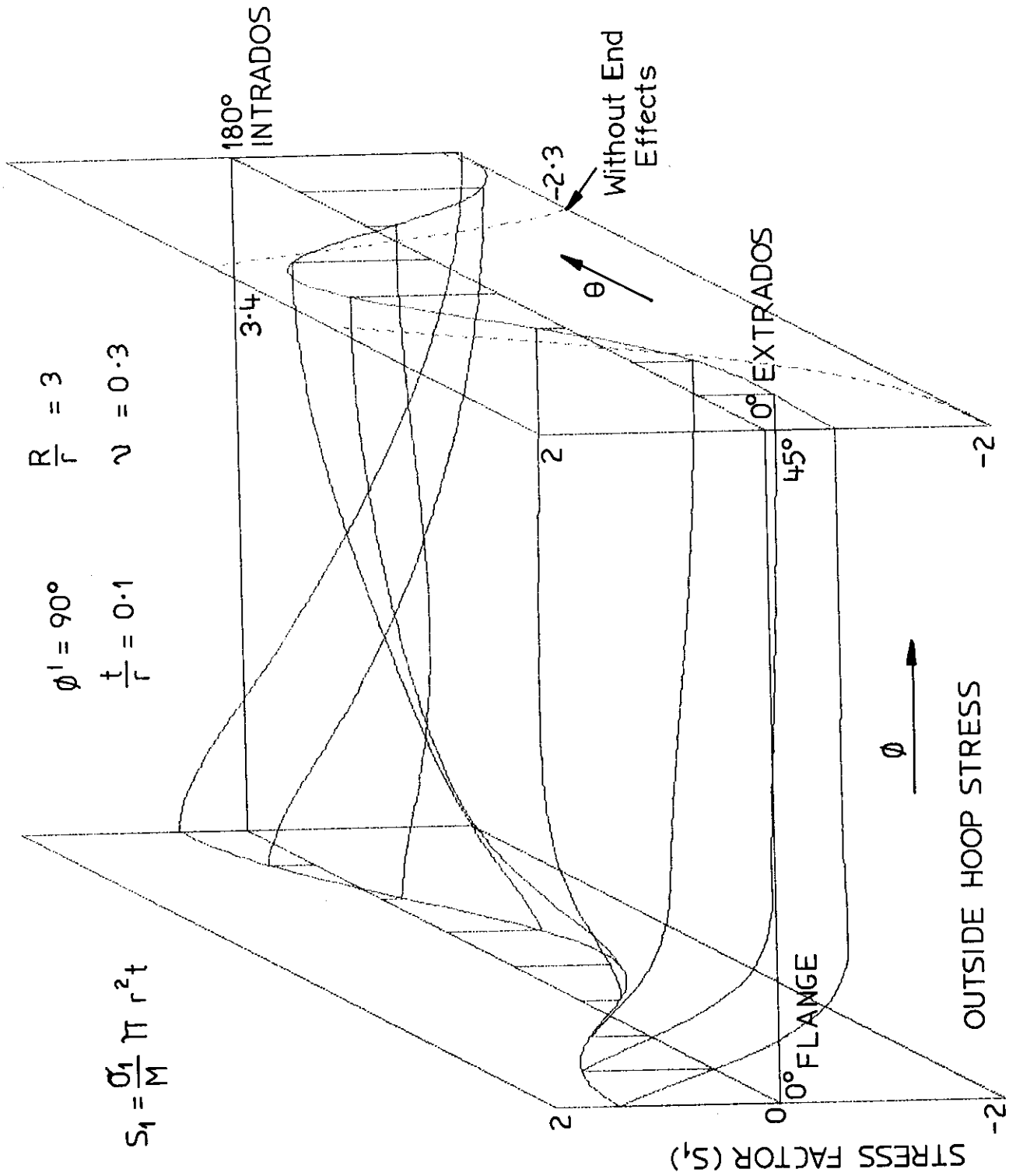


FIGURE A15

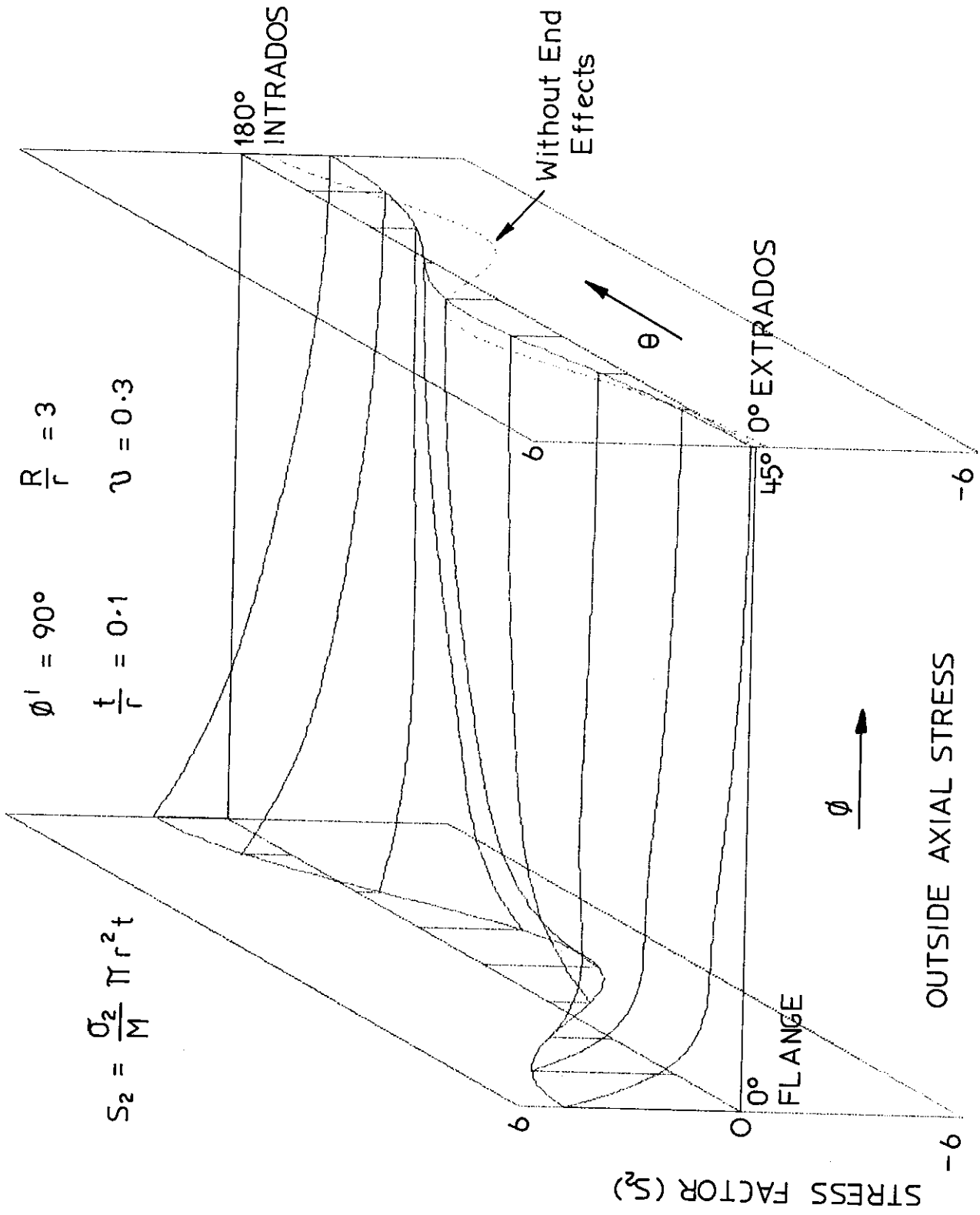


FIGURE A16

TABLE A15

R/r = 3.0 t/r = 0.10

THETA	PHI=0.0	OUTSIDE HOOP STRESS FACTORS							WITHOUT END EFFECTS		
		15.0	20.0	25.0	30.0	35.0	40.0	45.0	45.0	45.0	
180.0	0.6006	-0.5683	-0.9697	-1.3221	-1.6222	-1.8554	-2.0041	-2.0553	-1.8824	-2.0553	-1.8824
157.5	0.4032	-0.6749	-0.9703	-1.2064	-1.3939	-1.5330	-1.6194	-1.6488	-2.2597	-1.6488	-2.2597
135.0	-0.1921	-0.4222	-0.4912	-0.4490	-0.3876	-0.3291	-0.2886	-0.2742	-1.4023	-0.2742	-1.4023
112.5	-0.8402	-0.0211	0.2624	0.5061	0.7376	1.1063	1.2089	1.2439	1.7555	1.2439	1.7555
90.0	-0.9351	0.3626	0.6728	0.8716	1.0298	1.1570	1.2496	1.3241	3.3624	1.3241	3.3624
67.5	-0.3539	0.1995	0.2909	0.3041	0.2951	0.2808	0.2663	0.2555	1.5784	0.2555	1.5784
45.0	0.4993	-0.0803	-0.2794	-0.3410	-0.4090	-0.4671	-0.5109	-0.5383	-0.8183	-0.5477	-0.8183
22.5	1.1748	-0.1567	-0.5657	-0.5870	-0.6200	-0.6467	-0.6652	-0.6798	-1.8438	-0.6798	-1.8438
-0.0	1.4232	-0.1923	-0.6244	-0.6128	-0.6191	-0.6238	-0.6255	-0.6261	-1.9848	-0.6261	-1.9848

THETA	PHI=0.0	OUTSIDE AXIAL STRESS FACTORS							WITHOUT END EFFECTS		
		15.0	20.0	25.0	30.0	35.0	40.0	45.0	45.0	45.0	
180.0	2.0020	-0.6163	-1.1046	-1.5315	-1.8945	-2.1731	-2.3480	-2.4075	-0.6837	-2.4075	-0.6837
157.5	1.3441	-1.0114	-1.3499	-1.6204	-1.8399	-2.0053	-2.1084	-2.1435	-1.4797	-2.1435	-1.4797
135.0	-0.6404	-1.4403	-1.4423	-1.3953	-1.3389	-1.2928	-1.2639	-1.2541	-2.6914	-1.2541	-2.6914
112.5	-2.8006	-0.8594	-0.5738	-0.2954	-0.0577	0.1192	0.2273	0.2635	-1.5775	0.2635	-1.5775
90.0	-3.1171	0.3003	0.6319	0.9165	1.1429	1.3046	1.4011	1.4332	1.3099	1.4332	1.3099
67.5	-1.1796	0.9618	1.1131	1.2265	1.3100	1.3652	1.3963	1.4064	2.5023	1.4064	2.5023
45.0	1.6645	0.9777	0.9167	0.8553	0.8071	0.7709	0.7481	0.7403	1.4945	0.7403	1.4945
22.5	3.9160	0.8105	0.6325	0.4847	0.3787	0.3062	0.2635	0.2493	0.1867	0.2493	0.1867
-0.0	4.7440	0.7392	0.5306	0.3628	0.2456	0.1673	0.1218	0.1068	-0.3029	0.1068	-0.3029

THETA	PHI=0.0	OUTSIDE SHEAR STRESS FACTORS							WITHOUT END EFFECTS		
		15.0	20.0	25.0	30.0	35.0	40.0	45.0	45.0	45.0	
180.0	0.0000	0.0000	0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	0.0	-0.0000	0.0
157.5	-0.3293	-0.0942	-0.0203	0.0359	0.0638	0.0622	0.0374	0.0000	0.0	0.0000	0.0
135.0	-0.5240	-0.1223	-0.0607	-0.0133	0.0134	0.0207	0.0140	-0.0000	0.0	-0.0000	0.0
112.5	-0.4504	-0.1324	-0.1164	-0.0991	-0.0796	-0.0564	-0.0293	-0.0000	0.0	-0.0000	0.0
90.0	-0.1055	-0.0340	-0.0518	-0.0612	-0.0591	-0.0462	-0.0252	0.0000	0.0	0.0000	0.0
67.5	0.2819	0.1563	0.1068	0.0690	0.0427	0.0243	0.0109	0.0000	0.0	0.0000	0.0
45.0	0.4508	0.2577	0.1919	0.1411	0.1001	0.0645	0.0316	0.0000	0.0	0.0000	0.0
22.5	0.3217	0.1852	0.1386	0.1032	0.0742	0.0482	0.0238	0.0000	0.0	0.0000	0.0
-0.0	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	0.0	-0.0000	0.0

TABLE A16

R/ = 3.0 / = 0.10

THETA	INSIDE HUOP STRESS FACTORS										WITHOUT END EFFECTS		
	PHI=0.0	5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	WITHOUT END EFFECTS	45.0	WITHOUT END EFFECTS
180.0	-0.4692	-0.0968	-0.0011	0.0956	0.2777	0.5263	0.7892	1.0149	1.1655	1.2181	1.8776	1.2181	1.8776
157.5	-0.4707	-0.0524	0.1227	0.2507	0.3933	0.5496	0.6985	0.8191	0.8966	0.9232	2.2678	0.9232	2.2678
135.0	-0.3146	-0.0452	0.1191	0.1528	0.0956	-0.0048	-0.1145	-0.2101	-0.2748	-0.2976	1.1824	-0.2976	1.1824
112.5	0.0591	-0.2458	-0.3433	-0.5445	-0.8252	-1.1158	-1.3719	-1.5696	-1.6942	-1.7367	-2.5210	-1.7367	-2.5210
90.0	0.3296	-0.4392	-0.6914	-0.9136	-1.1401	-1.3365	-1.4872	-1.5918	-1.6534	-1.6737	-4.3099	-1.6737	-4.3099
67.5	0.2732	-0.3340	-0.4926	-0.5177	-0.5182	-0.5055	-0.4816	-0.4556	-0.4363	-0.4293	-2.1465	-0.4293	-2.1465
45.0	0.0069	-0.0388	-0.1171	-0.0100	0.1168	0.2234	0.3111	0.3778	0.4194	0.4336	0.6534	0.4336	0.6534
22.5	-0.2454	0.1975	0.0741	0.1790	0.3052	0.3960	0.4606	0.5053	0.5317	0.5404	1.8291	0.5404	1.8291
-0.0	-0.3431	0.2777	0.1101	0.1925	0.3003	0.3704	0.4152	0.4439	0.4600	0.4651	1.9872	0.4651	1.9872
INSIDE AXIAL STRESS FACTORS													
THETA	INSIDE AXIAL STRESS FACTORS										WITHOUT END EFFECTS		
	PHI=0.0	5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	WITHOUT END EFFECTS	45.0	WITHOUT END EFFECTS
180.0	-1.5641	-0.7502	-0.3449	-0.2098	-0.1671	-0.1280	-0.0744	-0.0180	0.0240	0.0394	1.2586	0.0394	1.2586
157.5	-1.5688	-0.7603	-0.4129	-0.3178	-0.3087	-0.3091	-0.2988	-0.2816	-0.2667	-0.2609	0.8534	-0.2609	0.8534
135.0	-1.0486	-0.7903	-0.6933	-0.6670	-0.6865	-0.7263	-0.7667	-0.7983	-0.8179	-0.8245	-0.5912	-0.8245	-0.5912
112.5	0.1970	-0.7637	-0.9227	-0.8499	-0.7892	-0.7699	-0.7713	-0.7782	-0.7840	-0.7862	-1.8210	-0.7862	-1.8210
90.0	1.0985	-0.4619	-0.5892	-0.3913	-0.2215	-0.1132	-0.0427	0.0042	0.0317	0.0408	-1.0452	0.0408	-1.0452
67.5	0.9108	0.1845	0.1805	0.3475	0.4941	0.5933	0.6606	0.7066	0.7339	0.7431	0.5752	0.7431	0.5752
45.0	0.0230	0.9332	0.8598	0.8013	0.8034	0.8049	0.8007	0.7967	0.7944	0.7937	1.1429	0.7937	1.1429
22.5	-0.6179	1.4874	1.2170	0.9198	0.7834	0.6920	0.6207	0.5706	0.5413	0.5316	0.7644	0.5316	0.7644
-0.0	-1.1435	1.6860	1.3155	0.9231	0.7349	0.6094	0.5139	0.4475	0.4087	0.3960	0.4816	0.3960	0.4816
INSIDE SHEAR STRESS FACTORS													
THETA	INSIDE SHEAR STRESS FACTORS										WITHOUT END EFFECTS		
	PHI=0.0	5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	WITHOUT END EFFECTS	45.0	WITHOUT END EFFECTS
180.0	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0	0.0000	0.0
157.5	-0.2979	-0.5635	-0.7314	-0.7902	-0.7657	-0.6799	-0.5482	-0.3832	-0.1969	-0.0000	0.0	-0.0000	0.0
135.0	-0.4741	-0.9310	-1.0460	-0.9957	-0.8798	-0.7332	-0.5668	-0.3859	-0.1954	-0.0000	0.0	-0.0000	0.0
112.5	-0.4075	-0.6944	-0.6147	-0.4650	-0.3360	-0.2368	-0.1604	-0.0993	-0.0475	0.0000	0.0	0.0000	0.0
90.0	-0.0954	0.0858	0.2122	0.2726	0.2859	0.2649	0.2188	0.1551	0.0802	0.0000	0.0	0.0000	0.0
67.5	0.2551	0.7693	0.7465	0.6417	0.5396	0.4375	0.3321	0.2234	0.1123	0.0000	0.0	0.0000	0.0
45.0	0.4078	0.9158	0.7551	0.5794	0.4514	0.3461	0.2521	0.1648	0.0815	0.0000	0.0	0.0000	0.0
22.5	0.2911	0.5758	0.4328	0.3115	0.2321	0.1717	0.1215	0.0778	0.0380	0.0000	0.0	0.0000	0.0
-0.0	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	0.0000	0.0	0.0000	0.0

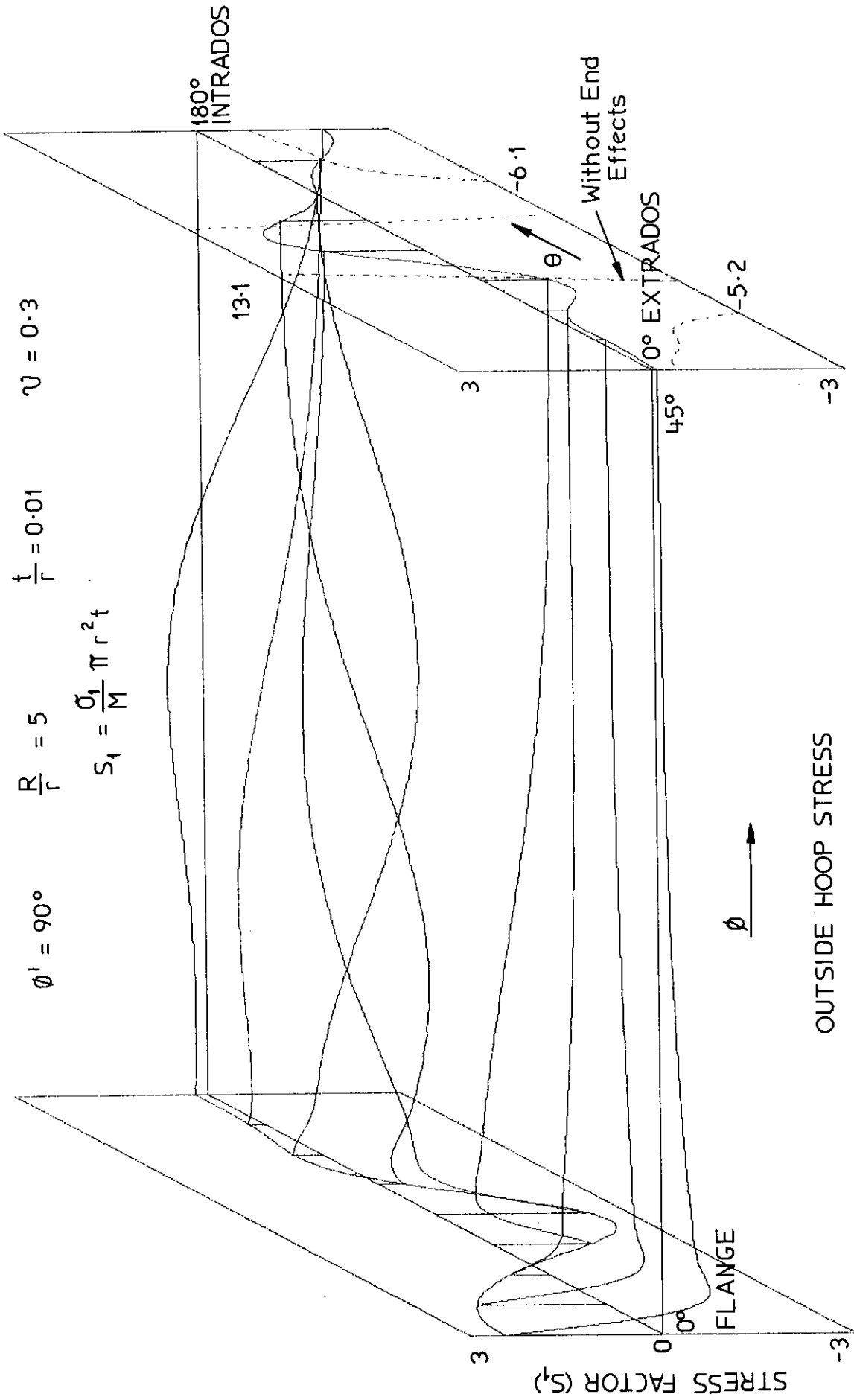


FIGURE A17

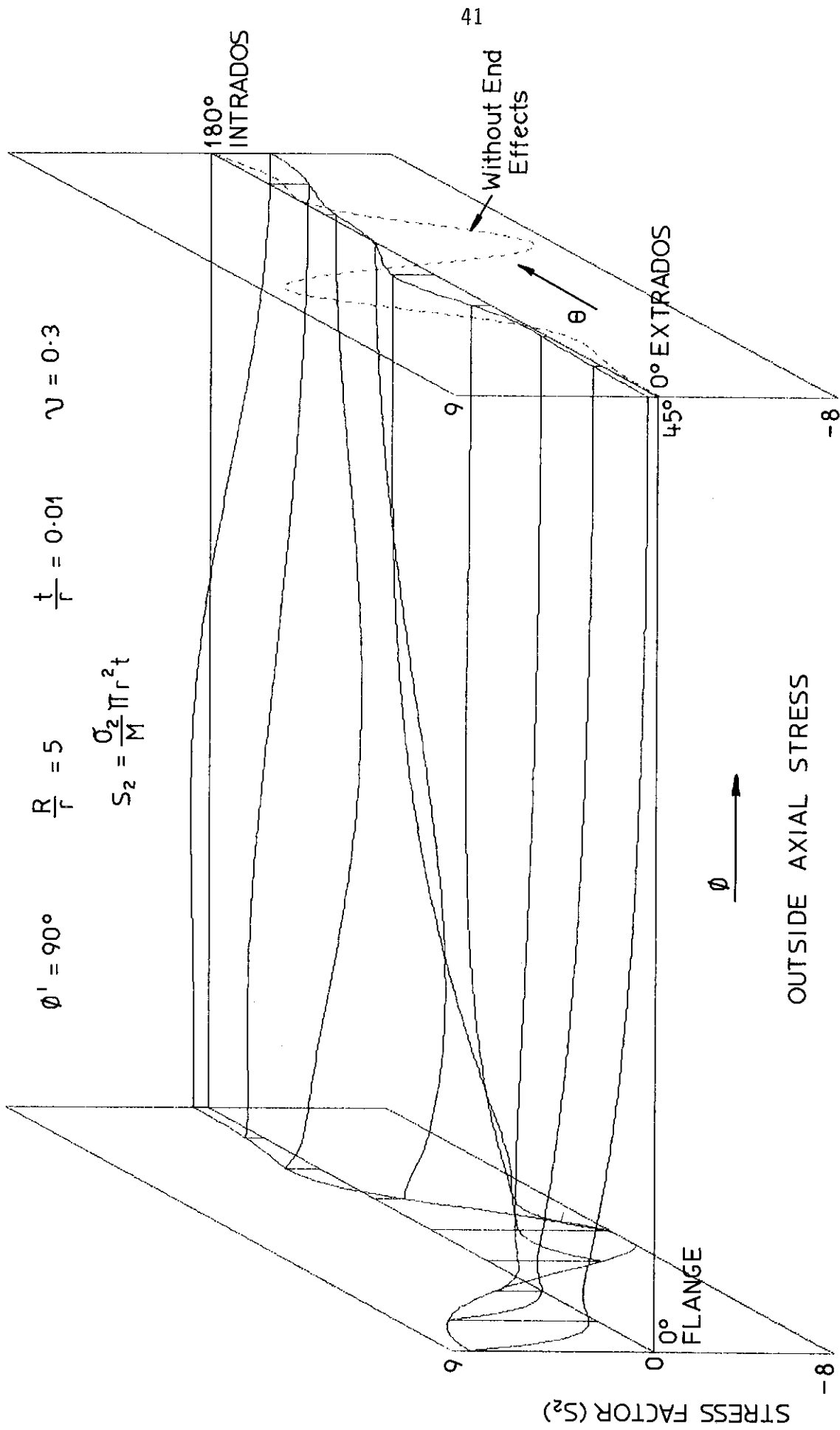


FIGURE A18

TABLE A18

R/r = 5.0 t/r = 0.01.

THETA	INSIDE HOOP STRESS FACTORS										WITHOUT END EFFECTS	
	PHI=0.0	5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	WITHOUT END EFFECTS	WITHOUT END EFFECTS
180.0	0.1815	0.1691	0.0739	-0.2074	-0.5001	-0.5296	-0.1910	0.3717	0.8785	45.0	0.9798	0.9726
157.5	0.1966	0.0383	-0.1658	-0.2247	-0.0904	0.1178	0.2844	0.3749	0.4099	1.0798	0.4178	0.9459
135.0	-0.0010	0.0564	0.3966	0.8816	1.2052	1.2083	0.9028	0.4362	0.0258	-0.1364	4.3291	4.3291
112.5	-0.5546	0.3243	0.4830	0.2348	-0.2458	-0.7420	-1.1083	-1.3059	-1.3785	-1.3926	1.3597	1.3597
90.0	-0.2463	-0.5497	-1.2847	-1.8270	-2.0942	-2.1244	-2.0081	-1.8430	-1.7095	-1.6591	-14.1285	-14.1285
67.5	0.1633	-0.0358	0.0655	0.2886	0.5283	0.7253	0.8568	0.9275	0.9564	0.9634	0.8029	0.8029
45.0	0.0395	-0.0214	0.1277	0.2463	0.3244	0.3695	0.3931	0.4051	0.4110	0.4128	4.1374	4.1374
22.5	-0.0291	-0.3255	-0.2190	-0.1491	-0.1018	-0.0686	-0.0449	-0.0289	-0.0196	-0.0165	0.9700	0.9700
-0.0	-0.0812	-0.4013	-0.2526	-0.1573	-0.0951	-0.0537	-0.0263	-0.0090	0.0006	0.0037	0.7688	0.7688
AXIAL STRESS FACTORS												
THETA	INSIDE AXIAL STRESS FACTORS										WITHOUT END EFFECTS	
	PHI=0.0	5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	WITHOUT END EFFECTS	WITHOUT END EFFECTS
180.0	0.6051	0.6672	0.6023	0.3395	-0.0956	-0.5465	-0.8651	-1.0105	-1.0401	-1.0376	0.4826	0.4826
157.5	0.6554	0.6270	0.3554	0.0435	-0.2218	-0.4428	-0.6492	-0.8403	-0.9819	-1.0346	0.6539	0.6539
135.0	-0.0035	0.0601	-0.3700	-0.5662	-0.6075	-0.5945	-0.5933	-0.6225	-0.6625	-0.6809	1.7084	1.7084
112.5	-1.8486	-2.1602	-2.3008	-2.1996	-1.9836	-1.6978	-1.3732	-1.0603	-0.8291	-0.7434	-4.7217	-4.7217
90.0	-0.8212	-3.0249	-2.0294	-1.1961	-0.5279	-0.0173	0.3444	0.5743	0.6969	0.7347	-3.9271	-3.9271
67.5	0.5444	-0.7208	0.2762	0.8590	1.1665	1.3002	1.3340	1.3218	1.3002	1.2907	5.2009	5.2009
45.0	0.2982	1.2105	1.1302	0.9789	0.8165	0.6726	0.5596	0.4809	0.4352	0.4203	1.1871	1.1871
22.5	-0.0969	2.3401	1.6968	1.2465	0.9317	0.7126	0.5630	0.4662	0.4117	0.3941	-0.1054	-0.1054
-0.0	-0.2705	2.7122	1.9042	1.3710	1.0136	0.7720	0.6105	0.5074	0.4500	0.4315	0.1070	0.1070
SHEAR STRESS FACTORS												
THETA	INSIDE SHEAR STRESS FACTORS										WITHOUT END EFFECTS	
	PHI=0.0	5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	WITHOUT END EFFECTS	WITHOUT END EFFECTS
180.0	-0.0000	-0.0000	-0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	45.0	0.0000	0.0
157.5	0.0008	0.0472	-0.0130	-0.2201	-0.5133	-0.7631	-0.8527	-0.7303	-0.4194	-0.0000	0.0	0.0
135.0	-0.1815	-0.3076	-0.6313	-0.8638	-0.9385	-0.8758	-0.7218	-0.5116	-0.2654	0.0000	0.0	0.0
112.5	-0.9341	-1.3347	-1.1612	-0.8427	-0.4967	-0.1987	0.0053	0.0946	0.0789	-0.0000	0.0	0.0
90.0	-0.9700	-0.5957	-0.0868	0.2292	0.3861	0.4212	0.3714	0.2692	0.1399	-0.0000	0.0	0.0
67.5	0.5215	0.9693	0.8940	0.7536	0.5951	0.4422	0.3059	0.1895	0.0899	0.0000	0.0	0.0
45.0	1.3332	1.2014	0.8461	0.5967	0.4195	0.2912	0.1955	0.1206	0.0576	0.0000	0.0	0.0
22.5	0.9454	0.7276	0.4769	0.3197	0.2174	0.1478	0.0979	0.0598	0.0284	0.0000	0.0	0.0
-0.0	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	0.0000	0.0	0.0

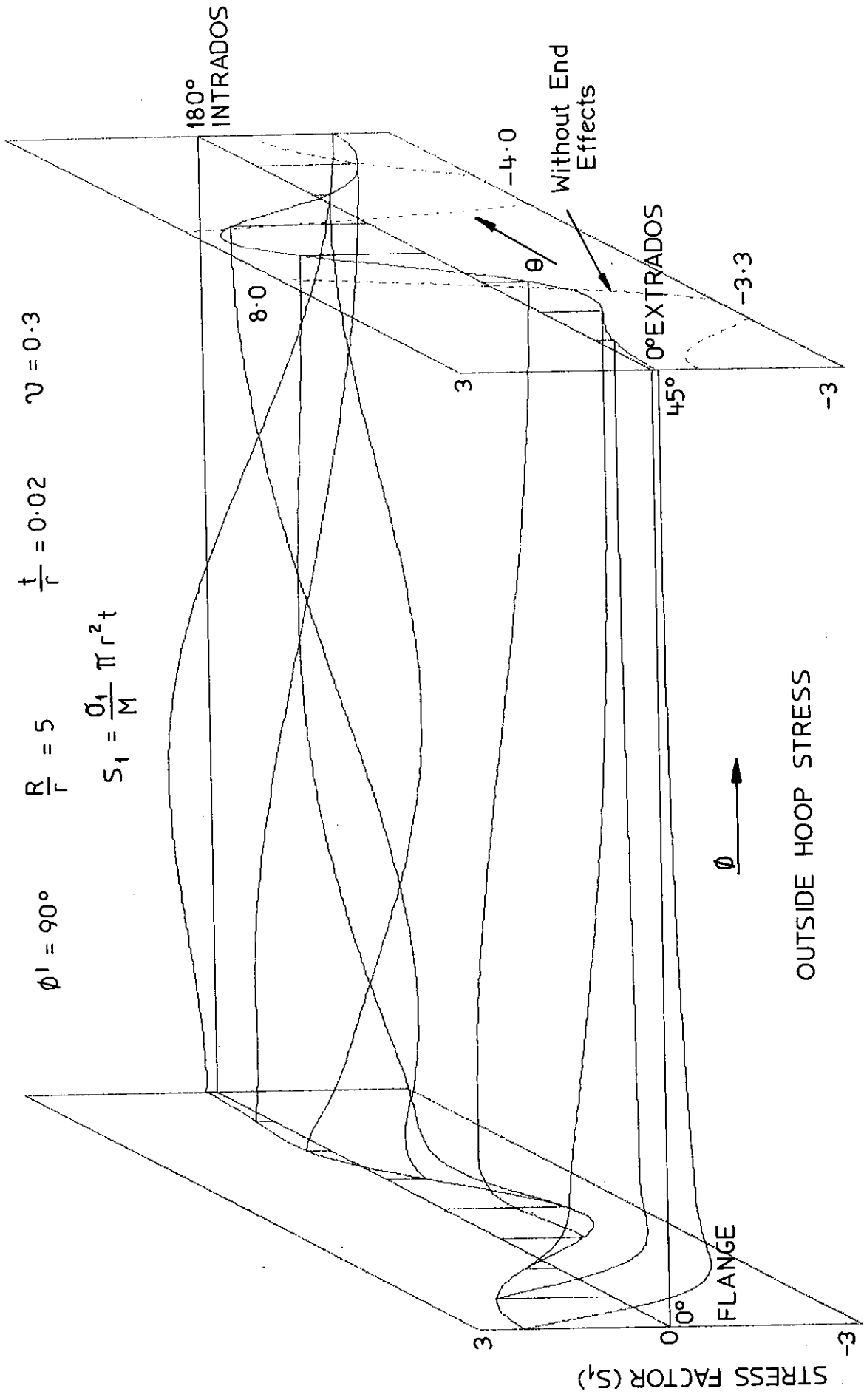


FIGURE A19

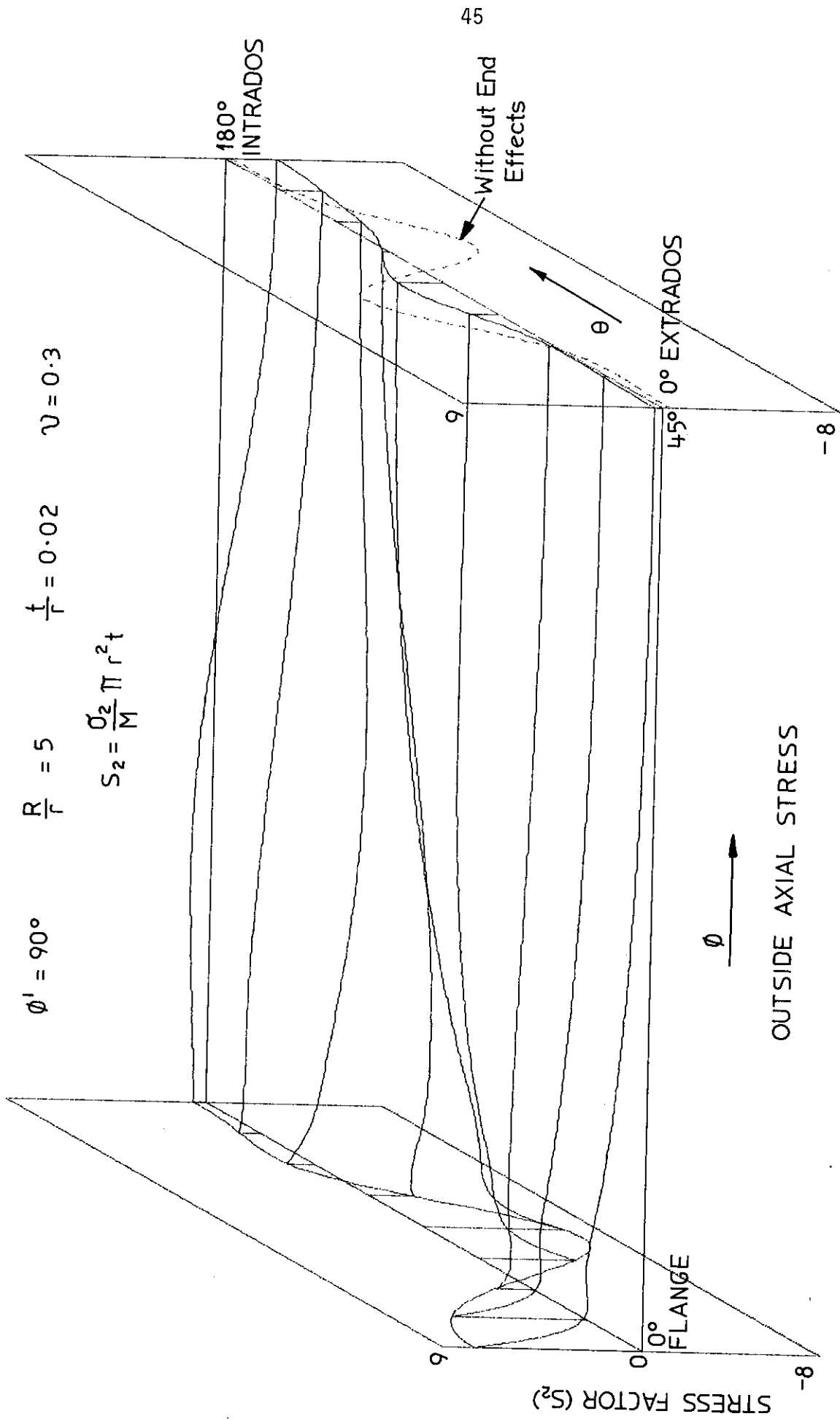


FIGURE A20

TABLE A19

R/r = 5.0 t/r = 0.02

THETA	PHI=0.0	OUTSIDE HOOP STRESS FACTORS							WITHOUT END EFFECTS		
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	
180.0	0.1694	0.3018	0.5432	0.6666	0.4881	-0.0178	-0.7216	-1.4222	-1.9291	-2.1130	-0.7488
157.5	0.2868	0.2469	0.1961	-0.0334	-0.3682	-0.7359	-1.0840	-1.3716	-1.5626	-1.6298	-1.6276
135.0	0.3703	-0.3595	-0.9190	-1.3781	-1.5583	-1.4357	-1.1004	-0.7017	-0.3901	-0.2733	-3.9828
112.5	-0.5983	-0.4810	-0.4966	-0.1935	0.2915	0.8387	1.3583	1.7836	2.0627	2.1601	1.1808
90.0	-1.9080	0.4626	1.0173	1.5346	1.8884	2.0645	2.0966	2.0464	1.9815	1.9534	8.0354
67.5	-1.3291	0.3210	0.2946	0.1735	-0.0169	-0.2304	-0.4306	-0.5912	-0.6946	-0.7302	1.3038
45.0	0.4774	-0.2755	-0.4837	-0.6724	-0.8180	-0.9162	-0.9726	-0.9989	-1.0078	-1.0095	-3.3249
22.5	1.8322	-0.4557	-0.4221	-0.3983	-0.3725	-0.3463	-0.3226	-0.3038	-0.2918	-0.2877	-1.7219
-0.0	2.2792	-0.4870	-0.3583	-0.2699	-0.2059	-0.1614	-0.1320	-0.1142	-0.1049	-0.1020	-0.7486

THETA	PHI=0.0	OUTSIDE AXIAL STRESS FACTORS							WITHOUT END EFFECTS		
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	
180.0	0.5645	0.7485	0.8797	0.7532	0.2945	-0.3977	-1.1462	-1.7872	-2.2098	-2.3564	-0.3233
157.5	0.9559	0.7245	0.4876	0.0866	-0.3713	-0.8306	-1.2550	-1.6052	-1.8383	-1.9204	-0.3891
135.0	1.2345	-0.4614	-1.2331	-1.7398	-1.9227	-1.8565	-1.6572	-1.4355	-1.2724	-1.2133	-2.7148
112.5	-1.9942	-2.5534	-2.6115	-2.3028	-1.7998	-1.2171	-0.6394	-0.1463	0.1872	0.3053	-4.0627
90.0	-6.3601	-2.2545	-1.0327	-0.0202	0.7567	1.3177	1.6971	1.9333	2.0598	2.0994	2.6695
67.5	-4.4304	-0.3042	0.6088	1.1149	1.3564	1.4320	1.4137	1.3567	1.3038	1.2828	4.5687
45.0	1.5914	1.1754	1.0552	0.8669	0.6668	0.4871	0.3429	0.2398	0.1787	0.1584	0.5610
22.5	6.1073	2.0938	1.4434	1.0021	0.6942	0.4817	0.3392	0.2491	0.1996	0.1838	-0.5878
-0.0	7.5975	2.4247	1.6450	1.1543	0.8299	0.6136	0.4707	0.3800	0.3297	0.3136	-0.3361

THETA	PHI=0.0	OUTSIDE SHEAR STRESS FACTORS							WITHOUT END EFFECTS		
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	
180.0	-0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	-0.0000	-0.0000	-0.0000	0.0000	0.0
157.5	-0.0048	-0.1780	-0.3208	-0.3394	-0.2380	-0.0859	0.0405	0.0947	0.0714	-0.0000	0.0
135.0	-0.2743	-0.4719	-0.4230	-0.3284	-0.2445	-0.1817	-0.1315	-0.0862	-0.0427	-0.0000	0.0
112.5	-0.8083	-0.6243	-0.3917	-0.2815	-0.2501	-0.2502	-0.2405	-0.1957	-0.1107	0.0000	0.0
90.0	-0.6701	-0.3302	-0.1772	-0.1090	-0.0721	-0.0472	-0.0288	-0.0157	-0.0067	0.0000	0.0
67.5	0.3684	0.4663	0.3762	0.3157	0.2701	0.2296	0.1856	0.1326	0.0695	-0.0000	0.0
45.0	1.0479	0.9162	0.6502	0.4761	0.3521	0.2577	0.1813	0.1157	0.0564	-0.0000	0.0
22.5	0.7908	0.6345	0.4259	0.2918	0.2009	0.1369	0.0901	0.0544	0.0256	0.0000	0.0
-0.0	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	0.0

TABLE A20

R/r = 5.0 t/r = 0.02

THETA	PHI=0.0	INSIDE HOOP STRESS FACTORS								WITHOUT END EFFECTS	
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	
180.0	0.2027	0.0509	-0.2542	-0.5604	-0.6110	-0.3115	0.2440	0.8572	1.3225	1.4947	0.7481
157.5	0.1434	-0.0272	-0.1070	-0.0104	0.2030	0.4583	0.7063	0.9145	1.0547	1.1044	1.6420
135.0	-0.2213	0.2292	0.7044	1.1476	1.3360	1.2143	0.8609	0.4308	0.0902	-0.0382	3.9928
112.5	-0.4939	0.2240	0.2164	-0.0876	-0.5711	-1.1072	-1.6075	-2.0115	-2.2746	-2.3660	-1.6151
90.0	-0.0691	-0.4623	-1.1572	-1.7300	-2.1092	-2.2847	-2.2988	-2.2237	-2.1380	-2.1019	-8.8648
67.5	0.2550	-0.2411	-0.3496	-0.2647	-0.0795	0.1431	0.3566	0.5292	0.6406	0.6790	-1.6739
45.0	0.1068	0.0088	0.2533	0.4843	0.6700	0.8012	0.8823	0.9250	0.9431	0.9478	3.3199
22.5	-0.0950	-0.2201	-0.0430	0.0583	0.1197	0.1543	0.1722	0.1805	0.1837	0.1845	1.7356
-0.0	-0.1657	-0.3497	-0.1985	-0.1268	-0.0838	-0.0559	-0.0367	-0.0234	-0.0153	-0.0126	0.7491

THETA	PHI=0.0	INSIDE AXIAL STRESS FACTORS								WITHOUT END EFFECTS	
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	
180.0	0.6756	0.5823	0.3504	-0.0024	-0.3359	-0.5407	-0.5926	-0.5406	-0.4643	-0.4304	0.5388
157.5	0.4781	0.4538	0.1947	-0.0204	-0.1891	-0.3210	-0.4240	-0.4991	-0.5450	-0.5603	1.0297
135.0	-0.7376	-0.2922	-0.5377	-0.5950	-0.6072	-0.6555	-0.7627	-0.9003	-1.0149	-1.0593	0.3945
112.5	-1.6464	-1.9306	-1.9356	-1.8382	-1.7075	-1.5631	-1.4195	-1.2956	-1.2113	-1.1814	-3.9197
90.0	-0.2302	-2.2992	-1.5939	-1.0365	-0.5770	-0.1914	0.1278	0.3736	0.5310	0.5854	-2.4121
67.5	0.8499	-0.5756	0.2375	0.7550	1.0818	1.2783	1.3862	1.4377	1.4577	1.4625	2.8580
45.0	0.3560	1.1156	1.1583	1.1047	1.0106	0.9051	0.8065	0.7273	0.6762	0.6586	2.0064
22.5	-0.3168	2.0506	1.4990	1.0921	0.8000	0.5919	0.4478	0.3540	0.3013	0.2843	0.1400
-0.0	-0.5523	2.3593	1.6447	1.1558	0.8279	0.6074	0.4611	0.3687	0.3177	0.3015	-0.1621

THETA	PHI=0.0	INSIDE SHEAR STRESS FACTORS								WITHOUT END EFFECTS	
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	
180.0	-0.0000	-0.0000	-0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0
157.5	-0.0047	0.0727	-0.1070	-0.3759	-0.6198	-0.7481	-0.7260	-0.5664	-0.3082	-0.0000	0.0
135.0	-0.2689	-0.4770	-0.7224	-0.8552	-0.8835	-0.8292	-0.7042	-0.5146	-0.2724	0.0000	0.0
112.5	-0.7923	-1.1843	-0.9729	-0.7002	-0.4371	-0.2260	-0.0849	-0.0122	-0.0079	-0.0000	0.0
90.0	-0.6568	-0.4503	-0.0586	0.1930	0.3333	0.3849	0.3631	0.2806	0.0079	-0.0000	0.0
67.5	0.3611	0.8431	0.8106	0.7176	0.5984	0.4710	0.3450	0.2246	0.1526	-0.0000	0.0
45.0	1.0272	1.1356	0.8247	0.5945	0.4226	0.2925	0.1931	0.2246	0.1104	0.0000	0.0
22.5	0.7752	0.6764	0.4442	0.2957	0.1986	0.1329	0.0866	0.1162	0.0543	0.0000	0.0
-0.0	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	0.0522	0.0246	-0.0000	0.0

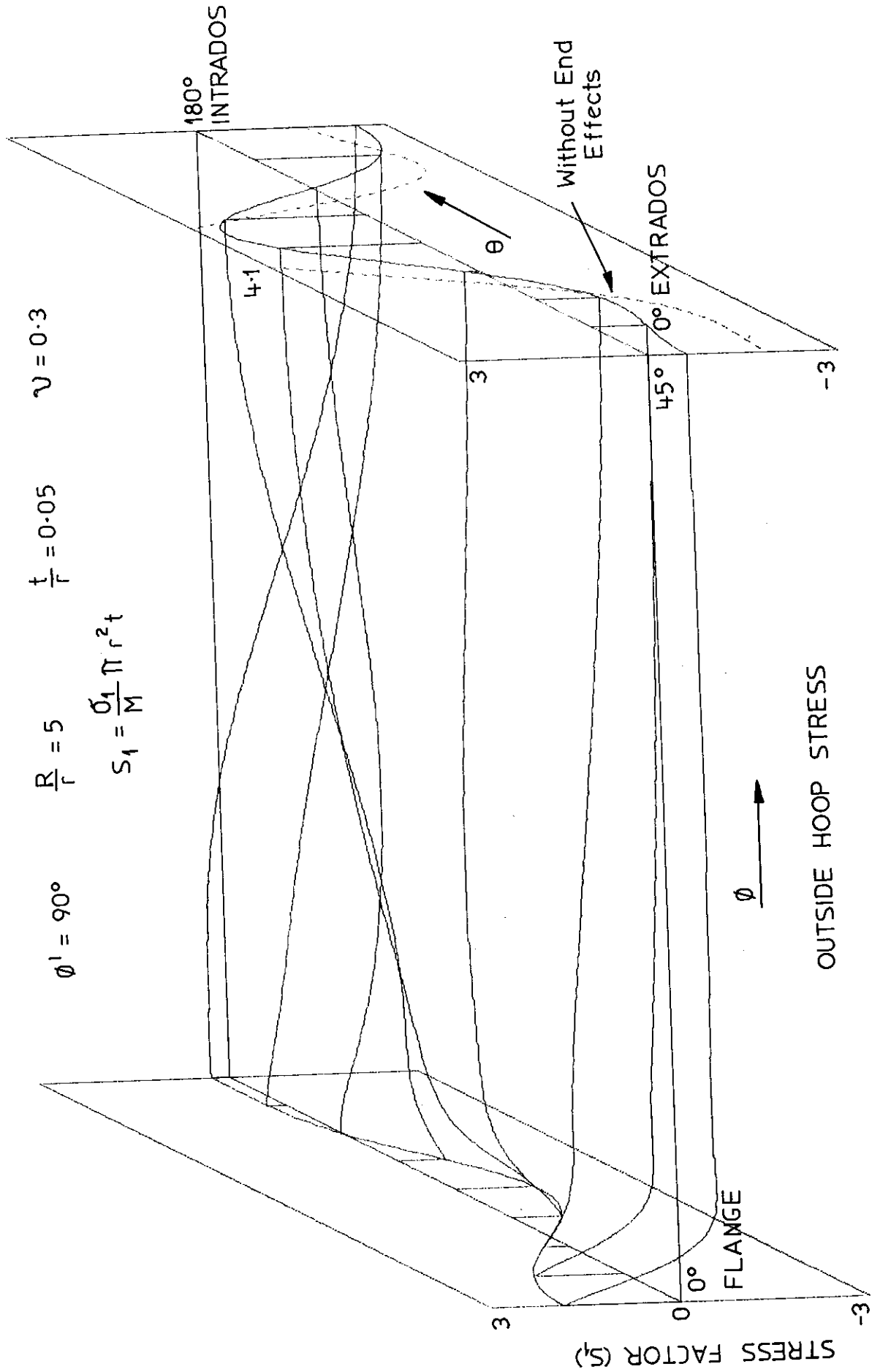


FIGURE A21

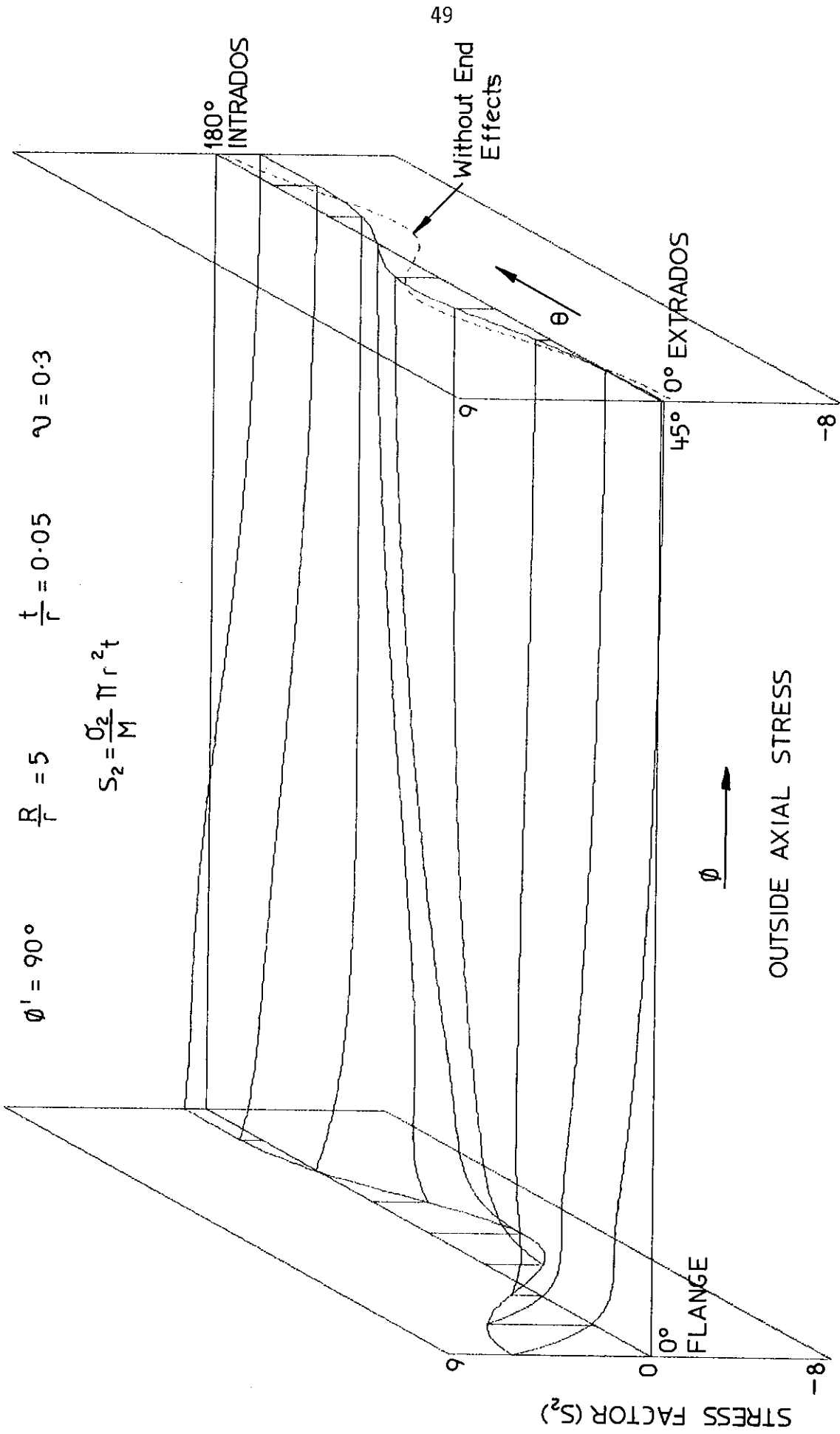


FIGURE A22

TABLE A21

R/r = 5.0 t/r = 0.05

THETA	PHI=0.0	OUTSIDE HOOP STRESS FACTORS								WITHOUT END EFFECTS			
		15.0	20.0	25.0	30.0	35.0	40.0	45.0	50.0	55.0	60.0	65.0	70.0
180.0	0.2880	0.0843	-0.5671	-1.1379	-1.6909	-2.1414	-2.4325	-2.5328	-1.7172				
157.5	0.2966	-0.5359	-0.8877	-1.2426	-1.5625	-1.8157	-1.9778	-2.0335	-2.2201				
135.0	0.0198	-0.8038	-0.7565	-0.6114	-0.4324	-0.2716	-0.1632	-0.1252	-1.6195				
112.5	-0.7404	0.2384	0.6657	1.1309	1.5696	1.9262	2.1580	2.2383	1.9449				
90.0	-1.2622	1.1214	1.4635	1.7435	1.9627	2.1218	2.2190	2.2518	4.1482				
67.5	-0.7969	0.5433	0.5299	0.4659	0.3799	0.2979	0.2401	0.2194	1.8438				
45.0	0.3749	-0.3684	-0.5249	-0.6779	-0.8141	-0.9218	-0.9910	-1.0149	-1.1647				
22.5	1.4392	-0.6516	-0.7290	-0.7885	-0.8314	-0.8600	-0.8763	-0.8816	-2.0043				
-0.0	1.8460	-0.6332	-0.6495	-0.6523	-0.6459	-0.6360	-0.6277	-0.6244	-1.9001				

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THETA	PHI=0.0	OUTSIDE AXIAL STRESS FACTORS								WITHOUT END EFFECTS			
		15.0	20.0	25.0	30.0	35.0	40.0	45.0	50.0	55.0	60.0	65.0	70.0
180.0	0.9599	0.0308	-0.5165	-1.0384	-1.4672	-1.7743	-1.9554	-2.0149	-0.3935				
157.5	0.9887	-0.5659	-0.9661	-1.3276	-1.6289	-1.8542	-1.9930	-2.0399	-1.1395				
135.0	0.0661	-1.4331	-1.5956	-1.5758	-1.5553	-1.5474	-1.5482	-1.5497	-2.4956				
112.5	-2.4681	-1.3540	-0.9587	-0.5763	-0.2473	0.0020	0.1563	0.2084	-1.6735				
90.0	-4.2075	0.1118	0.6404	1.0752	1.4241	1.6836	1.8447	1.8995	1.4342				
67.5	-2.6562	0.1152	0.6740	1.3459	1.6242	1.6945	1.7344	1.7474	2.7620				
45.0	1.2495	1.0515	0.9609	0.8613	0.7682	0.6933	0.6449	0.6282	1.4157				
22.5	4.7972	0.7954	0.5251	0.3225	0.1735	0.0703	0.0093	-0.0109	-0.0882				
-0.0	6.1534	0.7133	0.4036	0.1878	0.0397	-0.0570	-0.1118	-0.1295	-0.5706				

THETA	PHI=0.0	OUTSIDE SHEAR STRESS FACTORS								WITHOUT END EFFECTS			
		15.0	20.0	25.0	30.0	35.0	40.0	45.0	50.0	55.0	60.0	65.0	70.0
180.0	0.0000	0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	0.0				
157.5	-0.1255	-0.0703	0.0666	0.1606	0.1929	0.1658	0.0945	0.0000	0.0				
135.0	-0.3589	-0.0946	0.0109	0.0779	0.1041	0.0933	0.0542	-0.0000	0.0				
112.5	-0.5244	-0.1406	-0.1295	-0.1242	-0.1097	-0.0821	-0.0439	-0.0000	0.0				
90.0	-0.3049	-0.0953	-0.1245	-0.1411	-0.1358	-0.1068	-0.0587	-0.0000	0.0				
67.5	0.2207	0.1003	0.0518	0.0207	0.0029	-0.0044	-0.0042	0.0000	0.0				
45.0	0.5798	0.2433	0.1776	0.1320	0.0957	0.0632	0.0315	0.0000	0.0				
22.5	0.4686	0.1903	0.1401	0.1048	0.0765	0.0507	0.0254	0.0000	0.0				
-0.0	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000				

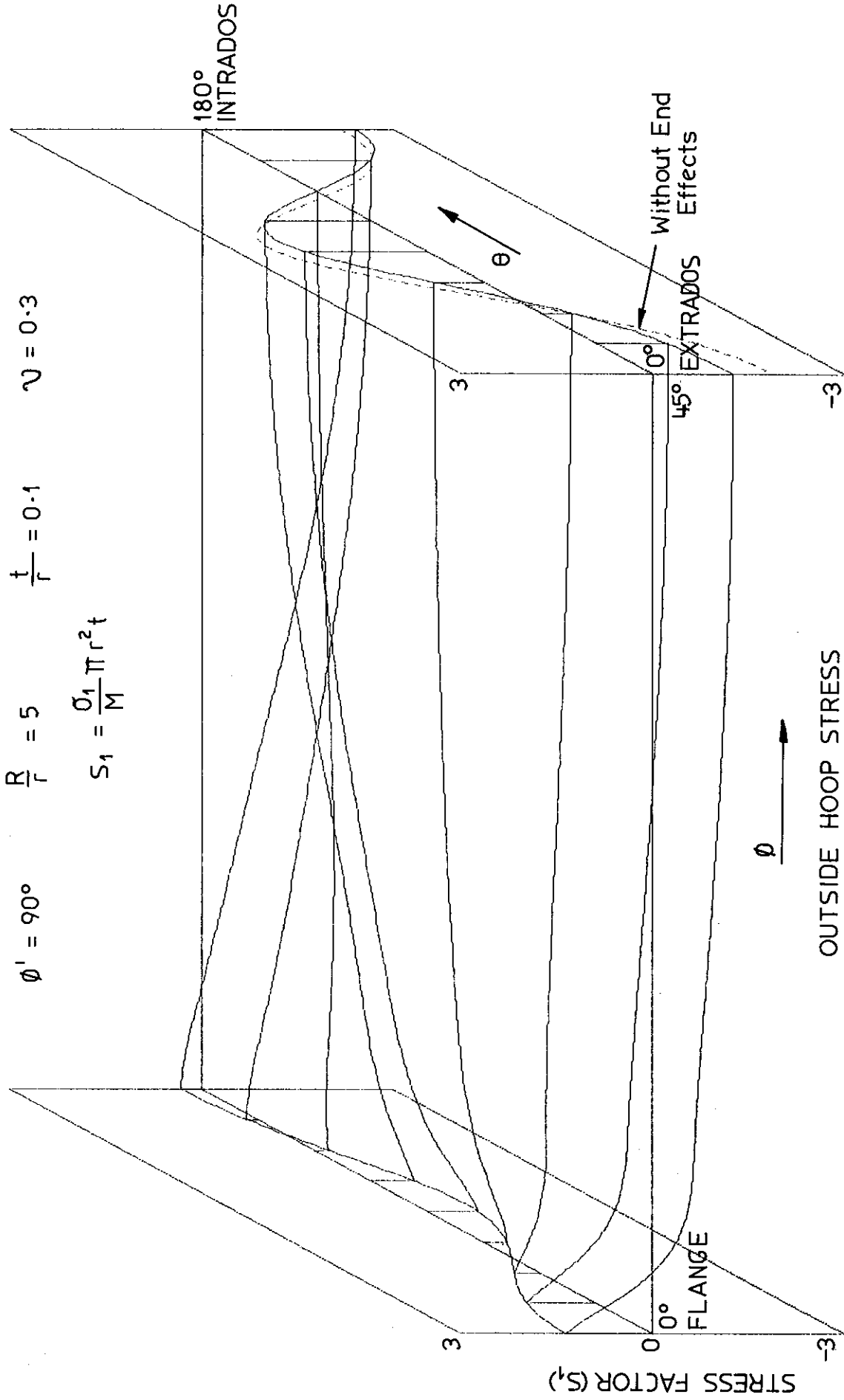


FIGURE A23

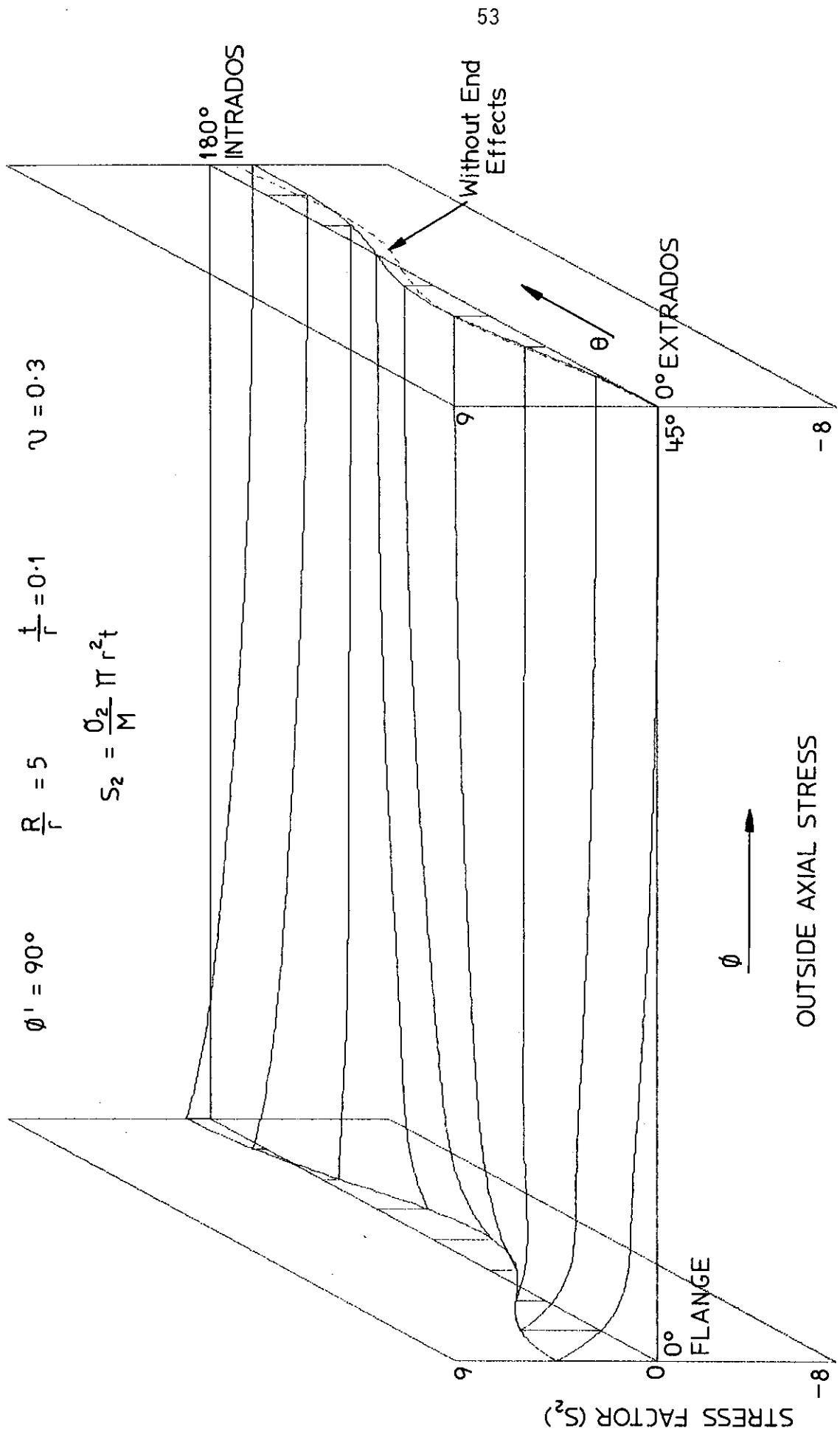


FIGURE A24

TABLE A23

R/r = 5.0 t/r = 0.10

THETA	PHI=0.0	OUTSIDE HOOP STRESS FACTORS								WITHOUT END EFFECTS	
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	54
180.0	0.3134	-0.0196	-0.4273	-0.8248	-1.2391	-1.6299	-1.9573	-2.1993	-2.3465	-2.3958	-2.1632
157.5	0.1780	-0.1195	-0.4593	-0.7478	-1.0221	-1.2717	-1.4786	-1.6316	-1.7251	-1.7565	-1.8049
135.0	-0.2174	-0.3006	-0.3006	-0.3011	-0.2493	-0.1837	-0.1238	-0.0788	-0.0515	-0.0425	-0.4198
112.5	-0.6744	-0.0845	0.2035	0.4758	0.7819	1.0730	1.3190	1.5032	1.6164	1.6545	1.5639
90.0	-0.7928	0.1460	0.5751	0.8737	1.1608	1.4159	1.6260	1.7829	1.8798	1.9126	2.3883
67.5	-0.3680	0.1523	0.3978	0.5117	0.5969	0.6617	0.7104	0.7457	0.7676	0.7750	1.3368
45.0	0.3937	-0.0944	-0.1153	-0.1753	-0.2541	-0.3309	-0.3978	-0.4490	-0.4809	-0.4917	-0.3864
22.5	1.0778	-0.3719	-0.5408	-0.6612	-0.7894	-0.9019	-0.9952	-1.0653	-1.1089	-1.1237	-1.5312
-0.0	1.3465	-0.4854	-0.6894	-0.8134	-0.9422	-1.0517	-1.1411	-1.2079	-1.2493	-1.2634	-1.8737

THETA	PHI=0.0	OUTSIDE AXIAL STRESS FACTORS								WITHOUT END EFFECTS	
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	54
180.0	1.0448	0.0538	-0.4617	-0.8831	-1.2534	-1.5393	-1.7362	-1.8587	-1.9240	-1.9443	-1.1114
157.5	0.5934	-0.3136	-0.7518	-1.0660	-1.3331	-1.5465	-1.7031	-1.8081	-1.8680	-1.8874	-1.4255
135.0	-0.7247	-0.9895	-1.1554	-1.1923	-1.2053	-1.2284	-1.2604	-1.2931	-1.3172	-1.3261	-1.6442
112.5	-2.2479	-1.1703	-0.9330	-0.6664	-0.4216	-0.2375	-0.1110	-0.0319	0.0103	0.0235	-0.7144
90.0	-2.6428	-0.6022	-0.1077	0.2853	0.6185	0.8790	1.0747	1.2113	1.2918	1.3184	0.8777
67.5	-1.2265	0.2430	0.6612	0.9170	1.1203	1.2794	1.4030	1.4930	1.5482	1.5668	1.6493
45.0	1.3125	0.8608	0.9852	0.9664	0.9467	0.9326	0.9245	0.9214	0.9209	0.9210	1.2039
22.5	3.5926	1.1444	0.9991	0.7542	0.5658	0.4257	0.3224	0.2512	0.2095	0.1957	0.3788
-0.0	4.4883	1.2147	0.9680	0.6417	0.3957	0.2142	0.0801	-0.0130	-0.0681	-0.0864	0.0116

THETA	PHI=0.0	OUTSIDE SHEAR STRESS FACTORS								WITHOUT END EFFECTS	
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0	54
180.0	0.0000	0.0000	0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	0.0
157.5	-0.1734	-0.1120	-0.0176	0.0892	0.1592	0.1834	0.1691	0.1270	0.0676	0.0000	0.0
135.0	-0.3110	-0.1379	-0.0366	0.0720	0.1397	0.1640	0.1530	0.1161	0.0622	0.0000	0.0
112.5	-0.3197	-0.1033	-0.0630	-0.0272	-0.0074	0.0031	0.0080	0.0084	0.0052	0.0000	0.0
90.0	-0.1436	-0.0239	-0.0417	-0.0753	-0.0960	-0.0998	-0.0882	-0.0649	-0.0342	-0.0000	0.0
67.5	0.1180	0.1004	0.0497	-0.0211	-0.0613	-0.0776	-0.0750	-0.0581	-0.0315	-0.0000	0.0
45.0	0.2754	0.1901	0.1274	0.0517	0.0098	-0.0124	-0.0209	-0.0196	-0.0115	-0.0000	0.0
22.5	0.2191	0.1525	0.1072	0.0582	0.0314	0.0155	0.0063	0.0017	0.0001	-0.0000	0.0
-0.0	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	0.0000	0.0

TABLE A24

R/r = 5.0 t/r = 0.10

THETA	PHI=0.0	INSIDE HOOP STRESS FACTORS								WITHOUT END EFFECTS			
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0			
180.0	-0.2648	-0.0037	0.1560	0.5028	0.9454	1.3858	1.7650	2.0504	2.2259	2.2850	2.1553		
157.5	-0.2837	0.0503	0.2342	0.4849	0.7688	1.0390	1.2687	1.4421	1.5494	1.5857	1.7682		
135.0	-0.2351	0.0518	0.1560	0.1209	0.0337	-0.0679	-0.1594	-0.2277	-0.2688	-0.2823	0.2374		
112.5	-0.0274	-0.1679	-0.3145	-0.6508	-1.0259	-1.3816	-1.6843	-1.9119	-2.0521	-2.0994	-1.9741		
90.0	0.1927	-0.4080	-0.6992	-1.0689	-1.4137	-1.7135	-1.9607	-2.1457	-2.2603	-2.2992	-2.8760		
67.5	0.2278	-0.3798	-0.5573	-0.6960	-0.7944	-0.8624	-0.9122	-0.9482	-0.9706	-0.9783	-1.6729		
45.0	0.0697	-0.1213	-0.1041	0.0025	0.1112	0.2158	0.3053	0.3727	0.4144	0.4285	0.2535		
22.5	-0.1301	0.1314	0.2532	0.4768	0.6595	0.8129	0.9363	1.0271	1.0829	1.1017	1.5097		
-0.0	-0.2167	0.2271	0.3707	0.6187	0.8091	0.9624	1.0827	1.1703	1.2238	1.2419	1.8790		

THETA	PHI=0.0	INSIDE AXIAL STRESS FACTORS								WITHOUT END EFFECTS			
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0			
180.0	-0.8827	-0.3111	-0.3003	-0.3074	-0.2359	-0.1250	-0.0102	0.0863	0.1497	0.1718	0.5764		
157.5	-0.9456	-0.4358	-0.4197	-0.4419	-0.4161	-0.3639	-0.3067	-0.2576	-0.2247	-0.2133	0.1343		
135.0	-0.7836	-0.7355	-0.6966	-0.7229	-0.7652	-0.8082	-0.8484	-0.8809	-0.9017	-0.9088	-0.8310		
112.5	-0.0915	-0.9354	-0.8161	-0.7733	-0.7974	-0.8454	-0.9012	-0.9513	-0.9854	-0.9975	-1.3302		
90.0	0.6422	-0.6987	-0.4750	-0.3316	-0.2699	-0.2421	-0.2340	-0.2358	-0.2400	-0.2419	-0.7305		
67.5	0.7592	0.0020	0.1858	0.3356	0.4279	0.4949	0.5435	0.5766	0.5958	0.6021	0.3451		
45.0	0.2323	0.8422	0.7678	0.7920	0.8113	0.8297	0.8478	0.8628	0.8728	0.8763	0.9476		
22.5	-0.4336	1.4657	1.0747	0.9408	0.8543	0.7936	0.7534	0.7283	0.7147	0.7103	0.9630		
-0.0	-0.7222	1.6883	1.1574	0.9546	0.8210	0.7244	0.6574	0.6134	0.5884	0.5803	0.8759		

THETA	PHI=0.0	INSIDE SHEAR STRESS FACTORS								WITHOUT END EFFECTS			
		5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0			
180.0	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0000	0.0		
157.5	-0.1569	-0.4066	-0.4690	-0.4538	-0.3955	-0.3147	-0.2286	-0.1466	-0.0711	-0.0000	0.0		
135.0	-0.2814	-0.6659	-0.6555	-0.5850	-0.4944	-0.3929	-0.2894	-0.1891	-0.0931	-0.0000	0.0		
112.5	-0.2892	-0.5285	-0.4124	-0.3168	-0.2492	-0.1950	-0.1460	-0.0980	-0.0493	-0.0000	0.0		
90.0	-0.1299	-0.0008	0.0807	0.1140	0.1131	0.0943	0.0694	0.0443	0.0213	0.0000	0.0		
67.5	0.1068	0.5345	0.4619	0.3986	0.3333	0.2652	0.1971	0.1302	0.0647	0.0000	0.0		
45.0	0.2492	0.7136	0.5309	0.4206	0.3357	0.2619	0.1939	0.1295	0.0641	0.0000	0.0		
22.5	0.1982	0.4782	0.3306	0.2507	0.1946	0.1496	0.1101	0.0729	0.0364	0.0000	0.0		
-0.0	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	-0.0000	0.0		

